

Spectral resolution effects on the information content in solar spectra

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ABSTRACT

Context. When interpreting spectropolarimetric observations of the solar atmosphere, wavelength variations in the emergent intensity and polarization translate into information on the depth stratification of physical parameters such as the temperature, velocity, and magnetic field. Resolving the fine details in the shapes of the spectral lines and their polarization gives us the capability to resolve small-scale depth variations in these physical parameters. With the advent of large-aperture solar telescopes and the development of state-of-the-art instrumentation, the requirements on spectral resolution have become a prominent question.

Aims. We aim to quantify how the information content contained in a representative set of polarized spectra of photospheric spectral lines depends on the spectral resolution and spectral sampling of that spectrum.

Methods. We used a state-of-the-art numerical simulation of a sunspot and the neighboring quiet Sun photosphere to synthesize polarized spectra of magnetically sensitive neutral iron lines. We then applied various degrees of spectral degradation to the synthetic spectra and analyzed the impact on its dimensionality using principal component analysis and the wavelength power spectrum using wavelet decomposition. Finally, we applied the Stokes Inversion based on Response functions (SIR) code to the degraded synthetic data to assess the effect of spectral resolution on the inferred parameters.

Results. We find that the dimensionality of the Stokes spectra and the power contained in the small spectral scales significantly change with the spectral resolution. We find that regions with strong magnetic fields where convection is suppressed have more homogeneous atmospheres and produce less complex Stokes profiles. On the other hand, regions with strong gradients in the physical quantities give rise to more complex Stokes profiles that are more affected by spectral degradation. The degradation also makes the inversion problem more ill-defined, so inversion models with a larger number of free parameters overfit and give wrong estimates.

Conclusions. The impact of spectral degradation in the interpretation of solar spectropolarimetric observations depends on multiple factors, including the spectral resolution, noise level, line spread function (LSF) shape, complexity of the solar atmosphere, and degrees of freedom in our inversion methods. To mitigate this impact, incorporating a good estimation of the LSF into the inversion process is recommended. Having a finely sampled spectrum may be more beneficial than achieving a higher signal-to-noise ratio per wavelength bin. Considering the inclusion of different spectral lines that can counter these effects, and calibrating the effective degrees of freedom in modeling strategies, are also important considerations. These strategies are crucial for the accurate interpretation of such observations and have the potential to offer more cost-effective solutions.

Key words. line: formation – radiative transfer – methods: observational – Sun: magnetic fields – Sun: photosphere

1. Introduction

Physical processes taking place in the solar atmosphere exhibit a remarkable diversity of spatial, temporal, and energetic scales, necessitating measurements with a high spatial, spectral, and temporal resolution, and a sufficient signal-to-noise ratio (S/N) to comprehend their underlying nature (see, e.g., Iglesias & Feller 2019). Specifically, resolving the wavelength variations in the emergent intensity and its polarization gives us an insight into the depth variation in physical parameters such as the temperature, the velocity, and the magnetic field (Del Toro Iniesta & Ruiz Cobo 1996). This is because the absorption and emission processes in spectral lines show strong variations in wavelength, giving us access to a range of depths in the atmosphere of the Sun while observing a relatively narrow wavelength range.

Two classes of instruments are mainly used to spectrally resolve the light received at the telescope: filtergraph- and spectrograph-based systems. Filtergraphs, with the Fabry-Pérot interferometer being the most popular choice, are used for narrow-band imaging. They obtain pseudo-monochromatic images of the observed field of view (FoV). These instruments brought a revolution to high-resolution solar spectropolarimetry (e.g., Schärmer et al. 2008; Cavallini 2006), making it possible to observe and analyze very small (<100 km) spatial details in the solar atmosphere (e.g., Rouppe van der Voort et al. 2017; Díaz Baso et al. 2021) and study their spatial distribution in large FoVs (e.g., Kianfar et al. 2020; Morosin et al. 2022). Spectral fidelity (the degree of similarity between the original spectrum and the recorded one) of these instruments is limited and often comes at the cost of sacrificing the S/N and/or temporal resolution (e.g., Schlichenmaier et al. 2023; Díaz Baso et al. 2023), making resolving complicated spectral lines in detail borderline-unfeasible. On the other hand, slit-based spectrographs (from

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now on, spectrographs) trade one spatial dimension for the instantaneous wavelength information, traditionally through a spectrograph slit (e.g., Collados et al. 2012). This way, the entire spectrum is captured with high spectral detail, but to obtain a two-dimensional map of an extended source, the slit needs to be moved to scan the FoV. Spectrographs are also used as wavelength discriminators in integral field units like MiHi (van Noort et al. 2022; Rouppe van der Voort et al. 2023), which are capable of capturing the spatial and wavelength information simultaneously, albeit at a limited FoV.

The high spectral resolution and fine sampling result in an increased number of measurements and, consequently, an improved S/N. Furthermore, resolving fine spectral features allows us to probe complicated depth variations in physical parameters (Sanchez Almeida & Lites 1992). This has been important for studies like probing the magnetic fields in the quiet Sun (Martínez González & Bellot Rubio 2009), filaments and prominences (Díaz Baso et al. 2016, 2019a), sunspots (Borrero et al. 2007; Esteban Pozuelo et al. 2024), and magnetic flux-emerging regions (Yadav et al. 2019). Thus, spectrographs are common choices for instrument suites of ground- and space-based telescopes like DST/SPINOR (Socas-Navarro et al. 2006), ZIMPOL (Povel 2001), the GREGOR Infrared Spectrograph (GRIS; Collados et al. 2012) at the GREGOR telescope (Schmidt et al. 2012), the TRI-Port Polarimetric Echelle-Littrow spectrograph (TRIPPEL; Kiselman et al. 2011) at the Swedish 1-m Solar Telescope (SST; Scharmer et al. 2003), and the spectropolarimeter (SP) of the Hinode satellite (Kosugi et al. 2007), among others. They remain crucial instruments for providing high-fidelity spectral information at the next-generation 4-meter class of telescopes, such as the existing Daniel K. Inouye Solar Telescope (DKIST; Rimmele et al. 2020) with the Visible Spectro-Polarimeter (ViSP; de Wijn et al. 2022) and the planned European Solar Telescope (EST; Quintero Noda et al. 2022) with integral field units like MiHi (van Noort et al. 2022) or MuSiCa (Dominguez-Tagle et al. 2022).

Choosing the spectral resolution of a spectrograph system is a challenge: an increase in the spectral resolution necessitates using finer sampling, and thus decreasing the S/N per spectral bin, as well as the wavelength range of the observations. High spectral resolution increases the design complexity, which increases the cost of the equipment and compromises the robustness of the instrument. On the other hand, the loss of the spectral resolution poses a potential loss of information that can ultimately cause us to miss important physical content or to misdiagnose physical conditions.

This work investigates the impact of limited spectral resolution on the information content in spectropolarimetric measurements and inferred quantities. Our goal is to quantify how the information content contained in a representative set of polarized spectra of photospheric spectral lines depends on the spectral resolution and spectral sampling of the instrument used to acquire that spectrum. We achieved this by calculating synthetic spectra from a state-of-the-art MHD simulation of the solar atmosphere and degrading them according to different spectral resolutions. We then analyzed the information content in the original and degraded spectra and in the atmospheric stratification inferred from them using a spectropolarimetric inversion code. This strategy was earlier successfully executed by for example de la Cruz Rodríguez et al. (2012), Milić et al. (2019), Campbell et al. (2021), Quintero Noda et al. (2023). We believe these works are excellent references to understand the impact of the observation mode and analysis tools, optimizing obser-

vational strategies, identifying instrumental requirements, and refining our scientific interpretation. This work is organized as follows. We begin with a brief introduction and presentation of the synthetic observables we use in this work (Sect. 2). We then analyze the dimensionality of the data to quantify the complexity of the Stokes profiles (Sect. 3), followed by an analysis of the spectral scales present in the observables (Sect. 4), and finalizing with a study of the accuracy of the inferred atmospheric parameters from spectropolarimetric inversions under different levels of instrumental degradation (Sect. 5). Finally, we discuss these discrepancies and present our conclusions and recommendations for the instrument design (Sect. 6).

2. Data preparation

2.1. Synthetic data

The main reason for opting for high-spectral-resolution observations is to improve the ability to resolve the shapes of spectral lines, allowing for a detailed inference of the vertical stratification of physical quantities. Under limited spectral resolution, narrower spectral lines will be the most affected. In solar conditions, narrow spectral lines are typically the lines of heavier elements formed in the solar photosphere. Therefore, we chose to study the two magnetically sensitive spectral lines of neutral iron around 630 nm, which are also observed by the space-based slit SP (Lites et al. 2013) on board the Hinode (Tsuneta et al. 2008) spacecraft, and a common choice for ground-based observations; for example, ViSP at DKIST. To calculate the synthetic spectra, we used a radiative-magnetohydrodynamic (RMHD) simulation of a sunspot performed with the MURaM code (Vögler et al. 2005; Rempel 2017; Schmassmann et al. 2021). The sunspot also contains a quiet (weakly magnetized) solar atmosphere around, and thus provides a diverse set of observables that can be found in real observation. That is, we find strong and weak magnetic fields of various inclinations as well as regions with varying velocities and temperatures. The size of the simulation box considered for the analysis is $2048 \times 256 \times 256$ in (x, y, z) , with a grid size of $\Delta x = 20$, $\Delta y = 20$, and $\Delta z = 8$ km. This simulation is considered to be the state of the art in the generation of a numerical solar sunspot and surroundings (Tiwari et al. 2013) and it has been used to test different spectropolarimetric inversion approaches (Asensio Ramos & Díaz Baso 2019; Pastor Yabar et al. 2019).

