

Tempestuous life beyond R_{500} : X-ray view on the Coma cluster with SRG/eROSITA

I. X-ray morphology, recent merger, and radio halo connection

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ABSTRACT

This is the first paper in a series of studies of the Coma cluster using the SRG/eROSITA X-ray data obtained in the course of the calibration and performance verification observations. The data cover a $\sim 3^\circ \times 3^\circ$ area around the cluster with a typical exposure time of more than 20 ks. The stability of the instrumental background and operation of the SRG observatory in the scanning mode provided us with an excellent data set for studies of the diffuse emission up to a distance of $\sim 1.5R_{200}$ from the Coma center. In this study, we discuss the rich morphology revealed by the X-ray observations (also in combination with the SZ data) and argue that the most salient features can be naturally explained by a recent (ongoing) merger with the NGC 4839 group. In particular, we identify a faint X-ray bridge connecting the group with the cluster, which is convincing proof that NGC 4839 has already crossed the main cluster. The gas in the Coma core went through two shocks, first through the shock driven by NGC 4839 during its first passage through the cluster some gigayear ago and, more recently, through the “mini-accretion shock” associated with the gas settling back to quasi-hydrostatic equilibrium in the core. After passing through the primary shock, the gas should spend much of the time in a rarefaction region, where radiative losses of electrons are small, until the gas is compressed again by the mini-accretion shock. Unlike “runway” merger shocks, the mini-accretion shock does not feature a rarefaction region downstream and, therefore, the radio emission can survive longer. Such a two-stage process might explain the formation of the radio halo in the Coma cluster.

Key words. galaxies: clusters: general – galaxies: clusters: individual: Abell 1656 – galaxies: clusters: intracluster medium – X-rays: galaxies: clusters – radiation mechanisms: non-thermal – shock waves

1. Introduction

The Coma cluster (Abell 1656) is one of the best-studied clusters in all energy bands. The combination of its mass ($M_{500} \sim 6 \cdot 10^{14} M_\odot$; [Planck Collaboration Int. X 2013](#)) and proximity ($z = 0.0231$) makes it an attractive target – bright and well resolved – for many case studies. For instance, the presence of dark matter in the Coma cluster was suggested by Fritz Zwicky in 1933 based on velocity measurements of member galaxies ([Zwicky 1933](#)). The Coma cluster was one of the very first clusters detected in X-rays (e.g., [Boldt et al. 1966](#); [Forman et al. 1972](#)). In radio band, it became the first cluster where a radio halo (e.g., [Seeger et al. 1957](#); [Large et al. 1959](#); [Willson 1970](#)) and a radio relic (e.g., [Jaffe & Rudnick 1979](#); [Ballarati et al. 1981](#); [Gubanov 1982](#)) have been detected. In microwaves, it became the first nearby cluster detected ([Herbig et al. 1995](#)) via the Sunyaev-Zeldovich (SZ) effect ([Sunyaev & Zeldovich 1972](#)). Evidence for diffuse emission in the extreme ultraviolet band from the Coma cluster has been reported ([Lieu et al. 1996](#)). X-ray observations of the Coma cluster provided robust evidence ([White et al. 1993](#)) that the baryon fraction in the cluster is lower than that derived from the Big Bang nucleosynthesis in a flat cosmology without dark energy. Recently, analysis of statistical properties of the X-ray

surface brightness fluctuations allowed [Zhuravleva et al. \(2019\)](#) to measure effective viscosity in the turbulent magnetized gas of the intracluster medium in the Coma outskirts.

While initially classified as a relaxed cluster (e.g., [Kent & Gunn 1982](#)), it later became recognized as a merger (e.g., [Fitchett & Webster 1987](#); [Briel et al. 1992](#); [Neumann et al. 2003](#)). Recent studies of the Coma cluster in X-rays revealed a number of substructures, which are plausibly connected to the recent merger(s), namely, a prominent X-ray excess to the west of the Coma center ([Neumann et al. 2003](#); [Simionescu et al. 2013](#)), an excess to the east, elongated in the east-west direction ([Vikhlinin et al. 1997](#); [Neumann et al. 2003](#); [Simionescu et al. 2013](#)), the NGC 4839 group merging with Coma (e.g., [Burns et al. 1994](#); [Neumann et al. 2001](#); [Lyskova et al. 2019](#); [Malavasi et al. 2020](#); [Mirakhor & Walker 2020](#)), and high density “arms” in the Coma core ([Churazov et al. 2012](#); [Sanders et al. 2013, 2020](#); [Zhuravleva et al. 2019](#)). Similarly, remarkable progress with characterizing the Coma cluster has been achieved in the optical and radio bands ([Adami et al. 2005](#); [Malavasi et al. 2020](#); [Brown & Rudnick 2011](#); [Bonafede et al. 2021](#), among others).

Deep X-ray observations covering the entire cluster, including the outskirts, with good spectral and angular resolution are indispensable to address the following problems: (i) validating

and refining the scenario for a merger between the Coma cluster and the NGC 4839 group; (ii) providing an accurate characterization of the “baryonic boundary” of the cluster well beyond R_{500} , where the gas joins the cluster for the first time, and (iii) examining a connection between X-ray emission and radio sources Coma C and 1253+275, which themselves are the archetypes of clusters’ radio halos and radio relics, respectively.

Here (paper I), we focus on the merger scenario and its connection to the radio halo using the data from the eROSITA telescope on board the SRG observatory.

The SRG X-ray observatory (Sunyaev et al. 2021) was launched on July 13, 2019, from the Baikonur cosmodrome. It carries two wide-angle grazing-incidence X-ray telescopes, eROSITA (Predehl et al. 2021) and the *Mikhail Pavlinsky* ART-XC telescope (Pavlinsky et al. 2021), which operate in the overlapping energy bands of 0.3–10 and 4–30 keV, respectively. On December 13, 2019, upon completion of the commissioning, calibration, and performance verification phases, SRG started its all-sky X-ray survey from a halo orbit around the Sun–Earth L2 point, which will consist of eight repeated 6-month-long scans of the entire sky. Here we report the first (preliminary) results on the Coma cluster obtained in the course of the calibration and performance verification observations by SRG/eROSITA. The large field of view of eROSITA combined with operation in a special scanning mode provided an exceptionally uniform and deep X-ray image covering ~ 10 sq. degrees centered on the Coma cluster.

Throughout the paper, we assume a flat Lambda cold dark matter (Λ CDM) cosmology with $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$, $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. At the redshift of the Coma cluster of $z = 0.0231$, one arcmin corresponds to 27.98 kpc. We assume $r_{500} = (47 \pm 1)$ arcmin (Planck Collaboration Int. X 2013) and $r_{200} \simeq 1.5r_{500} \simeq 70$ arcmin for the concentration parameter $c \simeq 4$ typical for massive galaxy clusters (e.g., Klypin et al. 2016, among others). For all radial profiles, we fix the Coma center at (RA, Dec) = $(12^h59^m47^s, +27^\circ55'53'')$, as it is done in Planck Collaboration Int. X (2013).

2. Observations and data handling

The SRG observations of the Coma cluster were performed in two parts, on December 4–6, 2019 and June 16–17, 2020. The observatory was in a scanning mode (not to be confused with the survey mode), during which a rectangular region of the sky is scanned multiple times to ensure uniform exposure of the region. In both observations, the telescope axis was scanning across the $\sim 3 \times 3^\circ$ field, albeit with a slight shift in the position angle between the two sessions. Here we report on SRG/eROSITA data obtained during these observations.

