Central matter distributions in rich clusters of galaxies from \( z \sim 0 \) to \( z \sim 0.5 \)

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Abstract. We have analyzed the galaxy number density and luminosity density profiles of rich clusters of galaxies from redshifts \( z \sim 0 \) to \( z \sim 0.5 \). We show that the luminosity profile computed with bright galaxies \( (M_R < -21) \) is significantly cusped in the center of the clusters, whatever the redshift. This is in agreement with the dark matter profiles predicted by numerical simulations. The galaxy number density profile for the bright galaxies is fitted equally well with a core model or a cusped model. In contrast, the luminosity and the galaxy number density profiles of the fainter galaxies are significantly better fitted by a core model. We did not detect any statistically significant different fits when applied to data in the range from \( z \sim 0 \) to \( z \sim 0.5 \). The difference in profile between faint and bright galaxies may be due to the rapid (relative to the age of the universe at \( z = 0 \) versus \( z = 0.5 \)) destruction of the faint galaxies by tidal forces and merging events in the denser central regions of the clusters. This process could erase the cusp by turning faint galaxies into diffuse light. In this case, the galaxies (with a cusp visible in the bright galaxy number density and mainly in luminosity profiles) would trace the total mass distribution.

Key words. galaxies: clusters: general – cosmology: large-scale structure of Universe

1. Introduction

Clusters of galaxies are key cosmological probes. They are one of the main products of the hierarchical models and the largest virialized structures in the Universe. Recent studies (e.g. Navarro et al. 1997) argue that whatever the cosmological model, a universal profile (NFW profile) with a cusp at the center should describe the cluster dark matter profile, in contrast to the beta-model (King 1962) used from many years (cf. Sarazin 1986). The shape of the galaxy number and luminosity density profiles (and their dependence on redshift) relates directly to the physical processes acting at the center of the clusters and we propose to investigate in this way these processes. While the dark matter profile (close to the total mass profile) seems to be very concentrated (Navarro et al. 1997), the galaxy distribution is nearly flat in the center of the nearby clusters (Adami et al. 1998c: ENACSVII). Furthermore, the X-ray gas distribution cannot be used to distinguish between a flat and a cusped model, except for the nearby clusters (e.g. Durret et al. 1994), due to a lack of resolution with Rosat, Einstein and Asca and due to cooling-flows.

In this paper we study the galaxy number density profile and the galaxy luminosity density profile (the sum of the luminosity inside the galaxies). This approach is clearly not new (e.g. Mazure et al. 1986), but we used here very large, homogeneously analyzed, samples. The use of all the optical wave band galaxy light allows us to take into account merging events. This method enables us to recover “erased” cusps as it is the light of merged galaxies which is counted, not the number of galaxies. The best way to investigate the mass profile would be to compute this profile via the velocity dispersion profile (e.g. Carlberg et al. 1997a,1997b; Biviano et al. 2001), the X-ray temperature profile, or gravitational lensing, but these techniques require large amounts of data, and therefore, it is very difficult to obtain large samples of clusters. Moreover, galaxy luminosity density profiles for early type galaxies are claimed (e.g. Kaiser 1999) to be similar to the mass profile in clusters. This is an important question, as galaxies would be sufficient to trace the mass profile. We will use in this paper homogeneous samples of thousands of galaxies and tens of clusters to compare the projected galaxy number density and luminosity profiles, and the simulated dark matter profiles (e.g. Navarro et al. 1997).
In Sect. 2, we describe the samples. In Sects. 3 and 4, we describe the methods we used and the profiles we generated. Section 5 discusses the results and Sect. 6 gives a summary of the results.

To relate values of \( z \) to distance and to be in agreement with Adami et al. (1998c, ENACSVII), we have taken \( H_0 = 100 \text{ km s}^{-1} \text{ Mpc}^{-1}, q_0 = 0 \) and \( \Lambda = 0 \).

2. Samples
2.1. Low redshift sample
We used the COSMOS composite cluster (see ENACSVII), but we briefly enumerate the main points here: we compiled photometric COSMOS data (Heydon-Dumbleton et al. 1989) for 77 of the 107 ENACS clusters \((z \leq 0.1)\). We adopted a limiting magnitude of \( b_j = 20 \).