We calculated the spectrum of the two FeI spectral lines at 630.15 and 630.25 nm using the “Stokes Inversion based on Response functions” code (SIR; Ruiz Cobo & del Toro Iniesta 1992). These spectral lines are sensitive to the temperature from the lower- to mid-photosphere. For canonical models of the solar atmosphere such as Fontenla et al. (1993), this corresponds to $\log \tau_{500} = 0 - \log \tau_{500} = -2$, where τ_{500} is the continuum optical depth at 500 nm. Regarding the spectral line sensitivity of these lines, the temperature is the most important parameter as it determines the ionization state of the gas, and the populations of the relevant atomic levels, and thus determines the emission and absorption properties of the plasma. They are also sensitive to the line-of-sight velocity because of Doppler shifts, and to the magnetic field through the Zeeman effect. The depth dependence of these physical parameters directly determines the complexity of the spectral line profiles. We carried out the synthesis assuming local thermodynamic equilibrium (LTE), for a very fine wavelength grid spanning from 630.1 to 630.3 nm, with a step of 5 mÅ. Although precise modeling requires a non-LTE approach (Smitha et al. 2021), differences are relatively small, and treating

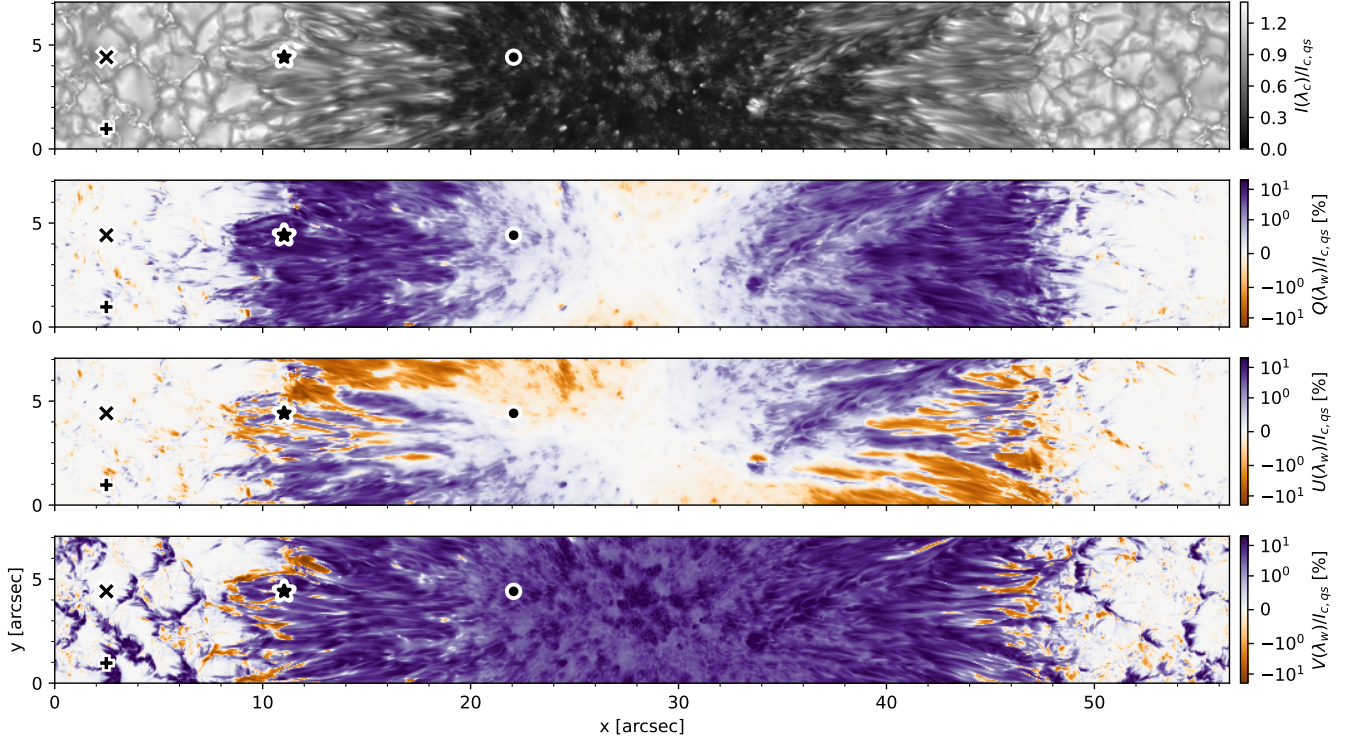


Fig. 1. Maps of synthetic intensity and polarization calculated from a snapshot of the MURaM simulation of a sunspot. The upper panel shows the continuum intensity, and the rest display the Stokes Q , U , and V signals at $\lambda_w = 6301.4 \text{ \AA}$, close to the core of the bluer spectral line. All the panels are normalized to the average quiet Sun continuum. The polarization signals are shown on a logarithmic scale for better visualization. Four symbols mark the location of the profiles shown in Fig. 2.

these spectral lines in LTE eases numerical experimentation significantly. Figure 1 shows the calculated continuum intensity and the polarization close to the core of one of the two lines.

2.2. Spectral degradation

The spectral resolution of a spectral discriminator (grating-based spectrograph or a Fabry-Perot filtergraph) is defined as the smallest wavelength separation $\delta\lambda$ that the instrument can distinguish. This is determined by the combination of the optical elements and the characteristics of the spectral discriminator. Spectral resolving power, a dimensionless quantity, is defined as $R = \lambda/\delta\lambda$. However, in the community, the number R is often referred to as the spectral resolution so we use the same designation here. We note that the spectral fidelity of the instrument is not uniquely identified by $\delta\lambda$ or R , but rather by the exact shape of the so-called line spread function (LSF, also known as the spectral point spread function). That is, the recorded spectrum, $I(\lambda)$, is related to the original (ideal) spectrum, $I_0(\lambda)$, as

$$I(\lambda) = I_0(\lambda) \star \text{LSF}(\lambda), \quad (1)$$

where $\text{LSF}(\lambda)$ is the LSF and $\star$ denotes the convolution in wavelength space. The LSF describes the response to a monochromatic light source: it explains how an infinitely thin spectral line (a delta function) would be at the focal plane. Furthermore, to take full advantage of the given spectral resolution, the sampling used to record the spectra should be optimal: following the Nyquist sampling criterion, two pixels were used per resolution element, $\delta\lambda$. The sampling we used to synthesize the data ($5 \text{ m\AA}$) is, at the given wavelength, optimal for a resolution of $R = 6 \times 10^5$, which is several times higher than the resolution regime we are planning to investigate. Thus, we consider the

spectra synthesized from the simulation to be at infinite spectral resolution compared to the spectra degraded by the LSF.

Depending on the properties of the instrument, the functional shape of the LSF will be different. For example, the LSF of a slit spectrograph is a sinc^2 profile (see, e.g., Casini & de Wijn 2014), which, together with other instrument imperfections, results in a final spectral profile that usually has an almost Gaussian shape (Borrero et al. 2016). We therefore consider our LSF to be Gaussian in the following analysis. It is very common to use the full-width at half maximum (FWHM) of the LSF as the smallest wavelength separation that the instrument can distinguish; that is, $\delta\lambda = \text{FWHM}$. For the following analysis, we generated the degraded spectra by spectrally convolving the original spectra by a Gaussian corresponding to a spectral resolution of $R = 10^5$. When performing spectropolarimetric inversions of these synthetic datasets, we considered spectral resolutions of $R = (5 \times 10^4, 1 \times 10^5, 2 \times 10^5, 3 \times 10^5)$ to estimate the impact of different degradations. Furthermore, as Sect. 5 shows, the spectral resolution of $R = 10^5$ allows a very reliable inference of atmospheric parameters, so we preferred to work on lower resolutions and sampling configurations. To visualize the effect of the spectral degradation, we show the Stokes profiles from four locations in the simulation (a granule, an intergranule, in the penumbra, and in the umbra) under different spectral resolutions in Fig. 2. As was expected, the spectral degradation smears out the fine details of the Stokes profiles, especially in the polarization signals. In the context of inversions, we also studied the effect that imperfect knowledge of the LSF has on the inferred atmospheric parameters. We focused on several specific scenarios because the full parameter space (number and spectral lines of interest, spectral resolution, noise level, LSF functional form, inversion configuration, etc.) prevents a concise and meaningful analysis.

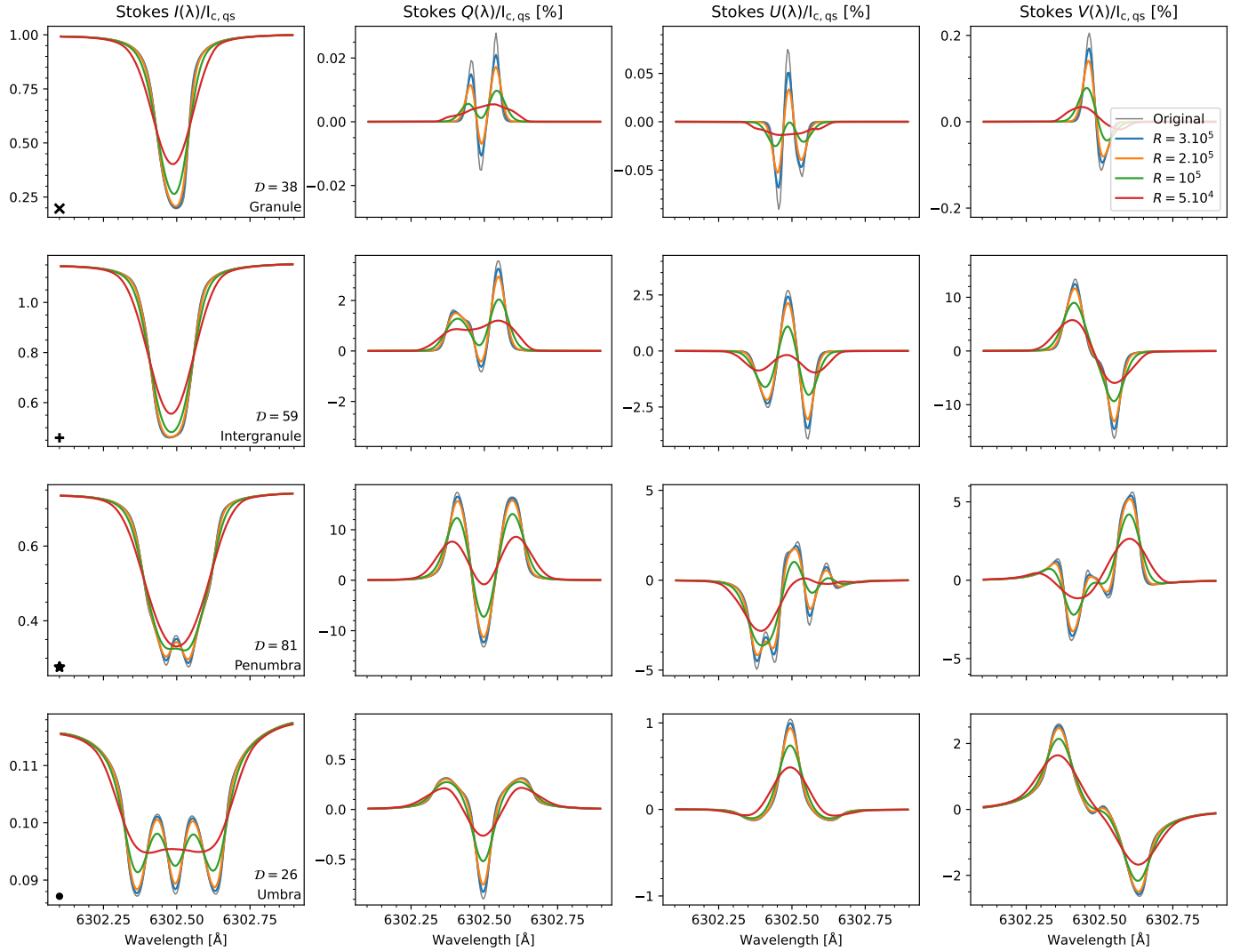


Fig. 2. Stokes spectra of example pixels from the simulation, under different spectral resolutions. Only one of the two Fe I lines is shown, for better visibility. The location of each pixel is indicated in Fig. 1 with the same symbols indicated in the lower left corner of each Stokes I panel, together with the total dimensionality of that spectrum, calculated for the non-degraded case.