In order to produce the calibrated event lists, the raw data were reduced using the eSASS software. Based on the analysis of the light curves, the data were cleaned of obvious artifacts. After the data cleaning, the accumulated exposure is fairly uniform over the $\sim 3^\circ \times 3^\circ$ field, reaching ~ 23 ks per point at the center.

The detector intrinsic background was estimated using the data from the all-sky survey collected during the periods when the filter wheels of the telescope modules were in the “CLOSED” position (i.e., when the telescope detectors were not exposed to the X-ray emission of astrophysical origin). The total background (intrinsic detector background plus astrophysical background) was estimated using observations of deep fields, taking the fraction of the resolved sources into account. Since the limiting flux of the resolved sources varies across the

studied field (due to the contribution of the Coma cluster emission and variations in the exposure time at the edges of the field), the total background was interpolated (see Appendix A) assuming a Log N–Log S curve in the 0.5–2 keV band derived from *Chandra* deep fields (Luo et al. 2017).

For the science analysis, only X-ray events within $28'$ from the center of the detector were used. Since the scanning mode is largely similar to the survey mode, we use the point spread function (PSF) of the telescope estimated via stacking many compact sources in the all-sky survey data. It turns out that a simple β -model (see Appendix B) provides a reasonable approximation for the shape of the PSF core.

In this study, we use the data from all seven eROSITA telescope modules for imaging, while the spectral analysis is limited to five telescopes equipped with the on-chip filter. These telescopes have a very similar response and, as a first approximation, the data can be directly co-added (as opposed to a more rigorous joint analysis of spectra obtained by individual telescopes). For the remaining two telescopes, we defer the analysis to future publications, when the quality of the spectral response calibration will allow the joint analysis to be performed. We reiterate here that some aspects of the eROSITA calibration are still preliminary, especially when dealing with hot clusters such as Coma. We, therefore, adopted a conservative approach and report here only the results that are robust against these uncertainties. Minor changes, especially related to the accurate temperature measurements, are still possible and will be reported elsewhere.

We note in passing that observations of the Coma cluster happened at the time of the Solar minimum. As a result, time variations in the detector particle background turned out to be small (see Pavlinsky et al. 2021; Sunyaev et al. 2021) and the solar wind charge exchange (SWCX) emission is expected to be minimal as well. The impact of the latter component was found to be important for the analysis of the *XMM-Newton* data on the Coma cluster (e.g., Takei et al. 2008). The location of the SRG at the L2 point already eliminates the contribution of near-Earth regions to SWCX, leaving the heliosphere and the He-focusing cone as possible sites for the production of SWCX. The analysis of the SWCX as seen by the SRG observatory will be reported elsewhere. Here we only note that the data accumulated during two Coma observations separated by ~ 6 months agree well, effectively providing good constraints on the (variable) SWCX flux.

3. X-ray images

The 0.4–2 keV band image of the full field, (detector) background subtracted, exposure corrected, and smoothed with a kernel corresponding to the telescope PSF is shown in Fig. 1 (with logarithmic color-coding). Such a smoothing kernel is chosen to optimize the sensitivity to faint point sources when the background dominates the signal.

A finding chart for the studied field is shown in Fig. 2, where black contours show the X-ray surface brightness. Three dashed circles indicate R_{500} , R_{200} and $2 \times R_{200}$ of the Coma cluster. It follows that the data cover the region up to $\sim 1.5 \times R_{200}$ extremely well. The extension of X-ray contours at $\sim R_{500}$ to the SW is due to the NGC 4839 group, which is in process of merging with the main cluster (e.g., Mellier et al. 1988; Neumann et al. 2001, among many others). This extension is aligned with the direction of a prominent filament of galaxies (e.g., Malavasi et al. 2020). Farther out in the same direction, at $\sim R_{200}$, is located the famous radio relic source 1253+275.

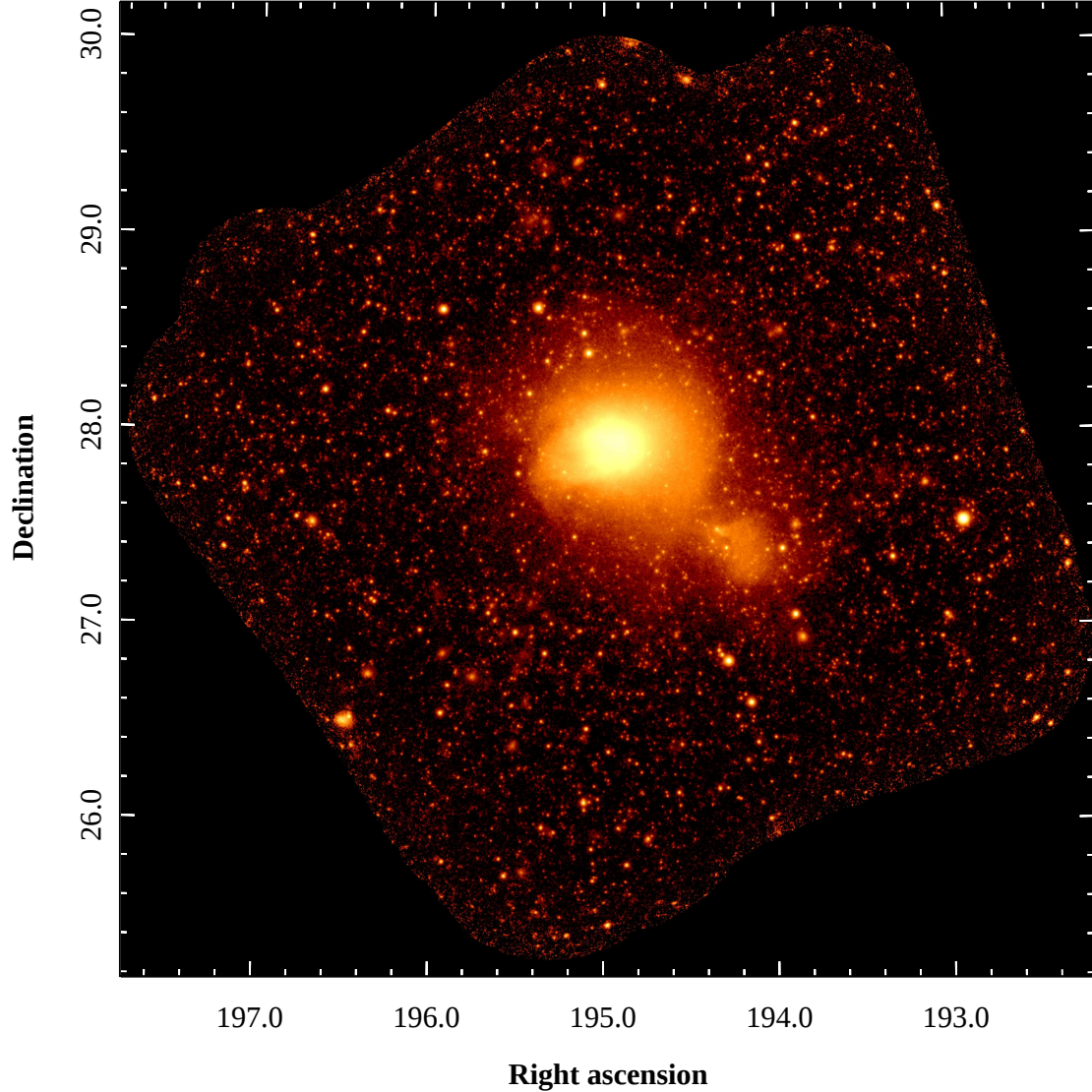


Fig. 1. X-ray image (background subtracted, exposure corrected) of the Coma cluster field in the 0.4–2 keV band accumulated during two scanning observations. The image is ~ 6 degrees on a side, corresponding to 10 Mpc at the distance of the cluster, with the logarithmic color-coding on a scale spanning five orders of magnitude.