We selected the clusters with:
1. a low level of substructure (both visually and with a Dressler-Sheetman test) in a 10 core radii on a side square (\( \sim 1200 \text{ kpc h}^{-1} \)), with more than 10 known redshifts in the main group (to avoid superposition effects);
2. a redshift lower than 0.1;
3. and a converging solution of the fit of analytical density profiles.

These selection criteria lead to a sample of 29 homogeneously selected clusters. With this sample we built a composite cluster with about 5000 galaxies. For each of the 29 clusters, we determined the center by a Maximum Likelihood fit. We can easily generalize the same code to fit a luminosity profile for the composite clusters.

2.2. High redshift sample
We used a sample of 7 clusters from the COP (Adami et al. 2000a; Holden et al. 2000) and CNOC (e.g. Carlberg et al. 1996) surveys selected with the same conditions as the low redshift sample:
1. low level of substructures in a 10 core radii square (\( \sim 1200 \text{ kpc} \)) from visual analysis;
2. more than 10 redshifts in the main group;
3. converging solutions of the fit of analytical galaxy number and luminosity density profiles (this excludes 2 clusters: MS 1008 and MS 1224). This sample is described in Table 1: the redshift range of this sample of distant clusters is \([0.33; 0.55]\) (mean redshift = 0.42). We have built a composite cluster of 459 galaxies with these 7 clusters, correcting for ellipticity and orientation of each real cluster.

We note that MS 1358 is regarded in the CNOC papers as a complex cluster. However, we used in this paper only the central regions of this cluster in order to focus on the central cluster shape: we limited this cluster to a region of \( \sim 160^\prime^\prime \) radius. With this restriction, MS 1358 can be included in our sample. We stress, however, that using larger areas will induce significant levels of substructures.

3. Methods and results
3.1. Low redshift galaxy number density and luminosity profiles
The individual parameters (with individual clusters) of the low redshift sample profiles are described in Adami et al. (1998b; ENACSVII). They have been computed with a Maximum Likelihood fit. We can easily generalized the same code to fit a luminosity profile for the composite clusters.

We weighted each galaxy with its luminosity (assuming all the galaxies at the cluster redshift): \( \text{Lum}_k \). Similar to ENACSVII, the probability that the assumed profile “produces” a galaxy in position \((x_k, y_k)\) is \( \sigma(x_k, y_k) \) (with \( k = 1...N \)). The combined probability that the assumed profile will produce galaxies in the positions \((x_k, y_k)\) that they actually have is:

\[
L = \prod_{k=1}^{N} \text{Lum}_k \times \sigma(x_k, y_k).
\]

The best fit model is found from a maximization of \( L \). We have chosen, instead, to compute \(-\ln(L)\) with:

\[
\ln L = \sum_{k=1}^{N} \ln(\text{Lum}_k \times \sigma(x_k, y_k)).
\]

The best model (which produces the best fit) is found from a minimization of \(-\ln(L)\), using the MINUIT package (e.g. ENACSVII for details).

To be able to quantify the degree of cuspiness at the center of the clusters, we fitted in ENACSVII both a projected beta-model:

\[
\mu(r) = \mu_0 \left( 1 + \left( \frac{r}{r_c} \right)^2 \right)^{-\beta} + \mu_b,
\]

and a cusped profile:

\[
\mu(r) = \mu_0 \left( \frac{r}{r_c} \left( 1 + \frac{r}{r_c} \right)^2 \right)^{-\beta} + \mu_b.
\]
For the luminosity profiles, $\mu$ is the surface brightness, which replaces the surface density $\sigma$ of the formulae in ENACSVII. These models, fitted to the individual clusters, have 7 free parameters: two for the position of the center ($x_0$, $y_0$), two to describe deviations from symmetry (ellipticity $e$ and position angle $\phi$, included in $\epsilon$), two that specify the profile ($r_c$ and $\beta$) and the background density $\mu_b$ (assumed constant within the aperture of each cluster).

To be able to compare the fit quality of the two models (cusped profile and beta-model), we use the logarithm of the ratio of the Maximum Likelihood values for each fit as explained in ENACSVII. This value has a $\chi^2$ distribution (Meyer 1975) which we then use to determine the statistical significance level of the best fit of one profile type versus the other.