3. Dimensionality analysis

3.1. Dimensionality estimation

To understand and quantify how spectral degradation affects the Stokes profiles of these specific photospheric spectral lines, we first analyzed their complexity and put it in the context of the physical structure of the underlying solar atmosphere. More complex profiles are expected to be harder to model with spectropolarimetric inversion techniques but potentially hold more information. Very complicated or unusual profiles will point to interesting atmospheric structures with potential for scientific discovery.

Motivated by the work of Asensio Ramos et al. (2007), we quantified the complexity of the Stokes profiles by calculating their dimensionality using principal component analysis (PCA, e.g., Press et al. 2007), which allows us to decompose a Stokes profile into a series of orthogonal components ordered according to the amount of variance they explain. In general, the number of complex profiles is a small fraction of the total number of profiles, so the ordering of the PCA components according to the variance is compatible with an ordering according to their complexity. Thus, we used the number of components

required to reproduce a profile as a measure of its dimensionality (Martínez González et al. 2008). To compute the dimensionality, $\mathcal{D}$, of each Stokes spectrum, we first created the set of basis vectors, separately for intensity, linear, and circular polarization, using the entire FoV. For simplicity, from now on the linear polarization (defined as $L = \sqrt{Q^2 + U^2}$) will be analyzed instead of the Stokes Q and U separately. We defined the dimensionality of each spectrum as the number of components needed to reproduce the profile S with a standard deviation lower than a given threshold, σ (Borrero et al. 2016). That is,

$$\mathcal{D}(S) = \min_N \left\{ N \mid \sqrt{\left(\sum_{i=0}^N c_i \mathcal{V}_i - S \right)^2 / N_w} < \sigma \right\}, \quad (2)$$

where i enumerates the order of the basis vectors, c_i are the coefficients in the PCA decomposition, $\mathcal{V}_i$ the eigenvectors of the basis, and N_w the number of wavelength points in the Stokes parameter, S . Figure 3 shows the average dimensionality of each Stokes parameter on different thresholds for the 524 288 (256×2048) Stokes profiles of the MURaM snapshot. In this figure, the dimensionality of the Stokes parameters rises very

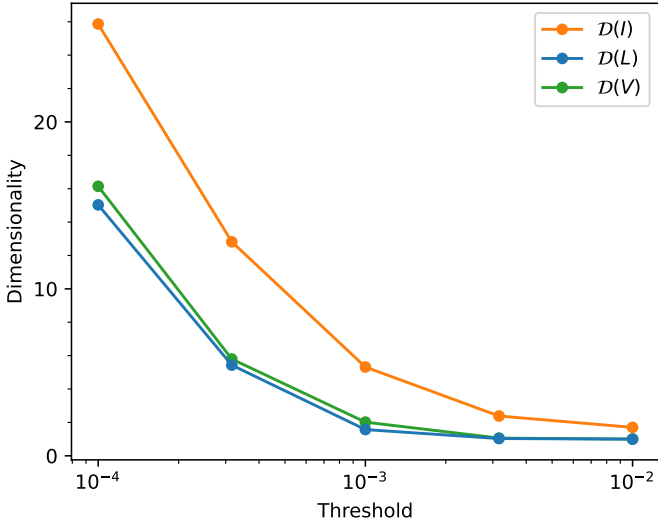


Fig. 3. Spectra dimensionality calculated by PCA based on different thresholds for the reconstruction of the 5×10^5 Stokes profiles from the MURaM snapshot. This is estimated on the spectra containing the two Fe I spectral lines at full spectral resolution. The filled circles are the average dimensionality of each distribution.

rapidly as the threshold decreases (note the logarithmic scale in the horizontal axis). For a threshold between 10^{-2} and 10^{-3} , the spectra can be explained mainly with 2–5 components. The very small-scale features are only identified when the threshold is lowered to 10^{-4} , which suggests that the Stokes parameters are usually simple to explain and the substructure of the profiles has a smaller amplitude. Our choice of threshold is driven by typical photon noise found in spatially resolved solar spectropolarimetric observations. In the following, the dimensionality has been calculated using $\sigma = 10^{-4}$ for all the Stokes parameters. We have verified that the overall results were not significantly affected by the specific choice.

Our threshold is defined in an absolute way. So, Stokes profiles with very weak polarization signals, or weak spectral features, will be classified as low-dimensional even though they might appear to be very complicated. This is because the criterion from the Eq. (2) is satisfied already for a small N , because a few first basis vectors are enough to reproduce the profile closely to the threshold. Said differently, our approach classifies profiles according to the dimensionality that we can detect with our limited S/N. An alternative approach would be to use Eq. (4) with the threshold defined in a relative way (for example, fraction of the maximum polarization signal), and thus characterize the complexity of the low-amplitude signals. This approach would, on the other hand, identify complex profiles that cannot be detected in actual observations due to the photon noise.

3.2. Spatial distribution of dimensionality

Figure 4 shows the spatial distribution of the dimensionality of the Stokes profiles over the FoV. The top panel shows the dimensionality of Stokes I . The distribution is very homogeneous, having an average value of 30 in the weakly or intermediate magnetized regions and decreasing to 15 in the umbra. Only very few locations (1.2% of the FoV) need more than 50 components, where this value can go up to 110. The second row shows the spatial distribution for the linear polarization signals and their dimensionality resembles very closely their amplitude (see the second and third panels of Fig. 1). A high number of PCA

components is needed to reproduce the signals in the penumbra because of its strong and complicated magnetic fields and the presence of velocity field gradients. Outside the penumbra, the signals might appear to be complex but their amplitudes are well below the specified threshold. Again, this is a consequence of our definition of dimensionality.

The dimensionality of Stokes V (third panel) presents high values in the intergranular lanes and the core of the penumbral filaments. On the contrary, the profiles that emerge from the umbra have a very low dimensionality. This can be understood as a consequence of the homogeneous properties of the solar atmosphere in those particular regions; that is, the temperature, the velocity, and the magnetic field also show a decrease in dimensionality (see Fig. A.2). Some umbral dots appear to have an increased dimensionality (in particular in Stokes V), which is not clearly visible in the dimensionality of the physical quantities. This behavior can be interpreted as an indication of the nonlinear radiative transfer process that generates the observed Stokes profiles.

Lastly, to compare the results of the degradation in pixels with different complexity, we calculated a binary mask (shown at the bottom panel of the same figure) of the spectra whose total dimensionality (sum of individual dimensionalities, i.e., $D(I) + D(L) + D(V)$) is larger than a specific threshold. This will be used later to distinguish “simple” profiles from “complex” ones. A value of 80 is a good compromise to capture an important percentage (~20%) of the profiles that present small-scale features in the region. To understand the relation between the estimated dimensionality and the typical shapes of the Stokes profiles, Fig. 2 also displays the total dimensionality in the bottom right corner of each of the extracted pixels.

3.3. Influence of limited spectral resolution on the dimensionality

To quantify the impact of the spectral degradation on the dimensionality of the Stokes profiles, we degraded the original synthetic profiles to a spectral resolution of $R = 10^5$ and calculated the dimensionality with the same procedure (i.e., using Eq. (2)). Figure 5 shows the ratio between the dimensionality before (formulated as $\mathcal{D}_\infty$) and after the degradation, using the same threshold, σ , for the total dimensionality (upper panel) and for each individual Stokes parameter (bottom row).

As was expected, the degradation decreases the dimensionality of the data; that is, the ratio is always lower than 1 across the region. The spatial distribution of the upper panel shows that the umbra is less affected by the degradation. Regarding individual Stokes contributions, there is a trend where the dimensionality tends to decrease by half for pixels with high dimensionality. This is more visible in Stokes I and V than in the linear polarization. We would expect that pixels with lower dimensionality should not change much because the degradation should mainly affect profiles where many components are needed to reproduce small-scale features. However, the 2D histograms of each Stokes parameter show an average value lower than unity also at low $\mathcal{D}$ values. The fact that we calculate the dimensionality using different PCA bases derived from each dataset could explain why the new degraded data requires fewer eigenvectors to efficiently represent the observations.

In summary, the PCA decomposition can be used to evaluate the complexity of the profiles. The largest change in dimensionality is found in the profiles with the highest original dimensionality; that is, the spectra emerging from the penumbra and intergranular lanes.