A multitude (some 5000) of compact and diffuse sources is seen in the image, most of them being background active galactic nuclei (AGNs). The sensitivity to point sources is a few 10^{-15} erg cm $^{-2}$ s $^{-1}$ outside the very central region, where the diffuse emission from Coma dominates, and the very edges, where the exposure drops. The analysis of background AGNs and distant clusters, as well as foreground Galactic objects, in the Coma field will be reported in separate publications.

The pseudo-color RGB version of the X-ray image is shown in Fig. 3. It is based on a combination of the 0.3–0.6, 0.6–1.0, and 1.0–2.3 keV images derived from the same data set. The colors were tuned to emphasize the emission from galaxy clusters. The overall reddish color of the image is due to the soft diffuse emission, in particular the OVII line, to which the Milky Way makes the dominant contribution. In this map, AGNs appear as bluish or yellowish objects, while galaxy clusters, including the Coma cluster itself, the NGC 4839 group, and more distant background clusters have a distinct white color.

One can readily detect and subtract point (or mildly extended) sources from the image in order to get a better view

of the large-scale distribution of Coma’s diffuse emission. An image of the diffuse emission in the central $\sim 2 \times 2$ degrees of the field, corresponding to ~ 3.2 Mpc, is shown in Fig. 4.

All these images demonstrate rich morphology of the Coma cluster on Mpc scales, including a number of sharp “edges” close to R_{500} . The qualitative study of these structures is the primary focus of this paper.

3.1. Radial X-ray surface brightness profile

The radial profile of the X-ray surface brightness in the 0.4–2 keV band is shown in Fig. 5. A 90° wedge to the SW, which contains the NGC 4839 group, has been excluded from this analysis. The green points correspond to the total observed surface brightness profile. For comparison, the estimated total background surface brightness (detector intrinsic background plus astrophysical background) is shown with the dashed horizontal line. The red data points correspond to the surface brightness after excising sources and removing various components of the background, including the estimated contribution of the “stray

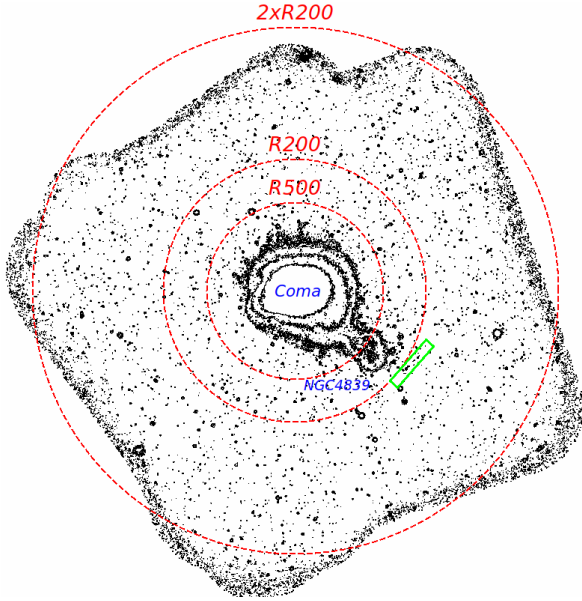


Fig. 2. Sketch of the Coma field with three circles showing estimated R_{500} , R_{200} , and $2 \times R_{500}$. The NGC4839 group is approximately at R_{500} (~ 1.3 Mpc). The green box marks the brightest part of the radio relic (radio source 1253+275), which is just outside R_{200} (~ 2.1 Mpc from the Coma center).

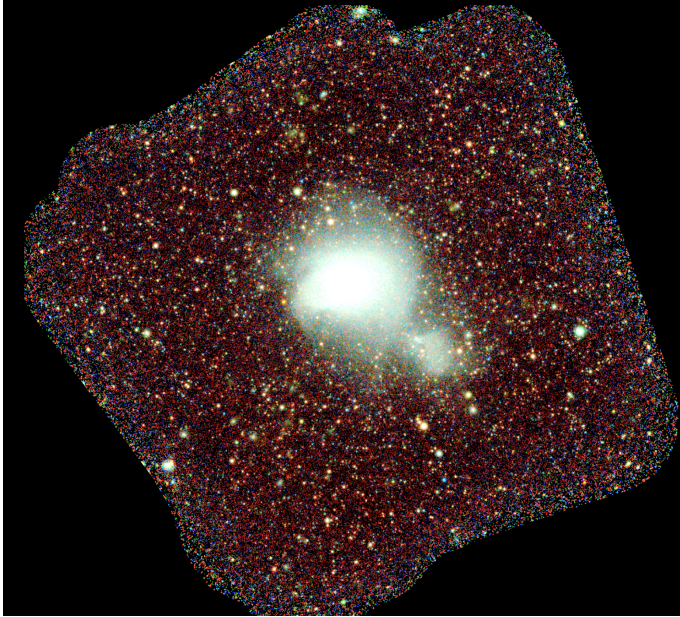


Fig. 3. Pseudo-color RGB image of the Coma cluster field based on a combination of 0.3–0.6, 0.6–1.0, and 1.0–2.3 keV images. The diffuse emission, which is dominated by the Milky Way contribution appears red in this image. Distant AGNs and a few galactic sources (including stars) span full range of colors. Clusters of galaxies, including the Coma cluster itself, appear as extended white objects in this image.

light,” which is associated with photons scattered by the mirrors only once (as opposed to the nominal two-scattering scheme in the Wolter I mirrors).

The radial profile of the stray light component, which extends to some 3° from the source, was estimated using observations of the brightest compact objects in the all-sky survey. The X-ray image (after subtraction of the detector intrinsic background)

was been convolved with the stray-light profile, yielding the estimated contribution of the singly scattered photons to the observed radial profile¹. This estimated contribution is shown in Fig. 5 with the cyan dashed line. Since the X-ray signal from the bright sources used to derive the stray-light profile suffer from the pile-up effect, an accurate estimate of the stray-light contribution is problematic. We, therefore, defer the discussion of the X-ray radial profile at the largest radii to subsequent studies. In the present study, we focus on the data within R_{200} , where the importance of the stray-light component is less critical.

Despite the remaining uncertainty in the stray-light magnitude, it is clear that with the present data set, the X-ray surface brightness profile can be traced all the way to $\sim 100'$, corresponding to $\sim 1.4 \times R_{200}$. At this distance, the X-ray surface brightness is 5×10^4 times smaller than in the core of the cluster. For comparison, the purple line in Fig. 5 shows the estimated root-mean-square (RMS) of the X-ray flux variations associated with the pure Poisson noise of the number of unresolved CXB sources using the known Log N-Log S taken from Luo et al. (2017). Clearly, this is not the main source of uncertainty in the present data set.

In Appendix D, we compare the radial profile extracted from the eROSITA all-sky survey data with the 0.4–2.4 keV profile obtained by ROSAT. The good agreement of these profiles suggests that the background subtraction and the correction for the stray-light contribution do not introduce any major biases.

3.2. Flat-fielded X-ray image

As shown in the previous section, the traceable X-ray surface brightness varies by almost four orders of magnitude from the core to the outskirts. To cope with such a large dynamic range and to emphasize faint non-radial structures in the X-ray image, it is useful to artificially suppress the brightness of the core. A simple β -model with $r_c = 10.4'$ and $\beta = 0.73$ provides a reasonable first-order approximation to the observed profile. A division by the β -model would flat-field the image, but it would also boost the noise in the cluster outskirts. We, therefore, divided the image by the following function

$$f(r) = 1 + \frac{c}{[1 + (r/r_c)^2]^{3\beta - \frac{1}{2}}}, \quad (1)$$

where c is set to 30. With this definition, the division of the image by $f(r)$ at $r \ll r_c$ is equivalent to the division by the beta model. At large r , the value of $f(r)$ approaches unity, that is the image is unchanged. The parameter c controls the transition radius and, implicitly, the level of the core brightness suppression relative to the outskirts, which is a factor $c + 1 = 31$ in our case. The resulting image is shown in Fig. 6.