Moreover, we have checked the consistency between the center of the clusters determined using the galaxies (see ENACSVII) and the center determined using the galaxies weighted with their luminosity. We find a shift of only $(32 \pm 21)$ kpc. This shift is not large enough to erase a cusp (e.g. ENACSVII Fig. 8) and we have assumed the centers using only the galaxy number density.

### 3.2. High redshift galaxy number density and luminosity profiles

We used a similar approach as for the low redshift sample, but with an additional step to take into account the high background level. It is nearly impossible to measure redshifts for all galaxies of all the clusters in our high redshift sample, due to the large amount of observing time needed. Therefore, we used the red sequences in the Color Magnitude Relations (CMR hereafter) to reject many of the field galaxies along the lines of sight (e.g. Yee et al. 1999).

The color intervals we used are given in Table 1. We chose these intervals manually in order to match the prominent structures in the CMR of each line of sight. We have confidence that we made a good choice of intervals as these intervals are very similar to the theoretical predictions of Kodama & Arimoto (1997).

We give in Table 1 the best fit values of $r_c$ and $\beta$ for the 7 high redshift clusters, the 2 analytical models (beta-model and cusped profile) and the galaxy number and luminosity density profiles parameters ($r_c$ is ranging from 63 to 299 kpc and $\beta$ from 0.8 to 1.04 for a beta-model). We give also the fit quality: which analytical model fits best, core or cusp?

We now examine whether these values could have been affected by the following bias: the CMR rejects not only field galaxies but also the late-type galaxies that are cluster members. Since these galaxies are preferentially located in the outskirts of clusters (e.g. Adami et al. 1998a), this could affect the density profiles.

- At low redshift, this is not a serious concern as more than 75% of the cluster galaxies in a 1200 $h^{-1}$ kpc square are early-type objects (Adami et al. 1998a);

- For the higher redshift clusters, however, the spiral fraction increases (e.g. Dressler et al. 1997) and can contribute up to 60% in the outer parts of the clusters (Ellingson et al. 2000). As we want to focus on the central cluster shape, we limited ourselves to a region of $0.5r_{200}$ (5 core radii). In this region, the field-like galaxy contribution is lower: $\sim 30\%$. We have tested, however, the significance of the effect by removing these galaxies when we fit the density profiles. We used the CNOC cluster MS 1358 because redshifts are available for nearly all the galaxies along the line of sight. We can, therefore, select the cluster member galaxies on a firm basis. We see in Table 1 that using the CMR or the redshift selection does not affect in a significant manner the fitted parameters: these parameters are similar at the 1-$\sigma$ level: for a beta-model $r_c$ is ranging from 117 to 95 kpc and $\beta$ from 0.91 to 0.98. This is not a definitive test as we are using a single cluster, but the results are still very suggestive.

Using the CMR seems, therefore, a good way to remove field galaxies in order to discriminate between cusped profiles and profiles with a core. However, as we go to faint magnitudes, the uniform field contribution becomes stronger. This field contribution is between 50% and 75% for the clusters in our sample (estimated from the redshift catalogs of these cluster lines of sight). This could have the effect that the cluster density profiles will appear flatter for faint galaxies.

- This does not affect our results for nearby clusters (we do not sample the clusters at magnitudes fainter than $R = 19$, where the CMR becomes to be less contrasted compared to the field contribution: Adami et al. 2000b);

- This does not affect our results for distant clusters ($z \sim 0.4$) for the brightest bin of Table 3 (magnitudes brighter than $R = 19$);

- This could have an influence for the 3 faintest bins of the distant composite cluster. However, the goal of this...
Table 1. High redshift sample with cluster name, selection of the cluster galaxies (color interval or redshift), redshift, characteristic radius and $\beta$ for the beta-model (galaxy number density profile: dens. gal.), characteristic radius and $\beta$ for the cusped model (galaxy number density profile: dens. gal.), characteristic radius and $\beta$ for the beta-model (galaxy luminosity profile: dens. lum.), characteristic radius and $\beta$ for the cusped model (galaxy luminosity profile: dens. lum.) and best fit (galaxy number and luminosity density profiles). The quoted errors are at the 1-$\sigma$ level. No error means that we were not able to get a reliable estimate for this error.