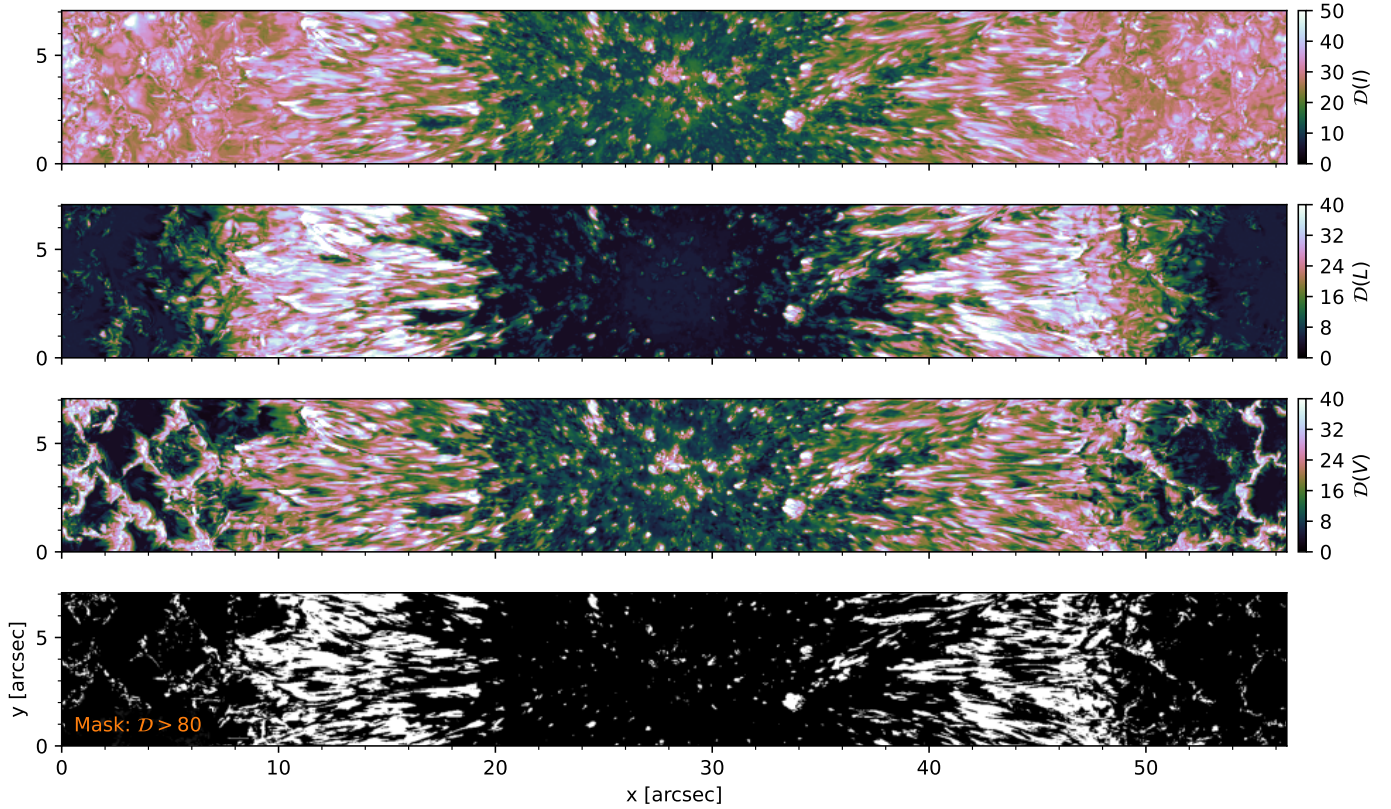


Fig. 4. Spatial distribution of the dimensionality of Stokes I (top panel), linear polarization (second panel), and Stokes V (third panel), defined as the number of PCA components needed to reproduce such signals under a threshold of $\sigma = 10^{-4}$. The bottom panel shows a binary mask, where white pixels mark the spectra whose total dimensionality, $\mathcal{D}(I) + \mathcal{D}(L) + \mathcal{D}(V)$, is larger than 80.

4. Wavelet analysis

4.1. Wavelet decomposition

It is expected that a limited spectral resolution will suppress the small-scale spectral features. To quantify this effect, we analyzed the power contained in different spectral scales in the Stokes profiles. We chose the wavelet decomposition technique instead of Fourier decomposition because the signals (the Stokes profiles) are confined in the original domain (wavelength range). Fourier decomposition is made in sinusoidal signals defined across the whole domain, while in wavelet analysis the base signal (i.e., “the mother wavelet”) has a confined functional form and can be shifted and scaled to cover the domain. Given the similarity with the Stokes profiles, the DOG (derivative of Gaussian) wavelet was chosen as the mother wavelet. We defined the “spectral scale” of our profiles as half of the wavelet period. The decomposition was performed using the `pycwt`¹ Python package. The wavelet coefficients were then used to compute the wavelet power spectrum, defined as the square of the absolute value of the wavelet coefficients. We note that, depending on the mother wavelet, the power spectrum can be slightly different, so we should treat these results as a representative behavior and not as a precise description of the scales in the spectra.

4.2. Degradation of spectral scales

In the following analysis, we focus on Stokes V signals, but the results for other Stokes components are similar. The first panel of Fig. 6 shows the power, $\mathcal{P}$, contained in the wavelet decom-

position at scales of 45 mÅ for the Stokes V signals. We chose this scale as it is slightly below the FWHM that corresponds to the 10^5 resolution at 630 nm, and we thus expect it to be substantially influenced by the finite spectral resolution. However, the power at any other scale presents a very similar distribution because the power scales with the square of the signal amplitude, and the pixels with the strongest signals have the most power. This is, in a way, similar to the results of the previous section in which we found that the pixels with larger polarization amplitudes show higher dimensionality.

To focus on the spectral shape and not on the amplitude of the signals, we normalized each pixel to its maximum amplitude before computing the wavelet decomposition. This way, we can analyze the spectral scales present in the profiles. The power contained in the normalized spectra, $\mathcal{P}_N$, at two different wavelength scales is shown in the second and third panels of the same figure. The smallest scales (second panel) are predominantly found within the granules, whereas the larger scales (third panel) have relatively more power in the intergranules, penumbra, and umbra. This is expected because the magnetic field broadens the Stokes V profiles. From this analysis, we can conclude that although there are many pixels with small spectral scales, they will be impossible to detect under a specific S/N, confirming the results from the PCA analysis.

When the spectra are degraded to $R = 10^5$, the smallest scales (similar to or shorter than the width of the LSF) are the most affected by the degradation and larger scales are mostly unaffected. To show this, we calculated the ratio, $\mathcal{R}$, of the power before and after the degradation (without normalizing the data). This is shown in the fourth panel of Fig. 6 only for the small scales (45 mÅ). The ratio is always lower than 1, with very low

¹ <https://github.com/regeir/pycwt>

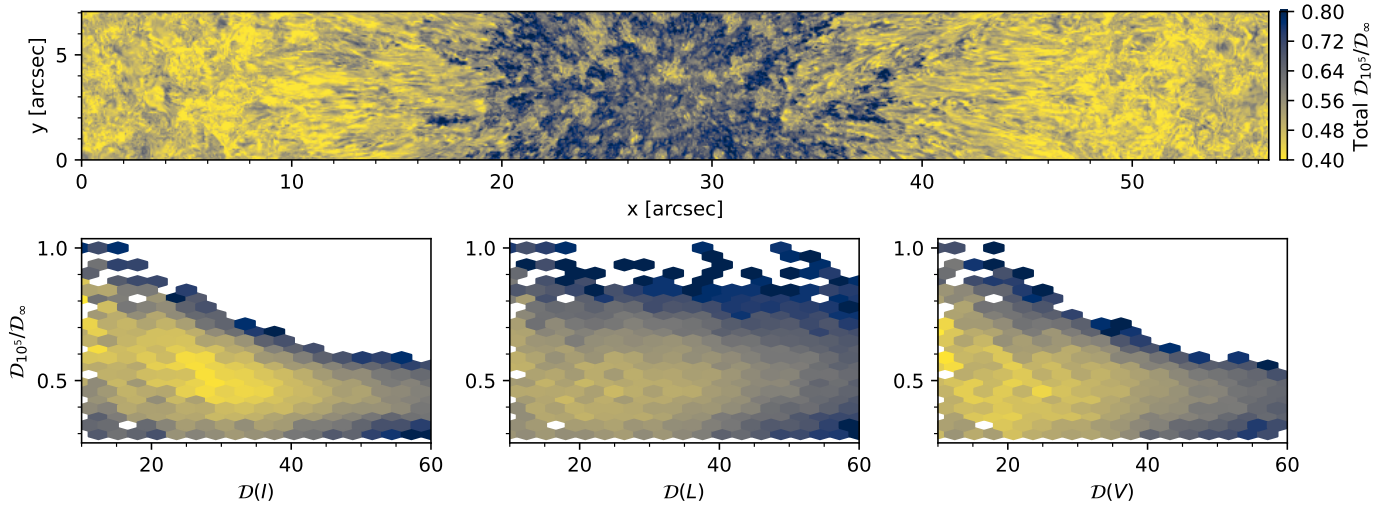


Fig. 5. Difference in the dimensionality of the original and degraded spectra emerging from the simulation. Upper panel: Ratio of the dimensionality calculated from the original spectra emerged from the simulation and after degrading it to a spectral resolution of $R = 10^5$ (smaller values are regions where the degraded spectra are more affected). Bottom row: 2D histograms of the ratio of the dimensionality for each Stokes parameter.

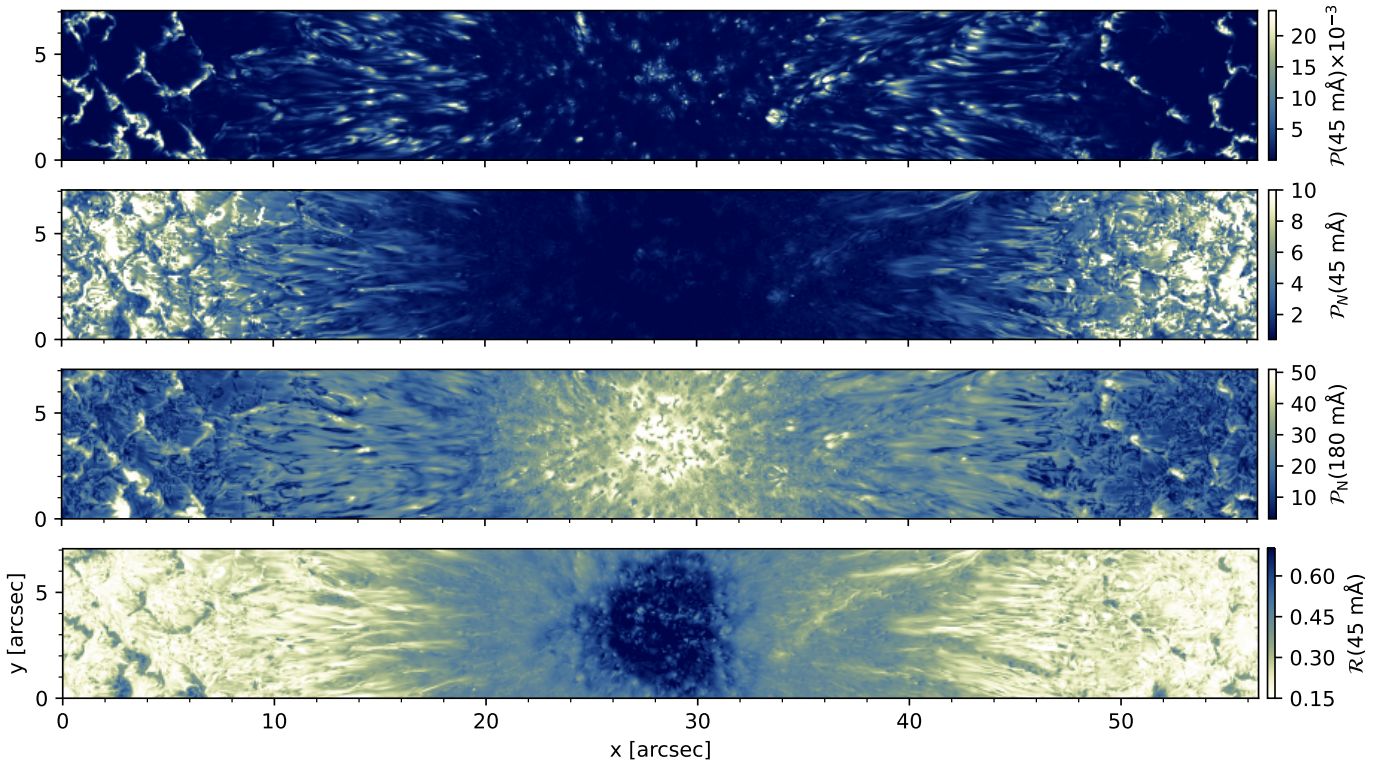


Fig. 6. Summary of the wavelet analysis of the Stokes V profiles. The first panel shows the power contained in the wavelet decomposition at scales of 45 mÅ. The second and third panels show the power contained in the normalized spectra at scales of 45 and 180 mÅ, respectively. The fourth panel shows the ratio of the power before and after the degradation at a scale of 45 mÅ.

values not only within the granules but also in many locations inside the penumbra. A good example of how the spectral degradation smears out these smallest scales in those regions is shown in Fig. 2.