This image reveals some of the features, which appear less prominently in the original image. Some of these features have already been noticed in the ROSAT, *XMM-Newton* and *Chandra* images (e.g., Vikhlinin et al. 1997; Donnelly et al. 1999; Watanabe et al. 1999; Neumann et al. 2003; Sanders et al. 2013; Simionescu et al. 2013; Mirakhor & Walker 2020), although in the flattened eROSITA image these features can now be traced over their full extent². The most spectacular is a bow-like sharp

¹ Formally the singly scattered photons should be removed from the observed profile before the convolution. Here we ignore this second-order effect.

² We note in passing that the choice of the flat-fielding procedure is ambiguous and another procedure would lead to a slightly different appearance of the image.

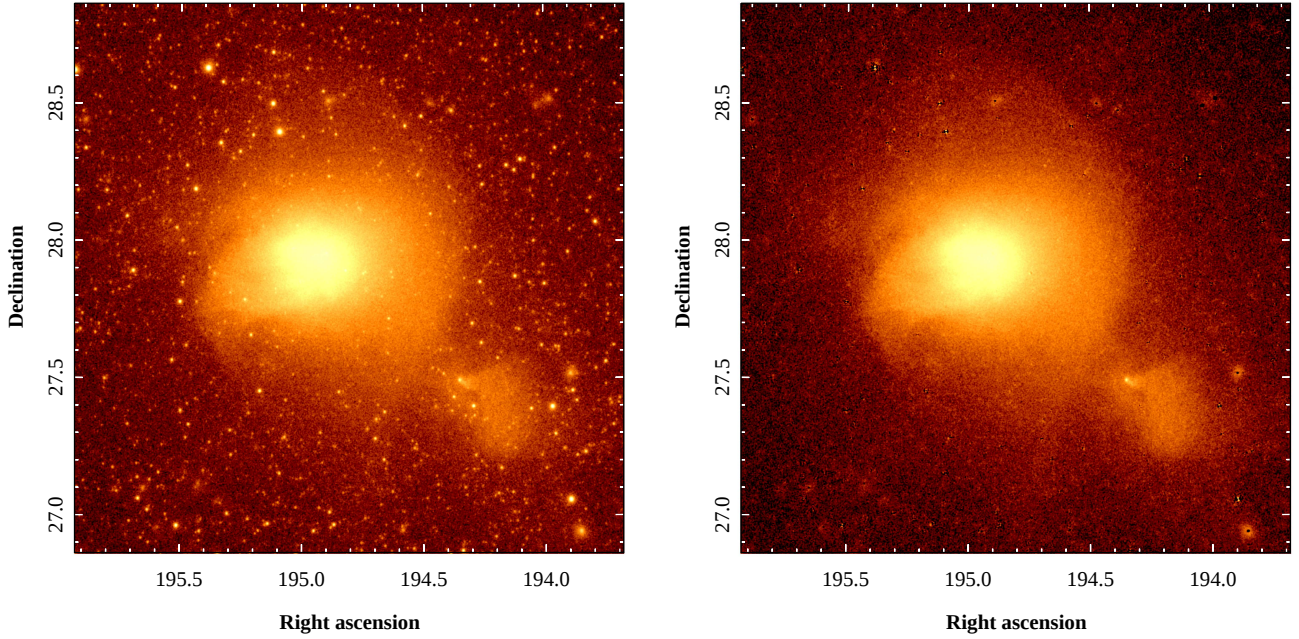


Fig. 4. X-ray image of the central $\sim 2 \times 2$ degrees of the field showing 0.4–2 keV surface brightness on a logarithmic scale. *Left panel:* original image without subtraction of the multitude of foreground, background and Coma-related sources. *Right panel:* map of the diffuse emission obtained after modeling and subtraction of the confidently detected point-like and mildly extended sources using the β -profile approximation of the PSF described in Appendix B.

feature to the west of the core, which is believed to be a shock (hereafter “W-shock”). In the eROSITA image, the W-shock boundary can be traced over ~ 3 Mpc. Another sharp feature is seen to the east of the core, which turns out to be a contact discontinuity (see below).

In addition, there are several new features that can be seen in this image. In particular, these include: (i) a faint “bridge” connecting the main cluster and the NGC4839 group; (ii) an extended diffuse region to the west of the main cluster (better seen in the smoothed image; see Sect. 4); (iii) several faint filaments extending to the south barely visible in the image; (iv) a trace of an extended (in the north-south direction) surface brightness edge to the east of the core, which is reminiscent of a Bullet cluster shock (e.g., Markevitch et al. 2002; Di Mascolo et al. 2019) ahead of a contact discontinuity. We discuss the origin of some of these features in the subsequent sections.

3.3. Edges in X-ray image

The original and flattened X-ray images shown above feature a number of long but sharp “edges”. Some of these structures are Mpc-long, while in the transverse direction the surface brightness changes over some 10 kpc or less. There are several plausible explanations for the X-ray appearance of such structures (see, e.g., Markevitch & Vikhlinin 2007, for a review), namely (i) a shock front, when the pressure is changing across the edge and (ii) a contact discontinuity, when the pressure is continuous across the edge.

In the X-ray data, the shocks reveal themselves as structures that have brighter (denser) and hotter gas on the same side of the interface, while the opposite is true for the contact discontinuities.

In regard to contact discontinuities, one can further distinguish several cases: (a) discontinuity separating the Coma gas from the gas brought into the main cluster by the merger (could be still bound to the infalling halo or already stripped from it); (b)

a displaced lump of the main cluster gas, which was brought (by motions) into contact with another lump with different entropy (also from the main cluster); (c) a contact discontinuity arising due to shock crossing (e.g., Birnboim et al. 2010; Zhang et al. 2020a); (d) a contact discontinuity associated with the variations of the fractional contribution of cosmic rays and magnetic fields to the total pressure.

The latter type of contact discontinuities is more relevant for cool core clusters, where bubbles of relativistic plasma created by a central AGN displaces the gas, while the first three could be present in a merging cluster, e.g., in Coma.

The quality of the present data set allows one to robustly classify the most prominent features seen in Fig. 6. In Fig. 7, we show surface brightness and (projected) temperature profiles from two sectors, toward the west and the east of the cluster core with the position angles of $(-18^\circ, 40^\circ)$ and $(190^\circ, 230^\circ)$ respectively. Based on the observed radial profiles, we classify the west surface brightness edge as a shock front with the Mach number of ~ 1.5 , in agreement with the previous finding of Uchida et al. (2016); Planck Collaboration Int. X (2013).

Although the edge feature to the east of the Coma core is interpreted as a shock in Planck Collaboration Int. X (2013), the eROSITA temperature profile clearly shows that the denser region is actually colder than the less dense region, identifying this edge as a contact discontinuity. This does not exclude a possibility of a weak shock ahead of the cold front (farther to the east). A strong shock can be excluded since it would show up prominently in X-ray images. However, a weak (perhaps, transient) bow shock driven by a sloshing gas cannot be entirely excluded by the current analysis. We defer the detailed discussion of this feature for subsequent studies.