<table>
<thead>
<tr>
<th>Name</th>
<th>Selection</th>
<th>$z$</th>
<th>$r_c$ dens. gal. beta-model</th>
<th>$\beta$ dens. gal. beta-model</th>
<th>$r_c$ dens. gal. cusped</th>
<th>$\beta$ dens. gal. cusped</th>
<th>best fit dens. gal.</th>
<th>best fit dens. lum.</th>
</tr>
</thead>
<tbody>
<tr>
<td>MS 0332</td>
<td>$g - R$: [1.00, 1.80]</td>
<td>0.42</td>
<td>63 $\pm$ 12 kpc</td>
<td>0.93 $\pm$ 0.06</td>
<td>93 $\pm$ 32 kpc</td>
<td>0.52 $\pm$ 0.04</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>62 $\pm$ 12 kpc</td>
<td>0.94 $\pm$ 0.09</td>
<td>94 $\pm$ 29 kpc</td>
<td>0.52 $\pm$ 0.05</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td>MS 0451</td>
<td>$g - R$: [1.25, 1.85]</td>
<td>0.54</td>
<td>121 $\pm$ 32 kpc</td>
<td>0.87 $\pm$ 0.17</td>
<td>209 $\pm$ 108 kpc</td>
<td>0.53 $\pm$ 0.07</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>117 $\pm$ 29 kpc</td>
<td>0.88 $\pm$ 0.16</td>
<td>210 $\pm$ 120 kpc</td>
<td>0.53 $\pm$ 0.08</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td>MS 1358</td>
<td></td>
<td></td>
<td>117 $\pm$ 26 kpc</td>
<td>0.98 $\pm$ 0.09</td>
<td>455 $\pm$ 97 kpc</td>
<td>0.81 $\pm$ 0.05</td>
<td>cusped: not significant</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>119 $\pm$ 29 kpc</td>
<td>0.99 $\pm$ 0.08</td>
<td>469 $\pm$ 95 kpc</td>
<td>0.81 $\pm$ 0.05</td>
<td>cusped: not significant</td>
<td></td>
</tr>
<tr>
<td>MS 1358</td>
<td>$g - R$: [1.02, 1.50]</td>
<td></td>
<td>95 $\pm$ 22 kpc</td>
<td>0.91 $\pm$ 0.07</td>
<td>516 $\pm$ 172 kpc</td>
<td>0.83 $\pm$ 0.06</td>
<td>cusped: not significant</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>101 $\pm$ 13 kpc</td>
<td>0.92 $\pm$ 0.04</td>
<td>509 $\pm$ 151 kpc</td>
<td>0.83 $\pm$ 0.05</td>
<td>cusped: not significant</td>
<td></td>
</tr>
<tr>
<td>MS 1621</td>
<td>$g - R$: [0.85, 1.85]</td>
<td>0.43</td>
<td>67 kpc</td>
<td>0.80</td>
<td>735 kpc</td>
<td>0.86</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>68 kpc</td>
<td>0.81</td>
<td>737 kpc</td>
<td>0.85</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td>PDCS16</td>
<td>$V - I$: [1.35, 2.11]</td>
<td>0.40</td>
<td>299 $\pm$ 39 kpc</td>
<td>0.99 $\pm$ 0.20</td>
<td>882 kpc</td>
<td>0.68</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>303 $\pm$ 36 kpc</td>
<td>0.98 $\pm$ 0.18</td>
<td>885 kpc</td>
<td>0.67</td>
<td>beta-model: not significant</td>
<td></td>
</tr>
<tr>
<td>PDCS30</td>
<td>$V - I$: [1.10, 1.90]</td>
<td>0.33</td>
<td>189 kpc</td>
<td>1.04</td>
<td>302 $\pm$ 67 kpc</td>
<td>0.53 $\pm$ 0.04</td>
<td>beta-model: 85% level</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>189 kpc</td>
<td>1.01</td>
<td>227 $\pm$ 69 kpc</td>
<td>0.46 $\pm$ 0.03</td>
<td>beta-model: 85% level</td>
<td></td>
</tr>
<tr>
<td>PDCS62</td>
<td>$V - I$: [1.24, 2.20]</td>
<td>0.46</td>
<td>196 $\pm$ 10 kpc</td>
<td>1.01 $\pm$ 0.26</td>
<td>284 $\pm$ 73 kpc</td>
<td>0.53 $\pm$ 0.04</td>
<td>beta-model: 85% level</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>192 kpc</td>
<td>1.02</td>
<td>282 $\pm$ 71 kpc</td>
<td>0.53 $\pm$ 0.03</td>
<td>beta-model: 85% level</td>
<td></td>
</tr>
</tbody>
</table>