5. Spectropolarimetric inversions

Probably the most relevant test of information loss is to perform an end-to-end study of the inference process (see e.g., de la Cruz Rodríguez et al. 2012; Milić et al. 2019). We used the synthetic data as our observables and the inferred physi-

cal parameters were compared to the original stratification – in other words, to the “true” solution – and thus investigated how spectral degradation affects the inference process. To ensure the absence of biases related to model atoms, opacity packages, and specific numerical schemes, we once again employed the SIR code for the inversion. This approach is preferred as it helps avoid discrepancies that frequently arise when using different inversion codes. We implemented our own MPI parallelized version to speed up the inversions (see Appendix B for more information). In the following, we present the results of the inversions considering different levels of spectral resolutions,

Table 1. Hyperparameters used in the inversions: nodes configuration for the physical parameters depending on the scheme.

Parameters	Config 1	Config 2	Config 3
T	2, 3, 4	3, 5, 7	4, 7, 10
v_{LOS}	1, 2, 3	2, 4, 7	3, 4, 10
B	1, 2, 3	1, 2, 4	3, 4, 10
Θ_B	1, 1, 2	1, 2, 4	2, 3, 10
Φ_B	1, 1, 2	1, 2, 4	2, 3, 4

binning, and photon noise. We are motivated by the instrument requirements for the 4-m class of telescopes (Rimmele et al. 2020; Quintero Noda et al. 2022), so we did not perform any spatial degradation.

5.1. Inversion complexity

Inversion is an optimization process that tries to find the model atmosphere (i.e., set of depth-dependent physical parameters) that best reproduces the observed Stokes profiles. In SIR and other stratified inversion codes such as SNAPI (Milić & van Noort 2018), STiC (de la Cruz Rodríguez et al. 2016), or FIRTEZ (Pastor Yabar et al. 2019), the model atmosphere is parametrized at some locations in the optical depth scale (called nodes) and the remaining part of the atmosphere is obtained by interpolating a perturbation at the nodes (SIR, FIRTEZ) or by interpolating values at the nodes themselves (SNAPI, STiC). The nodes are the free parameters of our model and the number of nodes represents a measure of the complexity of the model. Inversion is generally an ill-posed problem, which means that many combinations of parameters yield equally good fits to the observations (i.e., the parameters are degenerate). This degeneracy increases with the complexity of our model. Using many nodes can result in overfitting, whereby the inferred atmosphere presents oscillatory or unrealistic solutions. On the other hand, using too few nodes can lead to underfitting, whereby the model cannot reproduce the observed profiles.

To understand the interaction between the complexity of the spectra and the complexity of the model, we used three configurations with varying numbers of nodes: a minimal configuration with a small number of nodes that provides a good estimation (configuration 1), a robust configuration that captures most of the features (configuration 2), and a sophisticated configuration that provides a very good fit to the data (configuration 3). The parameters that are allowed to change are the temperature (T), the line-of-sight velocity (v_{LOS}), the magnetic field strength (B), the inclination of the magnetic field with respect to the line of sight (Θ_B), and the azimuth of the magnetic field in the plane perpendicular to the line of sight (Φ_B). All the configurations have three cycles; that is, we ran the inversion three times, successively increasing the number of nodes until reaching the final number of nodes per physical parameter (see Table 1 for details). Additionally, to achieve as good inversion as possible, the results of the robust configuration were used as an input for the complex configuration.

5.2. Instrumental effects

To quantify the impact of the spectral resolution on the inferred physical parameters, we created and inverted datasets where different instrumental effects were applied: (i) the original spectra from the simulation, (ii) the spectrally degraded spectra, (iii) the

spectrally degraded spectra with noise, and (iv) the spectrally degraded spectra with noise, spectrally resampled according to the Nyquist-Shannon theorem for the corresponding spectral resolution. At the original sampling of 5 mÅ, we estimated the number of photons per bin in the following way (similar to Riethmüller & Solanki 2019):

$$N = \frac{2c^3}{\lambda^4(\exp(hc/\lambda kT) - 1)} \times \frac{D^2\pi}{4d^2} \times \Delta x^2 \times \Delta t \times \Delta \lambda \times \eta, \quad (3)$$

where the first factor on the right-hand side is the number of photons emitted per unit surface in unit solid angle per unit time per unit wavelength, the second is the solid angle spanned by the telescope, the third is the surface on the Sun corresponding to one pixel, the fourth is the exposure time, the fifth is the size of wavelength bin, and the sixth is the efficiency of the telescope-spectrograph system. We took $T = 5700$ K, $\lambda = 630$ nm, $D = 4$ m, $\Delta x = 14$ km (half of the diffraction limit for corresponding D calculated as $1.22\lambda/D$), $\Delta t = 1$ s, $d = 1.5 \cdot 10^{11}$ m (distance Earth–Sun), and $\Delta \lambda = 5$ mÅ. For efficiency, we took a very conservative $\eta = 0.03$, which is on the lower end for ground-based observatories (in Hinode/SOT/SP is estimated to have an efficiency of 0.25). This brings us to a S/N of around 350 in the Stokes I continuum, and, assuming the optimal demodulation ($1/\sqrt{3}$), approximately a S/N of 200 in other Stokes components. Following this estimate, we applied a noise of 5×10^{-3} in units of the continuum intensity to all four Stokes components, scaling the noise with the square root of the Stokes I continuum in each pixel.

For the resampled data, the Nyquist-Shannon theorem states that the sampling should be at least 2 pixels per resolution element. Under this spectral resolution, the spectral lines have been sampled to a pixel size of 30 mÅ. In that case, the noise level per spectral bin is decreased by more than a factor of 2, to 2×10^{-3} in units of the continuum intensity. To contextualize these values, the spectral resolution of the Hinode/SP instrument is around $R = 2 \times 10^5$ with 21.5 mÅ sampling (Lites et al. 2001). Our noise levels are higher than a typical Hinode/SP observation due to shorter exposure and a low estimate of η . Better noise levels can be achieved with longer exposure times, but we have preferred to be conservative in this step. Other reference values of spectral resolution at this wavelength are added for comparison: about 105 000 for VTF/DKIST (Bell et al. 2014), 180 000 ViSP/DKIST (de Wijn et al. 2022), 170 000 SPINOR/DST (Socas-Navarro et al. 2006), about 115 000 for CRISP/SST (Scharmer et al. 2008), and about 200 000 for TRIPPEL/SST (Kiselman et al. 2011).

All four sets of data – (i) original, (ii) convolved, (iii) convolved and noised, and (iv) convolved, noised, and resampled – were inverted using each of the three configurations described in Sect. 5.1.

5.3. Inversion results

Before analyzing the inferred physical quantities, we studied the performance of each node configuration when reproducing the Stokes profiles. A measure of the quality of the fit,

$$\chi^2 = \frac{1}{4N_w} \sum_w \sum_i^4 \frac{(S_{i,w}^{\text{inv}} - S_{i,w}^{\text{obs}})^2}{\sigma_i^2}, \quad (4)$$

was calculated for each pixel, where N_w is the number of wavelength points, S_i^{inv} and S_i^{obs} are the inverted and observed Stokes profiles, respectively, and σ_i is the noise level. We consider that

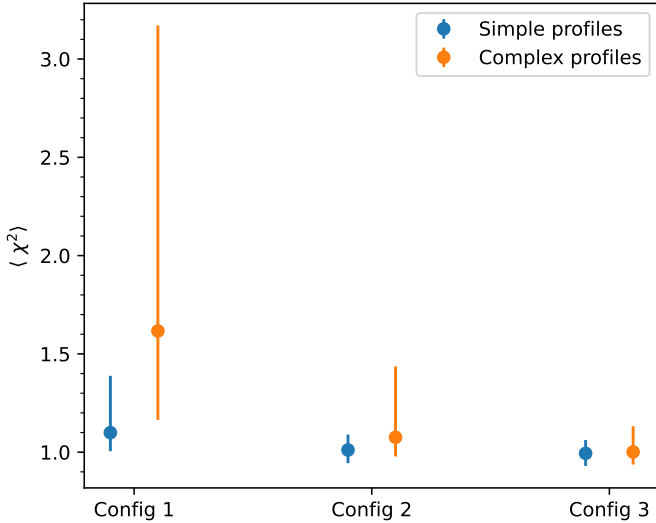


Fig. 7. Quality of the inversions for the different node configurations of increasing complexity (see Table 1). The filled circles are the average χ^2 (Eq. (4)) calculated for profiles whose total dimensionality is smaller (simple) or larger (complex) than 80 (see binary mask in Fig. 4). The error bars show the 16th and 84th percentiles of each distribution.

the inversion is able to reproduce the observed profiles when $\chi^2 \approx 1$. The average quality of each configuration $\langle \chi^2 \rangle$ is shown in Fig. 7 for the noisy degraded case. In this figure, we have also separated the simple and complex profiles according to the mask defined in Fig. 4. This figure shows that the simple profiles are reproduced well by all configurations. On the other hand, the complex profiles are better reproduced when increasing the complexity of the configuration. This makes clear that worse retrievals using the sophisticated configuration are not due to a problem when reproducing the profiles but due to the overcomplicated solutions.

The results of the inversions of the four datasets are displayed in Fig. 8. This figure depicts the standard deviation between the inferred and the true values for the temperature, magnetic field strength, and line-of-sight velocity across the FoV in the range of heights with larger sensitivity (between $\log \tau_{500} = -0.5$ and $\log \tau_{500} = -1.5$). This quantity can be understood as an average error or discrepancy between the inferred and true values. Reducing the range of optical depths to a single point in height (at $\log \tau_{500} = -1$) has almost no impact on the spatially averaged errors. The results are presented for the different configurations and the different scenarios.