4. X-ray and SZ images

Due to different dependences of the X-ray and SZ signals on the gas density and temperature, it is possible to use them in order

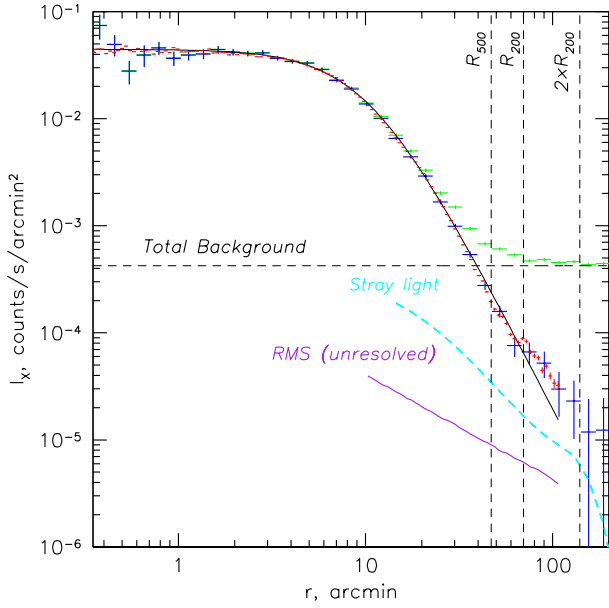


Fig. 5. Radial surface brightness profile of the Coma cluster in the 0.4–2 keV band. The surface brightness is normalized per single (out of seven) eROSITA telescopes. The 90° wedge in the SW direction, which contains the NGC 4839 group, has been excluded from the analysis. The green points show the raw surface brightness (including all types of the background) as measured in the all-sky survey. The blue points are the same data after excising compact sources and removing different types of the residual background and foreground (both instrumental and astrophysical), and subtracting the estimated contribution of the stray light. The red points show similarly processed data from the data set discussed in this paper. For comparison, the thin black line shows a β -model with the co-radius $r_c = 10'$ and $\beta = 0.73$. Three vertical lines show R_{500} , R_{200} , and $2 \times R_{200}$. The dashed horizontal line shows the total background in the 0.4–2 keV band. The cyan curve shows the estimated level of the stray light, which was removed from the profiles. At the moment of writing, the exact shape and normalization of this component are still uncertain. Finally, the purple line shows the estimated level of flux variations associated with the Poisson fluctuations of the number of unresolved sources (in the outer regions where the Coma contribution is subdominant).

to constrain the gas thermodynamic properties or variations of these properties (see, e.g., Ghirardini et al. 2018; Churazov et al. 2016). In particular, Mirakhor & Walker (2020) combined the *XMM-Newton* and *Planck* data on the Coma cluster in a number of wedges. With the extended spatial coverage provided by eROSITA, it is now possible to further advance the joint analysis of the SZ and X-ray data. To this end, we constructed a 2D map, which characterizes the density-weighted projected gas temperature distribution. When doing so, we made two simplifying assumptions.

First, we assumed that the X-ray emissivity in the 0.4–2 keV band is largely independent of the gas temperature, which a good approximation for hot clusters (see Appendix C), namely the X-ray surface brightness

$$I_X = \int n_e^2 \epsilon_c(T) dl \approx \epsilon_c(\langle T \rangle) \int n_e^2 dl, \quad (2)$$

where $\epsilon_c(T) \approx \text{const}$ is known. The second assumption is that, to the first approximation, the surface brightness distribution (and the underlying 3D distributions of density) can be described by the β -model as shown above.

The X-ray and SZ images of the Coma cluster ($\sim 4.4 \times 4.4$ degrees) are shown in Fig. 8. The X-ray image is the same as shown in Fig. 1 with compact sources excised and smoothed with a Gaussian filter ($\sigma = 200''$). The SZ image shown is largely similar to the one used in Planck Collaboration Int. X (2013). The contours in both images come from the SZ data; the lowest contour corresponds to the Compton parameter $y = 2.5 \times 10^{-6}$. Each subsequent contour is factor of two higher. Here

$$y = \frac{\sigma_T}{m_e c^2} \int k T n_e dl \equiv k \tilde{T} \frac{\sigma_T}{m_e c^2} \int n_e dl, \quad (3)$$

where $\tilde{T}$ is the electron-density-weighted temperature $\tilde{T} = \int T n_e dl / \int n_e dl$.

The close correspondence of the faint diffuse structures in X-rays and SZ images, which extend beyond R_{500} is clear, including a well known extension in the direction of NGC 4839, but also fainter extensions to the west of the core and in the SE direction, which can already be recognized in the flattened X-ray image, albeit barely (Fig. 6). This correspondence suggests that these extensions are due to diffuse gas rather than a combination of faint unresolved compact X-ray sources.

While the appearance of the X-ray and SZ images is largely similar, the quality of the data in the central region is sufficient to make a point by point comparison on spatial scales large enough so that the limited angular resolution of the *Planck* data is not a major issue.

The electron-density-weighted temperature $\tilde{T}$ can be expressed through the ratio of the two images as

$$k \tilde{T} \approx \frac{y}{I_X} \frac{m_e c^2}{\sigma_T} \frac{1}{4\pi} \frac{1}{(1+z)^2} \epsilon_c \left(\frac{n_H}{n_e} \right) \frac{\int n_e^2 dz}{\int n_e dz}, \quad (4)$$

where I_X is the surface brightness in $\text{counts s}^{-1} \text{sr}^{-1}$, ϵ_c is the eROSITA counts “production rate” per unit emission measure for a plasma with a given temperature. For eROSITA $\epsilon_c(T) \approx \text{const} \approx 50 \times 10^{-14} \text{ counts s}^{-1} \text{cm}^5$ (see Appendix C); $\left(\frac{n_H}{n_e} \right) \approx 0.83$ for the ICM. The last term can be evaluated only under assumption of a known 3D gas density distribution. For a beta model, this term reduces to

$$\frac{\int n_e^2 dz}{\int n_e dz} = \frac{n_{e,0}}{\left[1 + \left(\frac{r}{r_c} \right)^2 \right]^{3/2\beta}}, \quad (5)$$

where $n_{e,0} \sim 4 \times 10^{-3} \text{ cm}^{-3}$ is taken from deprojected spectral analysis. Since eROSITA images have higher spatial resolution than the *Planck* ones, the above correction factor was first applied to the eROSITA 0.4–2 keV image, which was then smoothed with a broad Gaussian ($\sigma \approx 250''$) to match (approximately) the angular resolution of *Planck*. Compact sources have been subtracted from the image prior to smoothing. To avoid excessive noise at the edges of the map, the ratio was computed only over the area, where the surface brightness of the Coma emission is larger than the $\sim 25\%$ of the surface brightness due to the nominal background.