The paper is to discriminate between density profiles with a cusp or with a core. In order to quantify the probability of a cusped profile mis-interpreted as a profile with a core due to a high field contribution, we performed simulations. We generated a circular artificial cluster profile with a cusp in the center (as described in Sect. 3.1 with $r_c = 200$ kpc and $\beta = 0.67$) and we added to this cluster a uniform field contribution with various galaxy densities. We finally computed the relative fit quality between a profile with a core and with a cusp. For field contributions as high as 80% of the total number of galaxies along the line of sight, a model with a cusp is preferred at the 80% significance level. For contributions equal to 85%, a model with a cusp is preferred at the 70% significance level. For higher field contributions, we are not able to discriminate between a profile with a core or with a cusp (a model with a cusp is still preferred but with significance levels lower than 65%, which is not significant). The results are plotted in Fig. 1. This means that even with a high field contribution, we are still able to discriminate between profiles with a core or with a cusp because the field contribution along the lines of sight we used is not higher than 80%. Our results are, therefore, valid regarding the core/cusp discrimination.

3.3. Analysis of the results

- We compare the characteristic parameters $r_c$ and $\beta$ of the distant clusters with those of the nearby sample (ENACSVII). Table 2 first used the individual clusters. We do not see a statistically significant evolution with redshift: the agreement between $z \approx 0$ and $z \approx 0.4$ is consistent at the 2-$\sigma$ level (for a beta-model, individual clusters and galaxy number density, $r_c \approx 130$ kpc and $\beta \approx 1$). If we compare now the fitted parameters $r_c$ and $\beta$ of the galaxy number and luminosity density profiles (regardless of the redshift), they also agree at the 2-$\sigma$ level (for a beta-model, composite clusters and luminosity profiles, $r_c \approx 110$ kpc and $\beta \approx 1.05$);

- As for the nearby sample (e.g. ENACSVII), the cluster galaxy distribution of the distant cluster sample is
Table 2. Galaxy number density and luminosity profile parameters (characteristic radius $r_c$ and slope $\beta$) for nearby and distant clusters. The values for the individual cluster galaxy number density profiles are the mean and the 1-$\sigma$ uncertainty between the individual fits. The values for the composite clusters are the fitted values. No error means that we were not able to get a reliable estimate for this error.

<table>
<thead>
<tr>
<th>DENSITY</th>
<th>$r_c$ beta-model</th>
<th>$r_c$ cusped</th>
<th>$\beta$ beta-model</th>
<th>$\beta$ cusped</th>
<th>best fit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nearby sample ($z \sim 0.07$) (Individual clusters)</td>
<td>$&lt;128 &gt; \pm 88$ kpc</td>
<td>$&lt;292 &gt; \pm 191$ kpc</td>
<td>$&lt;1.02 &gt; \pm 0.08$</td>
<td>$&lt;0.61 &gt; \pm 0.05$</td>
<td>beta-model</td>
</tr>
<tr>
<td>Distant sample ($z \sim 0.4$) (Individual clusters)</td>
<td>$&lt;147 &gt; \pm 79$ kpc</td>
<td>$&lt;431 &gt; \pm 268$ kpc</td>
<td>$&lt;0.94 &gt; \pm 0.08$</td>
<td>$&lt;0.64 &gt; \pm 0.14$</td>
<td>beta-model</td>
</tr>
<tr>
<td>Nearby sample ($z \sim 0.07$) (Composite cluster)</td>
<td>89 $\pm$ 5 kpc</td>
<td>318 $\pm$ 34 kpc</td>
<td>1.00 $\pm$ 0.02</td>
<td>0.56 $\pm$ 0.01</td>
<td>beta-model</td>
</tr>
<tr>
<td>Distant sample ($z \sim 0.4$) (Composite cluster)</td>
<td>119 $\pm$ 8 kpc</td>
<td>215 $\pm$ 9 kpc</td>
<td>1.08 $\pm$ 0.05</td>
<td>0.65 $\pm$ 0.04</td>
<td>beta-model</td>
</tr>
</tbody>
</table>