For the original scenario where no degradation has been applied, the complex configuration (indicated by the green solid line) achieves superior accuracy, exhibiting average errors of approximately 38 K for temperature, 45 G for magnetic field strength, and 0.14 km/s for line-of-sight velocity. However, as soon as we degrade the data, the error of each configuration increases. This effect is particularly significant in the most complex configuration. This is because the complex configuration is more prone to overfitting, and the data degradation makes the inversion process more ill-posed (i.e., more solutions can reproduce the observed Stokes profiles). The presence of noise significantly influences the accuracy of inversion results. The complex configuration becomes as bad as the simple configuration, while the robust configuration provides the best results.

Lastly, when the spectra are resampled, the robust configuration also provides worse results than the simple configuration (most of the time). While the noise level per spectral bin is lower

than in the degraded+noise case, spectral sampling makes the recovery of the physical parameters more difficult. In fact, the typical error at this point is on the order of twice the error of the ideal case. In summary, the best-performing configuration depends on the amount of information present in the data. This also shows that for this particular case the amount of information we lose when resampling the data is larger than what we gain in S/N. It is important to note, however, that sparser wavelength sampling allows for observations with a wider wavelength range, which could increase the stratified information by combining more spectral lines (Riethmüller & Solanki 2019).

We repeated the same analysis to quantify how different inversion configurations perform on spectra of different complexity. For that, we used a mask defined in Sect. 3, and the results when being split into these two groups are shown in Fig. 9. One might think that complex profiles could produce distinctive imprints from atmospheric conditions that would make the inverse process better constrained, but in fact complex profiles tend to have larger errors. This could be due to forward modeling and loss of information as part of radiative transfer, or in the inversion process due to, for example, further degeneracy in modeling, or the validity of the hydrostatic equilibrium hypothesis. Another result is that the distance between these two groups is smaller for the magnetic field strength than for the temperature and line-of-sight velocity. This result can be understood if the magnetic field strength in simple and complex profiles is not as different, but the temperature and line-of-sight velocity make the profiles look much more complex.

To further investigate the impact of the complexity of the depth stratification of the physical quantities on the inversion results, we calculated the dimensionality of the physical quantities of our simulation (see Appendix A). Later, we calculated the average dimensionality of the physical quantities for the simple and complex profiles. These results are shown in Fig. 10. As was expected, the complex profiles come from regions with a higher dimensionality in the physical quantities. In particular, if we look at the difference between the simple and complex profiles (solid gray line), we can see that the line-of-sight velocity is the physical quantity that shows the largest difference between the simple and complex profiles. In conclusion, the complexity of the Stokes profiles is mostly controlled by the gradients in the line-of-sight velocity (according to our simulation).

5.4. Additional tests

Our tests show visible effects of spectral resolution, binning, and noise on the inferred parameters. Still, the agreement between the original atmosphere and inferred parameters with varying degrees of instrumental effects is excellent: below 100 K in temperature, up to 100 G in the magnetic field, and up to 0.3 km/s in LOS velocity. In reality, these disagreements are likely to be shadowed by various systematics: imperfect knowledge of atomic parameters, the inadequacy of the assumption of LTE, or an insufficiently detailed knowledge of instrumental effects. It is not straightforward to perform an end-to-end study taking into account the effects one does not know about. Nevertheless, to take our inversion scheme to the brink of applicability we performed four more inversion tests: (i) using only one spectral line from the line pair (630.25 nm), (ii) using a low-spectral resolution case with $R = 5 \times 10^4$, (iii) treating spectral resolution as unknown and fitting the width of the LSF as a free parameter (through the macroturbulent velocity parameter), and (iv) degrading the spectra with a different LSF (sinc^2 function), but using a Gaussian LSF during the inversion. These tests aim

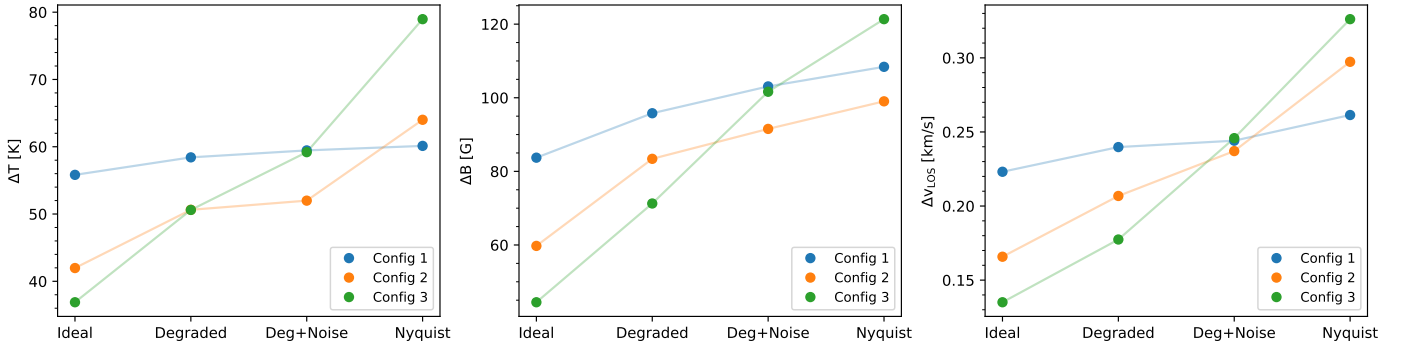


Fig. 8. Average error between the inferred and the original values from the simulation in the range $\log \tau_{500} = [-0.5, -1.5]$ for different scenarios and different inversion configurations. The error is measured as the standard deviation. The left panel shows the error in temperature, the middle magnetic field strength, and the right panel velocity. In each panel from left to right: inversions using the original spectra, degraded spectra, degraded spectra with noise, and degraded spectra with noise sampled according to the Nyquist-Shannon theorem at the corresponding spectral resolution.

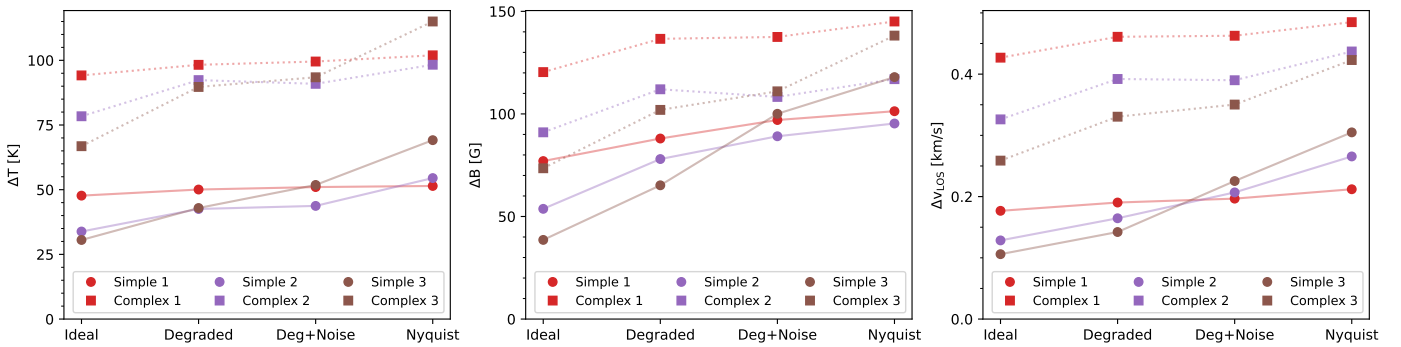


Fig. 9. Same as Fig. 8 but for the simple (solid lines) and complex (dotted lines) Stokes profiles.

to mimic a situation in which our information space is limited and/or we do not know our instrumental effects well enough.

The results of these runs are shown in Fig. 11. Starting with the case with the lower impact, if the sinc² LSF is approximated by a Gaussian the errors increase by about 20% in the temperature, 12% in the magnetic field strength, and 20% in the line-of-sight velocity. They might seem large percentages but in absolute units they represent still-low errors, indicating that the inversion process is not very affected by the choice of LSF. Using only one spectral line, the error increases in the magnetic field up to 15%, while the temperature and line-of-sight velocity are about 20% worse. This shows how the combination of the two spectral lines indeed provides additional constraints on the physical quantities. Treating the macroturbulent velocity as a free parameter increases the errors substantially. The errors increase by approximately 70% in the temperature, 30% in the magnetic field, and 30% in the velocity. Although the macroturbulent velocity as a free parameter could better reproduce the observed profiles, the inversion process is more ill-posed because of the degeneracy between the macroturbulent velocity and the physical quantities. One would expect to increase the errors in the temperature and magnetic field strength because all three control the broadening of the spectral lines. However, changing the temperature stratification will shift the formation region of the spectral line to different heights in the atmosphere. This shift alters the specific velocities required at those heights to accurately reproduce the observed spectral line profiles. Finally, the case with the highest impact is the low spectral resolution. The errors in the magnetic field strength increase by 130%, while those in the line-of-sight velocity increase by up to 60%. The error in the temperature is the least affected, with an increase of 12%. This is expected

because the degradation is especially effective in removing the small scales in the polarization profiles because of their oscillatory nature around zero, while Stokes *I* is barely affected (see Fig. 2).

We can conclude that the inversion process is very sensitive to the following effects (in decreasing order of importance): low spectral resolution, complete ignorance of the LSF, using only one spectral line, and approximating the LSF with a Gaussian. Although the error introduced by using only one spectral line and by approximating the LSF with a Gaussian are similar, it is advisable to use multiple spectral lines and the proper shape of the LSF to minimize errors effectively.

5.5. Effect of spectral resolution on inversions

Finally, to isolate the effect of spectral resolution and its impact on the inferred atmospheres, we repeated the same analysis for four different spectral resolutions: $R = 5 \times 10^4$ to $R = 3 \times 10^5$. The data was degraded using the most realistic scenario; that is, spectrally convolved, noised, and resampled according to the Nyquist-Shannon theorem, and then inverted using the robust configuration (configuration 2). This specific choice of instrumental degradation is intended to make the comparison more realistic and provide information that is better applicable to the design of real-life instruments. The results are shown in Fig. 12. All the errors decrease drastically when the spectral resolution goes from $R = 5 \times 10^4$ to $R = 10^5$, despite the increase in noise per wavelength bin. Moreover, a quick comparison of the results at $R = 5 \times 10^4$ between Figs. 11 and 12 shows that the impact of the sampling according to the Nyquist-Shannon theorem is more significant the lower the spectral resolution is. After that,

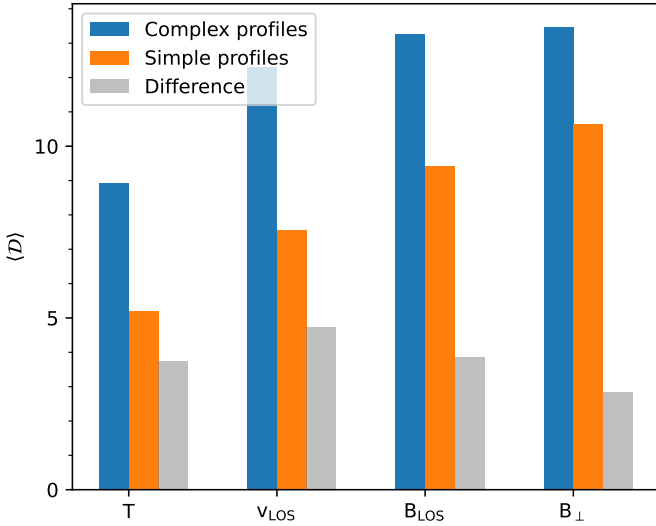


Fig. 10. Average dimensionality of the physical quantities in the simulation calculated from stratifications belonging to simple and complex profiles. The gray bars show the difference between the two.