Overall, the recovered temperature map agrees well with the X-ray measurements of the projected temperature, which show $\sim 8 - 10 \text{ keV}$ in the core (e.g., a temperature map in Sanders et al. 2013; Lyskova et al. 2019). In the eROSITA+*Planck* map, this temperature range corresponds to green color. To the north from the core, the temperature increases to $\sim 15 \text{ keV}$. This is slightly

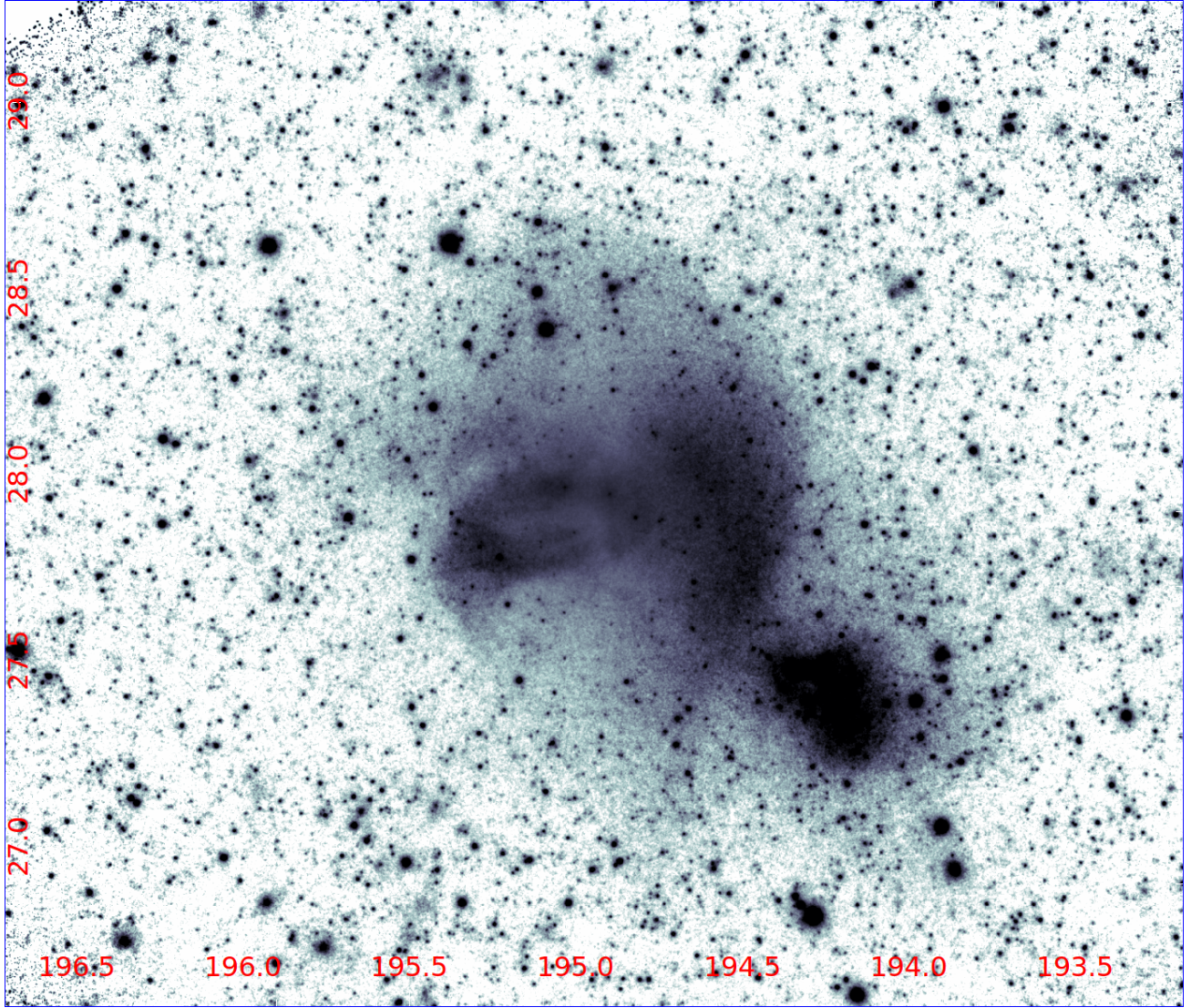


Fig. 6. Flat-fielded 3.5×2.4 degrees X-ray image of the Coma cluster. Flat-fielding procedure (see Eq. (1)) emphasizes departures from a smooth purely radial profile. The most spectacular is the bow-like sharp feature to the west of the core, which extends over ~ 3 Mpc from the north to the south. To the east of the core, there is another very sharp feature (~ 500 kpc in size), which turns out to be a contact discontinuity (see below). The NGC4839 (a dark spot to the SW from the core) appears to be connected with the main cluster via a rather faint “bridge.” In addition, one can spot a number of fainter filaments/extensions, which will be discussed in the forthcoming studies.

higher than typically found in X-ray data, although a tentative presence of a “hot spot” to the north was reported earlier (e.g., Donnelly et al. 1999; Watanabe et al. 1999). Also, the central part of the map is in reasonable agreement with the recent *XMM-Newton*+*Planck* temperature map by Mirakhor & Walker (2020). There are other prominent features in this image. First, there a “cold” spot toward the location of NGC 4839, well consistent with the presence of dense and relatively cold gas in this group (see, e.g., a temperature map in Lyskova et al. 2019; Mirakhor & Walker 2020). Another “cold” spot is to the SE from the core, which was seen in the *ASCA*, *Chandra* and *XMM-Newton* maps (e.g., Donnelly et al. 1999; Watanabe et al. 1999; Neumann et al. 2003; Sanders et al. 2013; Mirakhor & Walker 2020) and is tentatively associated with the infall of a galaxy group (e.g., Vikhlinin et al. 1997).

We note in passing that the manipulation with X-ray and SZ images described above is expected to produce a robust and meaningful characterization of the gas temperature only if the adopted 3D model (a beta-model in our case) is correct. Presence

of the NGC 4839 group obviously violates this assumption. Another structure affected by the same problem is the sharp discontinuity to the west of the core, which is a Mach ~ 1.5 shock (see Fig. 6) that does not show up prominently in this image. One possible reason for that might be a long electron-ion equilibration time on the downstream side of the shock, but for $M \sim 1.5$ this effect is expected to be small. There are, however, two other reasons why the “cold” spots appear more clearly in 2D images as discussed below.

If we neglect the temperature dependence of ϵ_c , the amplitudes of the X-ray and SZ signals at the shock front can be immediately compared as the ratio of the electron pressure and density squared jumps for the standard Rankine–Hugoniot conditions (assuming that electron and ion temperatures are equal). Namely,

$$YX_{\text{jump}} \equiv \frac{P_d/P_u}{\rho_d^2/\rho_u^2} = \frac{(2 + M^2(\gamma - 1))^2(1 + \gamma(2M^2 - 1))}{M^4(1 + \gamma)^3}, \quad (6)$$