LUMINOSITY

<table>
<thead>
<tr>
<th>$r_c$ beta-model</th>
<th>$r_c$ cusped</th>
<th>$\beta$ beta-model</th>
<th>$\beta$ cusped</th>
<th>best fit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nearby sample ($z \sim 0.07$) (Composite cluster)</td>
<td>101 $\pm$ 7 kpc</td>
<td>281 $\pm$ 41 kpc</td>
<td>1.01 $\pm$ 0.03</td>
<td>0.58 $\pm$ 0.03</td>
</tr>
<tr>
<td>Distant sample ($z \sim 0.4$) (Composite cluster)</td>
<td>119 $\pm$ 9 kpc</td>
<td>232 kpc</td>
<td>1.08 $\pm$ 0.04</td>
<td>0.66</td>
</tr>
</tbody>
</table>

better fitted with beta-models than with cusped profiles. Although the fit is better, it is not significantly better than a 75% significance level:

- To improve the statistical significance of the fits in order to distinguish between cusped profile and beta-profile fits, we used also composite clusters. The method used to build these composite clusters is described in Sect. 2.1. We found that the behavior of the fits was similar for the distant and nearby samples: the bright galaxies better followed a cusped luminosity profile, while the faint galaxy luminosity and galaxy number density profiles were better fitted with beta-models. This is also illustrated for the nearby sample with Fig. 2. We see that the bright galaxy luminosity density profile seems to be more peaked than for the fainter galaxies.

4. Cores or cusps: Comparison with literature

We have analyzed in this paper a very large sample of clusters and we have shown that we have a better fit for the galaxy number density if we used a model with a core rather than with a cusp (except for the bright galaxies). This is apparently contrary to the study of Carlberg et al. (1997a) which favored a model with a cusp for the galaxies of the CNOC clusters. We have shown in ENACSVII, however, that the results of Carlberg et al. are probably explained because Carlberg et al. did not correct for ellipticity of the cluster profiles, and more importantly, they only considered bright galaxies.

We have shown that if we limit ourselves to bright galaxies (see Table 3), there is no statistically significant difference between a model with a cusp or with a core for the galaxy number density. This result is in good agreement, for example, with the work of Biviano et al. (1996) on the Coma cluster.

We note that Durret et al. (1994) showed that, using the X-ray surface brightness profile of 12 clusters (based on ROSAT data), a model with a core does not fit significantly better the observations than a model with a cusp.

If we fit the luminosity density profiles for all galaxies with a beta-model and a cusped model, the core model is still preferred, but the difference is not significant over the redshift range from 0 to 0.5. For a comparison, we have plotted in Fig. 3 the ratio of the galaxy luminosity density to the galaxy number density (for the 4 luminosity bins).
Table 3. Best fit for the different models and composite clusters