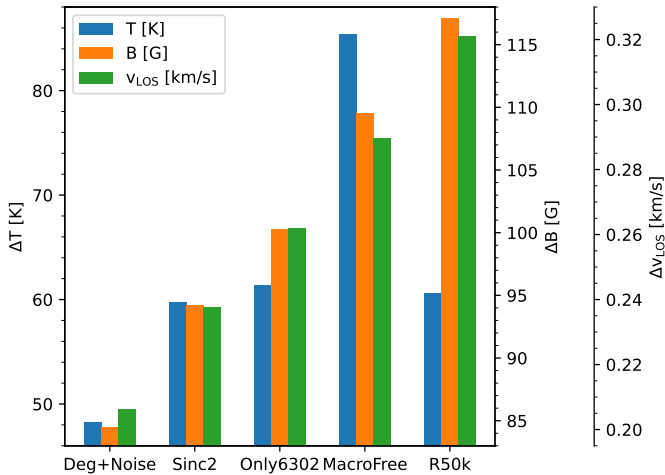


Fig. 11. Average error in the temperature, magnetic field strength, and line-of-sight velocity for the case in which a sinc^2 LSF is modeled with a Gaussian, when only one spectral line is used (630.15 nm), when the macroturbulent velocity parameter is let to vary in every pixel, or when there is a much lower spectral resolution ($R = 5 \times 10^4$) compared to the noisy degraded case ($R = 10^5$).

the improvement is less significant and the curve seems to saturate. We note that even ideal inversion with an infinite spectral resolution exhibits errors when compared to the simulation, due to the inability of the SIR code to exactly reproduce complicated atmospheric depth stratification found in the simulation. A more detailed comparison is given in Fig. 13, where we show the spatial distribution of the inferred parameters and the spatial distribution of the differences between the different inversions and the original simulation. The increase in accuracy between $R = 5 \times 10^4$ and $R = 10^5$ is again evident. The difference between the inferred and original physical parameters depends on the inverted feature: the umbra is typically well reproduced, while the penumbra and quiet Sun inversions exhibit systematic differences. We interpret these systematic differences as a feature of the inversion code, and it is highly possible that different inversion codes or even configurations would result in different systematics.

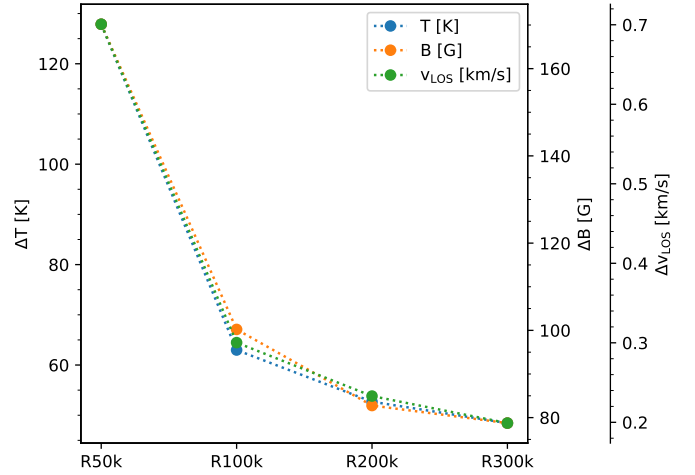


Fig. 12. Average error in the temperature, magnetic field strength, and line-of-sight velocity for the most realistic case (degraded, noisy, and resampled) using configuration 2 for different spectral resolutions.

From this test, we can conclude that the accuracy improvements brought by spectral resolutions above 10^5 are minimal. Consequently, expanding the wavelength range to include additional diagnostics may prove to be a more advantageous strategy. The latter approach has the potential to offer better insights into the stratification of physical quantities and could be more cost-effective.

6. Summary and conclusions

In this study, we have analyzed the impact of spectral degradation on the information content in polarized solar spectra and on our ability to recover that information. We achieved this by calculating photospheric spectra from a state-of-the-art RMHD simulation of a sunspot and then degrading the Stokes profiles to different spectral resolutions. We then analyzed the effect of spectral resolution by quantifying the complexity of the Stokes profiles using wavelet decomposition, and the accuracy of the inferred physical parameters using spectropolarimetric inversions. We analyzed a set of specific scenarios because the full parameter space (number and spectral lines of interest, spectral resolution, spectral binning, noise level, LSF functional form, node configuration, etc.) is too large to be investigated at once.

From the study of the dimensionality and spectral scales, we conclude that most of the complex profiles are found in the penumbra and intergranular lanes, which are the regions with intermediate magnetic fields and strong gradients in velocity. They are also the most affected by the degradation. On the other hand, within granules, profiles show features with smaller wavelength scales but their amplitudes are challenging to detect. Finally, profiles from the umbra are less complex in general because, as the convection is inhibited, the stratification tends to be simpler and the broadening due to the magnetic field makes the profiles show spectral scales much larger than the width of the LSF.

From the analysis of the spectropolarimetric inversions, the model complexity has a strong impact on the inversion results. This is found when the configuration with the highest number of nodes goes from providing the best results, in the original case, to the worst as soon as the spectra are degraded and the noise is included. Thus, the spectral degradation makes the inver-

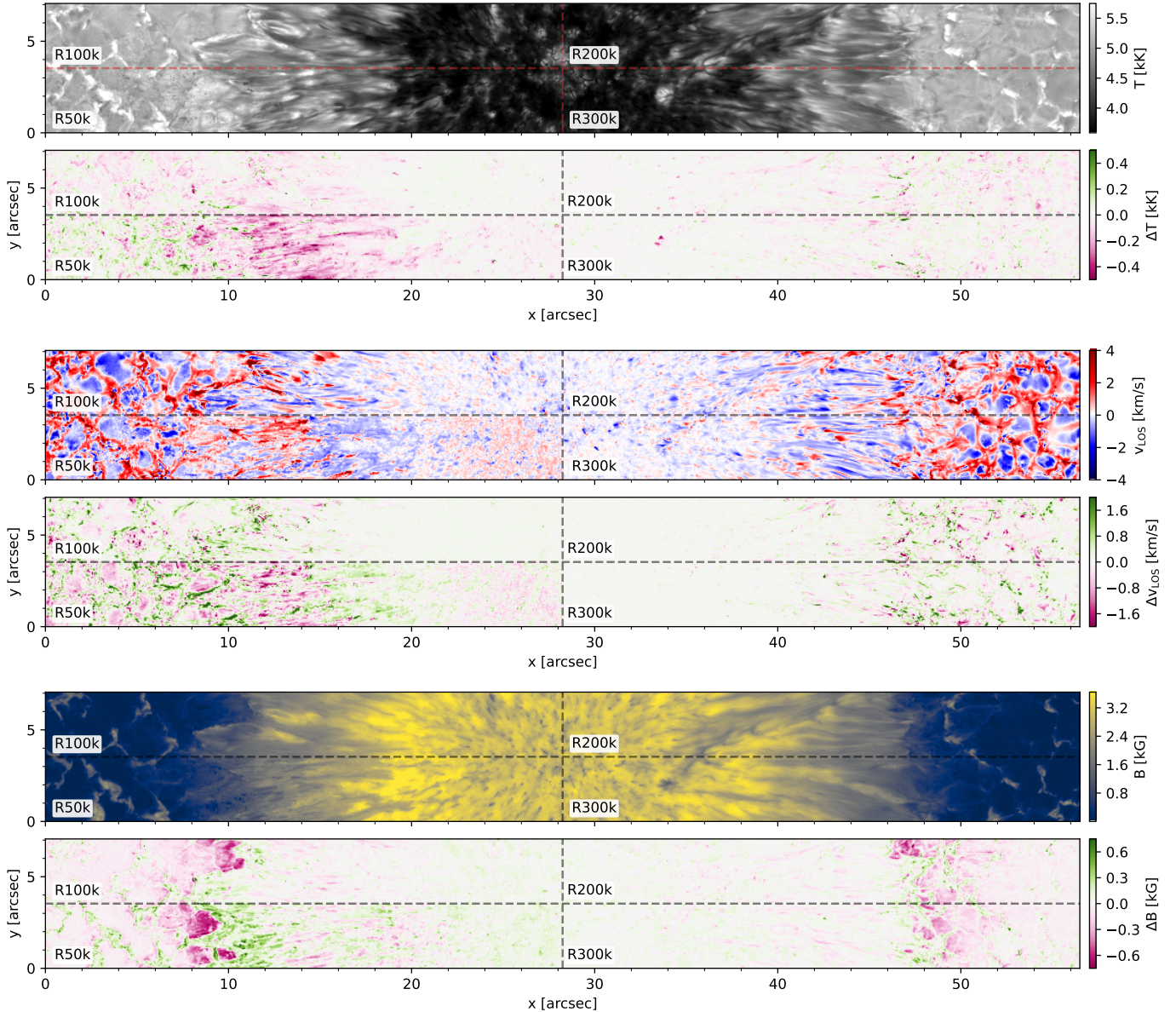


Fig. 13. Overview of the inferred physical parameters and the difference between the simulation and inversion at $\log \tau_{500} = -1$. The results for different spectral resolutions are shown in every corner of each map. From top to bottom: temperature, line-of-sight velocity, and magnetic field strength. A positive difference implies underestimation and negative overestimation of the given physical parameter.

sion process more ill-posed and the complexity of the model should be chosen carefully to avoid overfitting. To address this problem, for example, [Asensio Ramos et al. \(2012\)](#) proposed using Bayesian evidence ratios or simple proxies such as the Bayesian information criterion (BIC; [Schwarz 1978](#)) to compare quantitatively different models and favor more complex ones only when they remarkably improve the fit ([Sasso et al. 2011](#); [Díaz Baso et al. 2019b, 2022](#)). Nowadays, however, the new approach in some codes (STiC, SNAPI, FIRTEZ) consists of allowing a higher number of nodes but limiting the effective degree of freedom with a regularization term in the merit function, which will penalize strong gradients (both in the vertical and horizontal direction) if they are not needed when reproducing the observations ([Díaz Baso et al. 2025](#)).