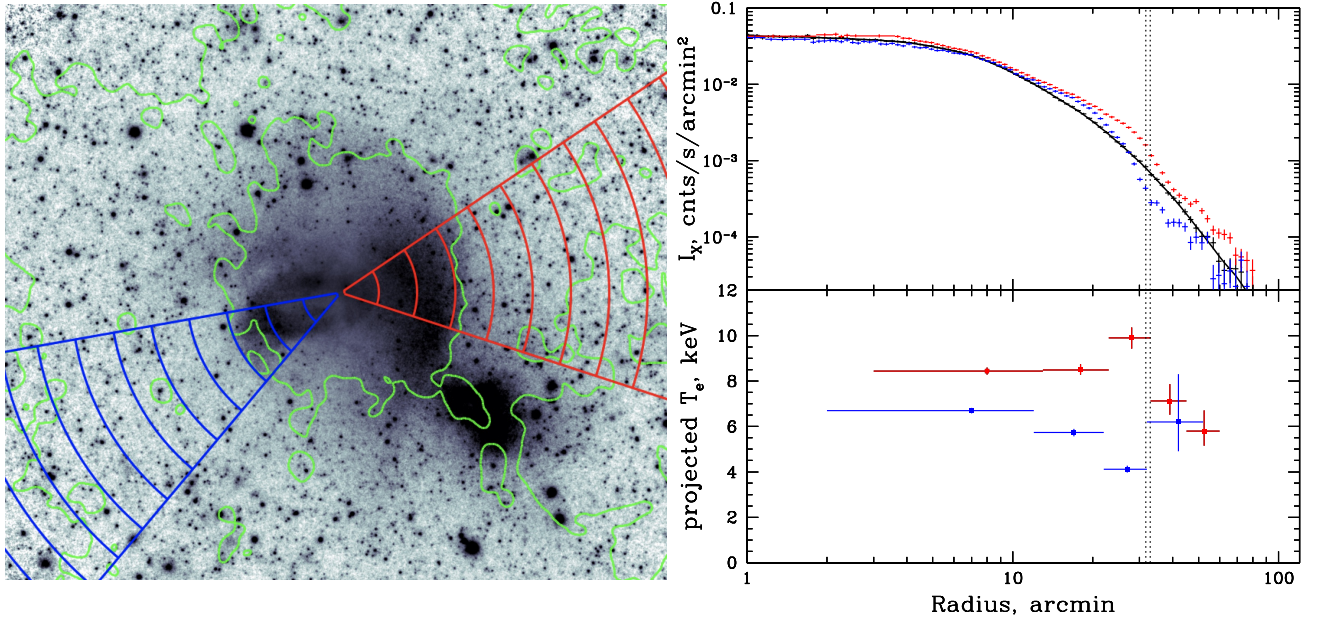


Fig. 7. Characterization of two sharp features in the X-ray image to the east and west of the Coma core. *Left:* two wedges used for extraction of the X-ray surface brightness and the spectral analysis. The flattened X-ray image is used as a background. For convenience, $10'$ rings are shown. The green contours show the brightness of the WSRT radio image at 352 MHz (Brown & Rudnick 2011). The inner contours approximately correspond to the boundary of the Coma radio halo. *Right:* surface brightness and projected temperature profiles to the west (in red) and to the east (in blue) of the Coma center. To highlight surface brightness gradients, the top panel shows also the azimuthally averaged profile I_X (the same as in Fig. 5) in black. To the west, sharp surface brightness discontinuity at $R \approx 33$ arcmin coincides with the temperature decline. Thus, our observations confirm the presence of a shock wave in the west with the Mach number of $M \approx 1.5$. The dotted line marks the position of the shock. To the east, we observe that the denser region is colder than the more rarefied region, thus making the eastern feature the cold front. The dotted lines show the positions of the X-ray surface brightness jumps.

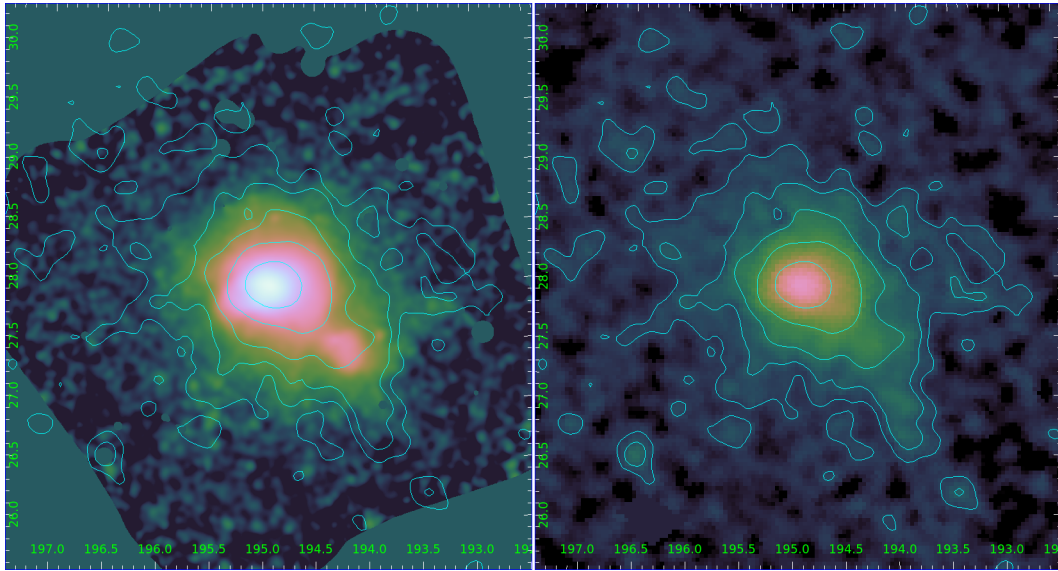


Fig. 8. 0.4–2 keV X-ray and SZ images of the Coma cluster. Compact sources have been excised from the X-ray image before smoothing with the broad Gaussian ($\sigma = 200''$). The size of the smoothing kernel was chosen to approximately match the angular resolution of the *Planck* Y-map. Contours from SZ image are shown in both panels. Many non-axisymmetric features in these two images match suggesting that they are due to the presence of hot gas.

where M is the shock Mach number, and the subscripts u and d correspond to the upstream and downstream sides, respectively. The minimum of YX_{jump} (see Fig. 9) is at

$$M_{\min} = \left(\frac{\gamma + \sqrt{\gamma(\gamma(5-2\gamma)-2)}}{\gamma(\gamma-1)} \right)^{1/2}. \quad (7)$$

For $\gamma = 5/3$, $M_{\min} \approx 1.6$ and at this Mach number $YX_{\text{jump,min}} \approx 0.87$; while at $M \approx 2.4$ the jump amplitudes are equal.

Now consider the behavior of the ratio of SZ and X-ray images (see Eq. (4)) when thermodynamic properties of a small lump (of otherwise isothermal) gas with along the line of sight are modified, so that electron pressure changes by a factor $1 + \eta_y$, while the density squared changes by another factor $1 + \eta_x$, where

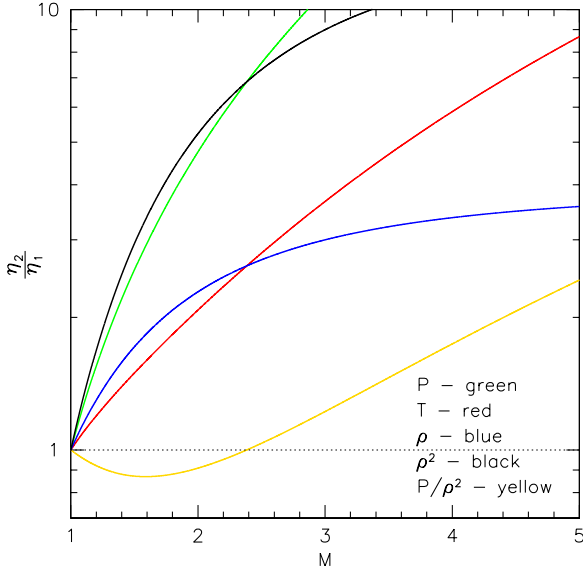


Fig. 9. Comparison of the “X-ray” and “Y” jumps for a shock in a gas with adiabatic index $\gamma = 5/3$ as a function of the shock Mach number M . Rankine–Hugoniot conditions provide jumps in thermodynamic properties (ρ , T or P). The ratio of P/ρ^2 approximately characterizes the ratio of the jumps in effective volume emissivities for X-rays and tSZ upstream and downstream of the shock. For $M \lesssim 2.4$, the jump in Y is smaller than in X-ray volume emissivities, implying that the shock appears slightly less prominent in Y than in the X-ray surface brightness. The minimum of the ratio (ignoring the temperature dependence of X-ray emissivity) is at $M \approx 1.6$ and is equal to 0.87.