<table>
<thead>
<tr>
<th>Nearby composite cluster</th>
<th>Luminosity density profile</th>
<th>Galaxy number density profile</th>
</tr>
</thead>
<tbody>
<tr>
<td>All galaxies, $r_c$ scaled</td>
<td>beta-model better than cusp: not significant</td>
<td>beta-model better than cusp 99% level</td>
</tr>
<tr>
<td>All galaxies, $r_{200}$ scaled</td>
<td>beta-model better than cusp: not significant</td>
<td>beta-model better than cusp 99% level</td>
</tr>
<tr>
<td>$b_1 = -22.4; -18.78$, $r_c$ scaled</td>
<td>cusp better than beta-model 95% level</td>
<td>beta-model better than cusp 95% level</td>
</tr>
<tr>
<td>$b_2 = -18.77; -18.03$, $r_c$ scaled</td>
<td>beta-model better than cusp 95% level</td>
<td>beta-model better than cusp 95% level</td>
</tr>
<tr>
<td>$b_3 = -18.02; -17.48$, $r_c$ scaled</td>
<td>beta-model better than cusp 75% level</td>
<td>beta-model better than cusp 95% level</td>
</tr>
<tr>
<td>$b_4 = -17.47; -16.89$, $r_c$ scaled</td>
<td>beta-model better than cusp 75% level</td>
<td>beta-model better than cusp 75% level</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Distant composite cluster</th>
<th>Luminosity density profile</th>
<th>Galaxy number density profile</th>
</tr>
</thead>
<tbody>
<tr>
<td>All galaxies, $r_c$ scaled</td>
<td>beta-model better than cusp 85% level</td>
<td>beta-model better than cusp 85% level</td>
</tr>
<tr>
<td>$R = -22.; -21.$, $r_c$ scaled</td>
<td>cusp better than beta-model 95% level</td>
<td>beta-model better than cusp 95% level</td>
</tr>
<tr>
<td>$R = -21.; -20.5$, $r_c$ scaled</td>
<td>beta-model better than cusp 95% level</td>
<td>beta-model better than cusp 95% level</td>
</tr>
<tr>
<td>$R = -20.5; -20.$, $r_c$ scaled</td>
<td>cusp better than beta-model: not significant</td>
<td>cusp better than beta-model: not significant</td>
</tr>
<tr>
<td>$R = -20.; -19.$, $r_c$ scaled</td>
<td>beta-model better than cusp 70% level</td>
<td>beta-model better than cusp 70% level</td>
</tr>
</tbody>
</table>

Fig. 3. Log of the ratio of the luminosity profiles and the galaxy number density profiles for the $r_c$ scaled nearby composite clusters (assuming $r_c \approx 100$ kpc) and the four magnitude ranges

We see that the ratio is constant for the faintest bins, while we have an increasing ratio for the brightest bin close to the center, inside $\approx 50$ kpc. As we have noted in previous sections, there seems to be a difference between the distribution of bright and faint galaxies and also between galaxy number density profile and the luminosity density profile. It seems that two different shapes apply. The faint galaxies exhibit a core. They have a distribution in agreement with a beta-model. The bright galaxies (at least for the luminosity profile) show a cusp. This would be in agreement with the dark matter profiles of the simulations of Navarro et al. (1997). As suggested by Kaiser (1999), the bright galaxies would, therefore, trace the cluster mass.

5. Discussion

We have presented different arguments favoring either a core or cusp model. The galaxy number density profiles do not exhibit a cusp, and the bright galaxies cannot be used to distinguish between models. On the contrary, the luminosity profiles can be used to produce a cusp or a core depending on whether just bright or faint galaxies are used to generate the luminosity density profile. This leads to suggest different scenarios for the evolution of the bright and faint objects:

- the bright galaxies luminosity profile could be cusped at the formation epoch of the clusters. It could also become cusped via evolutionary processes, such as a segregation process (bright galaxies in the center of the clusters);
- the faint galaxies, which exhibit a core, could originally have been in a cusped distribution, but this distribution erased by environmental effects such as tidal disruption or merging events. Galaxies near the cluster center and on radial orbits with low angular momentum would have to pass through the giant ellipticals and eventually would be swallowed up or disrupted in the process. This can lead to a lower density of faint galaxies near the cluster center.

5.1. Segregation effects

We examine if the luminosity profile cusp for bright galaxies is due to a segregation effect. In Adami et al. (1998a) it was shown that the elliptical galaxies are the brightest objects in a cluster. Moreover, they are more concentrated in the cluster centers than the other morphological types. This probably explains why we are not able to distinguish between a core and a cusp when we examine the galaxy number density profile of the bright galaxies (ENACSVII): bright galaxies are mainly elliptical and elliptical galaxies are mainly in the cluster centers.

To confirm this effect, we have removed the galaxies brighter than $b_1 = -21$ from the brightest bin of the nearby sample (28 galaxies). This removes the cD-like galaxies. When re-doing the fit of a beta-model and a cusped profile for the bright galaxy bin with the cDs removed, we still prefer a model with a cusp, with, however, at a lower significance level of 90% (instead of 95%). This effect does not appear, however, to be dominant.
We now discuss the difference between the galaxy number density and the luminosity profiles. A cusp in the galaxy number density profile could be erased by merging events, leading to a core. However, the luminosity profile of the bright galaxies has a cusp, but the same profile for the faint galaxies has a core. We discuss a scenario that would explain this result in the next subsection.