Spectral sampling is also crucial and while in binned data the noise amplitude per wavelength bin is lower, the recovery of the physical parameters is more difficult. According to this experiment, having an over-sampled spectrum might be more bene-

ficial than having a higher S/N per wavelength bin. This is, of course, in tension with spectral range, as the coarser wavelength binning allows wider wavelength ranges for the same detector size ([Riethmüller & Solanki 2019](#); [Trelles Arjona et al. 2021](#)). Indeed, the combination of the two spectral lines with an approximated LSF provided better results than only one line with a perfect knowledge of the LSF. Given these results, we believe that the LSF can be inferred from the observations, but only if the LSF is coupled (a unique functional form across the FoV), as a pixel-wise version is a very degenerated problem, as is shown here. This spatially coupled strategy has shown successful results in determining atomic parameters in spectropolarimetric inversions by [Vukadinović et al. \(2024\)](#).

We can conclude that the extent of information loss due to spectral degradation relies on multiple factors (such as the spectral resolution, noise level, LSF functional form, physical properties of the solar atmosphere, and degree of freedom in our inversion method, among others). To mitigate this loss, we can

incorporate a good estimation of the LSF into the inversion process, avoid coarse samplings (e.g., post-factum spectral binning), and consider including different spectral lines that may compensate for these effects. Similar studies should be conducted under typical chromospheric conditions, in which the magnetic field is generally weaker and signals are easily obscured by noise (Díaz Baso et al. 2019c; Yadav et al. 2021). Consequently, additional studies, akin to this one, should be carried out to optimize the design of new instrumentation according to our scientific requirements (Schlichenmaier et al. 2019). Additionally, it is worth noting that spatial degradation has a more pronounced impact on information loss (e.g., Centeno et al. 2023; Milić et al. 2024). However, the advent of new-generation telescopes with larger apertures and improved adaptive optics systems will yield high-spatial-resolution observations in which spectral degradation becomes the primary source of information loss. This is likely even more critical when detecting subtle signatures of scattering polarization and Hanle effect (Zeuner et al. 2020; Centeno et al. 2022). Finding ways to mitigate this loss becomes crucial for the accurate interpretation of such observations.

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Appendix A: Dimensionality of the simulation

More complex depth stratifications of temperature, velocity, and the magnetic field vector, will result in more complex shapes of the Stokes profiles. This means that the dimensionality of the Stokes profiles is related to the dimensionality of the underlying atmosphere. To complement our results from Sect. 3, we show the dimensionality of the depth stratifications of the temperature, velocity, and magnetic field in our model atmosphere. We calculate the dimensionality following the same PCA approach as in Sect. 3 (see Eq. 2), where now the basis vectors are functions of optical depth. The dimensionality is calculated over the range of optical depths where the Fe I lines are sensitive to the stratification, i.e., $\log \tau_{500} = [0, -2]$. The threshold criteria used to determine this dimensionality are 5 K for the temperature, 0.01 km/s for the velocity, and 1 G for the magnetic field components, where we treat horizontal and vertical magnetic fields separately. Fig. A.1 shows the spatial distribution of these four physical parameters at the optical depth $\tau_{500} = 1$, while Fig. A.2 shows the spatial distribution of the dimensionality of the quantities mentioned above.

Appendix B: MPySIR: A parallel wrapper for SIR

As the original SIR code² (Ruiz Cobo & del Toro Iniesta 1992) is not parallelized and the inversion process of large datasets is computationally expensive, we have implemented a parallelized version of the SIR code, called MPySIR³. The code is written in Python and uses the MPI library to distribute the inversion task across multiple processors. This implementation does not modify the original SIR implementation, and all the MPI calls are done from Python.

This new implementation integrates in a single configuration file the previous functionalities of the SIR code and new functionalities related to the parallelization. Through this file, users can control various aspects, such as the input/output files, abundances, the mode of synthesis or inversion, the number of nodes for each physical parameter, and more. Additional features include debugging tools, the option to perform inversions only within a specified region of the dataset, the ability to combine different inversion results, the option to use previous inversion results as inputs for subsequent cycles, along with numerous other possibilities. The only feature that we did not carry over is multi-component inversions, mostly because we are interested in very high-resolution observations where we deem that feature unnecessary.

² Available at <https://github.com/BasilioRuiz/SIR-code>

³ Available at <https://github.com/cdiazbas/MPySIR>.

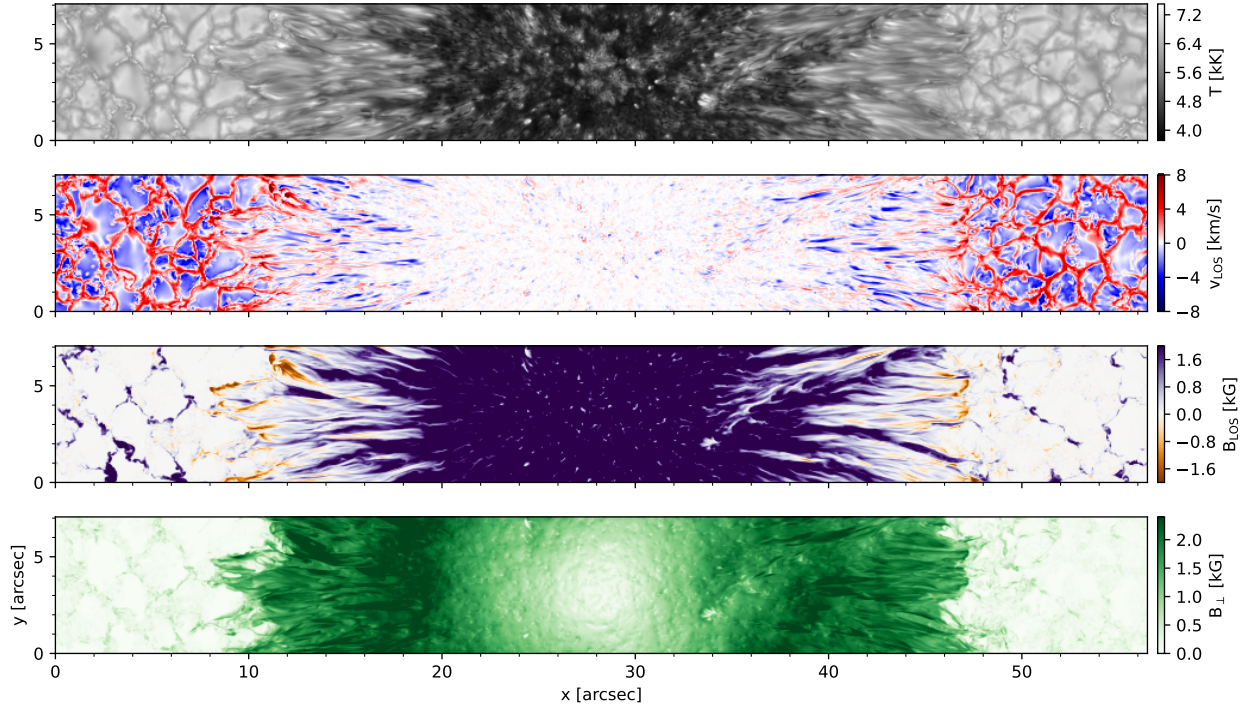


Fig. A.1. Overview of the physical parameters of the simulation at $\tau_{500} = 1$. From top to bottom: temperature, line-of-sight velocity, longitudinal magnetic field and transverse magnetic field.

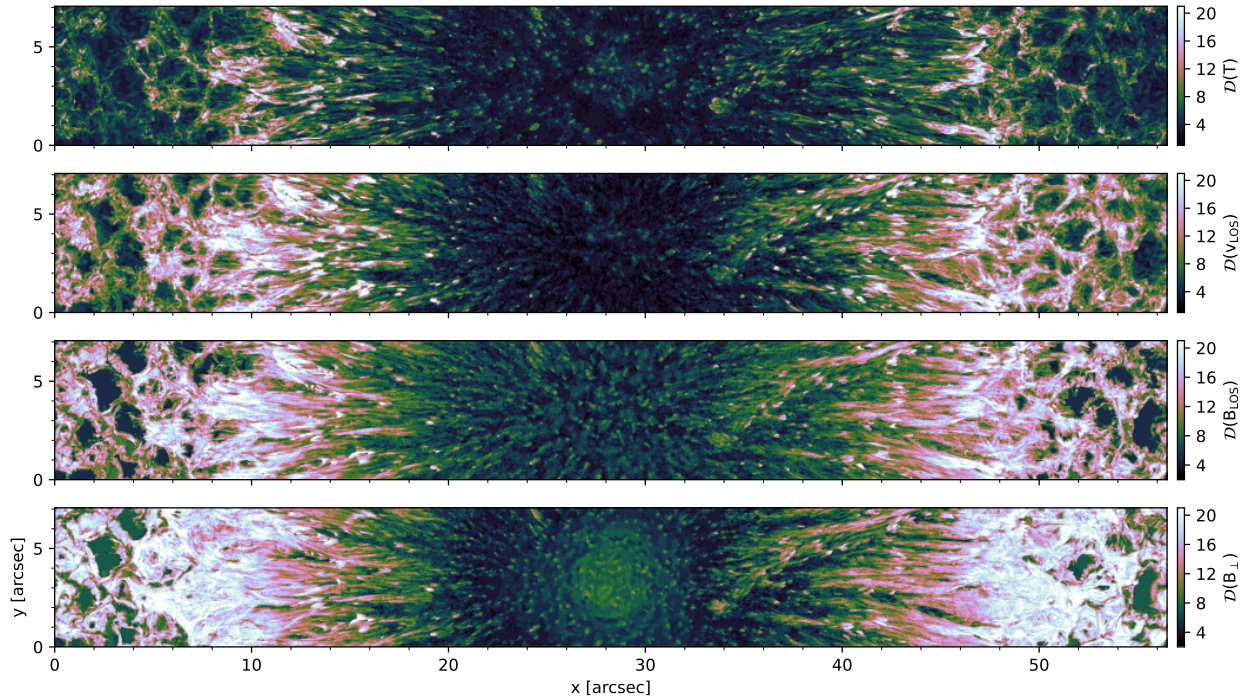


Fig. A.2. Dimensionality of each physical parameter of the simulation in the range $\log \tau_{500} = [0, -2]$ calculated using PCA and the following thresholds: 5 K for the temperature, 10^{-2} km/s for the velocity, and 1 G for the magnetic field components.