5.2. Destruction of the faint galaxies in the center of the clusters?

Suppose that the formation mechanism of the clusters does not initially produce a core, but only a cusp for both bright and faint galaxies, as in the simulations (e.g. Navarro et al. 1997). This cusp could be “erased” in the galaxy number density profile by merging events and “revealed” in the luminosity profile for the bright galaxies. We must now explain why the luminosity profile for the faint galaxies has no cusp. This could be explained if we consider the tidal disruptions. Tidal forces in the cluster center disrupt part of the faint galaxies, turning them into diffuse light, while the bright ones (more massive and more robust) are conserved. This explanation was, for example, proposed by Merrit (1984). By using simulations of the dynamical evolution of the cluster core, he predicted a tidal radius (lowest value for the size of a not tidally disrupted galaxy) of about $15h^{-1}$ kpc. The bright galaxies, like cD galaxies, are significantly larger. The cusp could be erased in this way only for the faint galaxies which are generally smaller. More recent simulations by Moore et al. (1998) show the same trend for the dwarf galaxies to be disrupted in the center of the clusters. Such a destruction of the faint galaxies has also been proposed on observational bases for example by Secker et al. (1997) or Gregg & West (1998). These last authors, using deep photometry of the Coma cluster, propose the disruption of the faint galaxies as an explanation of the lack of dwarf galaxies in the core of this cluster (e.g. also Adami et al. 2000b).

A way to investigate this possibility is, for example, to search for cusped profile in the diffuse light. Gregg & West (1998) give an approximation of the total luminosity lost for the galaxies by disruption and turned into diffuse light in the center of the Coma cluster. This value is about 20% of the luminosity of a cD galaxy. This contribution is around 50% of the luminosity sum of all galaxies fainter than $-18.77$ in the central bin (where the cusp is significant for the bright galaxies) of our nearby com-posite cluster. After rescaling to the total luminosity to get units coherent with Fig. 2, we see on this figure that such a contribution is large enough to enhance the three faint luminosity profiles, consistently with a cusped model.

A more quantitative study has been done for this same cluster by Bernstein et al. (1995). Using very deep images of a cluster-central area of $7' \times 7'$, they conclude that the faint galaxy luminosity profile is flat or decreasing in the central 40 kpc (see also Adami et al. 2000b for a spectroscopic survey of this area), while the luminosity profile of the brighter galaxies is peaked. Moreover, considering now the diffuse luminosity profile (not associated with visible galaxies), they also found a peaked profile. If we argue that the cusp of the faint galaxy luminosity profile is erased by tidal disruption of part of these galaxies, we should recover at least partially this shape in the diffuse light profile. It is exactly what Bernstein et al. saw in the Coma cluster.

5.3. Destruction time scale?

We demonstrated that the cluster profiles have the same central shape from $z \sim 0$ to $z \sim 0.5$. This would imply that the time scale of the destruction processes described above (merging + disruption) would be relatively short. This is because all the faint galaxies accreted between $z \sim 0$ and $z \sim 0.5$ do not contribute to the reconstruction of a cusp. The in-falling galaxies seem to be continuously destroyed, in a time close to the virialization time which is approximately 1.5 Gyear (e.g. Sarazin 1986) for faint galaxies. This estimate is, for example, in good agreement with the estimates of the time needed to disrupt a low surface brightness galaxy in the simulations of Calcaneo-Roldan et al. (2000). An alternative explanation in agreement with the observations is that the accretion rate could be already very low at $z = 0.5$ (e.g. Ellingson et al. 2000).

6. Summary

We have shown that the galaxy luminosity density profile is cusped for the bright galaxies from $z \sim 0$ to $z \sim 0.5$ and exhibits a core for the faint galaxies. On another hand, the galaxy number density profile has a core (not significant for the bright galaxies). This could be understood if we assume a cusped profile for all the galaxies in agreement for example with the simulations of Navarro et al. (1997). The cusp could be erased for the galaxy number density profiles by merging effects and for the luminosity profile of the faint galaxies with the destruction of these galaxies by tidal forces. This seems to be confirmed by two observational studies of the Coma cluster (Gregg & West 1998; Bernstein et al. 1995).

If this model is confirmed, this would imply that clusters of galaxy mass profiles are well traced by the bright galaxy luminosity density profiles.

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