$\eta_y \ll 1$ and $\eta_x \ll 1$. The smallness of η_y and η_x is needed here only to illustrate more clearly their impact on the derived temperature (by making Taylor expansion). In this case, the following variation of the gas temperature, derived from Eq. (4) is expected

$$\tilde{T} \propto \frac{(1 + \eta_y)y + Y}{(1 + \eta_x)x + X} \approx \frac{y + Y}{x + X} \left(1 + \eta_y \frac{y}{y + Y} - \eta_x \frac{x}{x + X} \right) \propto \quad (8)$$

$$T_0 \left(1 + \eta_y \frac{y}{y + Y} - \eta_x \frac{x}{x + X} \right), \quad (9)$$

where y, x are the contributions of this gas lump to integrated SZ and X-ray signals, respectively, while the capital Y, X stay for the contributions due to remaining gas. $T_0 = (y + Y)/(x + X)$ is the temperature of unperturbed gas. For isobaric perturbations, which can give rise to cold spots, $n_y = 0$ and the change of temperature is always negative. For shocks, both n_y and n_x are positive and are almost equal, unless $M \gg 2.4$ as shown in Fig. 9. Since they enter Eq. (9) with different signs, the sign of the temperature change depends on the relation between $\frac{y}{y+Y}$ and $\frac{x}{x+X}$. In the case of the shock to the west of the core, these terms partly compensate each other and the resulting temperature does not change strongly. Similarly, some of the temperature variations seen in Fig. 10, especially at outer regions, might also be induced by the very substantial deviations of the density distribution from the spherically symmetric beta-model.

The above effects can be mitigated by adopting a more appropriate 3D model of the gas distribution, for example, a parametric model with a jump (e.g., *Planck Collaboration Int. X 2013*) or doing independent deprojection of X-ray and SZ data in wedges (e.g., *Mirakhor & Walker 2020*), assuming that within each wedge all thermodynamic properties depend only on the radius.

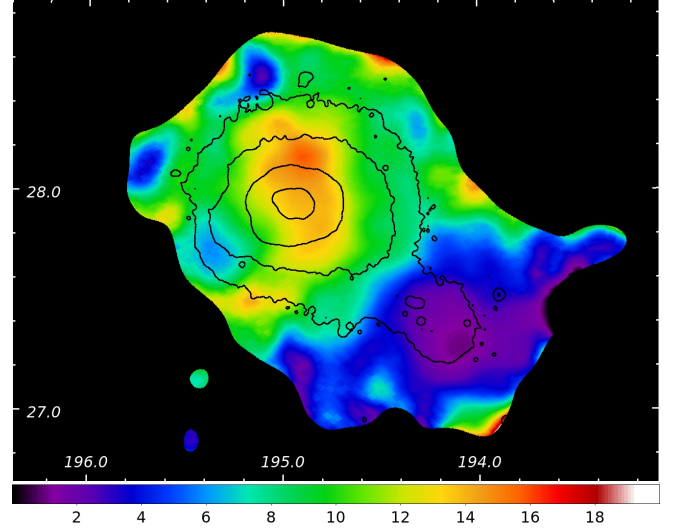


Fig. 10. Ratio of SZ and X-ray images of the Coma cluster, converted to the weighted electron temperature in keV. Contours show the X-ray surface brightness. Only the inner part of the studied region, where the signal is strong enough to evaluate the ratio of two images is shown. There are three clear features in the derived temperature distribution – a cool region at the position of the NGC 4839 group, a (marginally) hotter region to the north of the core and another cool region near the contact discontinuity to the east of the core.

For the W-shock, the comparison of the eROSITA and *Planck* data in a wedge yields consistent results (to be reported in a forthcoming publication).

5. Merger signatures

Massive galaxy clusters are dynamic systems that continuously accrete smaller structures. In the Coma cluster, the signatures of mergers have long been identified/suggested in the optical, radio or X-ray bands (see, e.g., *Brown & Rudnick 2011*; *Bonafede et al. 2021*; *Lyskova et al. 2019*; *Malavasi et al. 2020*, and references therein). Apart from the NGC 4839 group, these include the structures (shocks and contact discontinuities) discussed above. The famous radio relic has long been discussed in the association with a shock. Initially, it was suggested that the relic is located at the position of an accretion shock (*Ensslin et al. 1998*), namely, where the infalling gas decelerates and joins the Coma ICM. An alternative is a scenario, where the shock is driven “from inside,” that is by a merger with a smaller subcluster, which enters the main cluster from the opposite side and drives the shock which propagates outward and takes over the “nominal” accretion shock. Here we discuss current observations in the light of this scenario.

5.1. Broad brush merger scenario

Firstly, we outline the broad brush scenario, originally mentioned in *Burns et al. (1994)* and *Biviano et al. (1996)* and discussed in detail in *Lyskova et al. (2019)*; *Sheardown et al. (2019)*; *Zhang et al. (2019)*. In this scenario, the NGC 4839 group was initially moving from the NE along the general direction of the Coma-A1367 filament. It passed the pericenter for the first time some 1–1.5 Gyr ago, has already reached the apocenter, and is now falling back into the Coma center. This scenario was devised, in particular, to explain the apparent bent shape of

the X-ray tail of NGC 4839. An immediate consequence of this scenario is the prediction of a “runaway” shock, which had been driven by NGC 4839 during its first infall, but has separated from the group after the pericenter passage and at present continues to propagate in the general SW direction. The decreasing density of the main cluster with radius helps this shock wave in keeping its strength (in terms of the Mach number) over a large traveled distance, even though the NGC 4839 group is already moving in the opposite direction. In this scenario the radio relic marks the position of this runaway shock and fits into a generic scenario of merger shocks (e.g., Rottgering et al. 1997). The subtlety here is whether this runaway shock has already taken over the accretion shock or not (e.g., Birnboim et al. 2010; Zhang et al. 2020a). We defer this question for the subsequent publication with the eROSITA results on the outer regions of the Coma cluster.

5.2. Bridge between NGC 4839 and the main cluster

One can argue that while crossing the pericenter and reversing direction at the apocenter, the NGC 4839 could leave a long tail of stripped gas tracing its trajectory through the main cluster, as long as this trace is not distorted/dissolved by the gas motions. We speculate that in the flattened X-ray image (Fig. 6) one can see a faint and curved substructure that can be a trace of this gas (see also Fig. 11 below, where this feature is labeled as “Bridge”). Unambiguous identification of this feature as the stripped NGC 4839 gas is not robust, but a combination of accurate temperature and abundance measurements in X-rays and morphology of faint radio emission might help to do this.

5.3. Sharp western edge as a secondary shock

Apart from the NGC 4839, the next most prominent feature seen in the eROSITA X-ray images (Figs. 1, 4, and 6) is a long and sharp edge to the west of the Coma core, which spans more than 2 Mpc from north to south with its curvature changing from concave (closer to the Coma center) to convex at the farthest end in the south. The brightest part of this structure has already been recognized in the ROSAT, *XMM-Newton*, *Planck* images (e.g., Neumann et al. 2003; Simionescu et al. 2013; Planck Collaboration Int. X 2013; Mirakhor & Walker 2020) and reported to be a shock, although there was no consensus on the origin of this shock. Spectral analysis of eROSITA data (see Sect. 3.3) unambiguously identifies this structure as a shock. The brighter (closer to the Coma center) side is hotter, so this is the downstream side of the shock.

One possibility is that this is a classic accretion shock, namely the infall of the Intergalactic Medium (IGM), which is about to join the Coma cluster. There are two difficulties with this scenario. First, this shock is only 1 Mpc (i.e., $\lesssim R_{500}$), from the Coma center, what is unlikely, unless there is a dense filament in this direction. Second, the diffuse emission can be seen on the upstream side of the shock, namely farther away from the Coma, which would require preheating the upstream gas to the temperature ~ 5 keV.

Another possibility is that this feature is a merger (or a bow) shock driven by the NGC 4839 group³. The bow shock hypothesis clearly contradicts the morphology of the front. Indeed,

the bow shock would encompass the moving group and the hot (downstream) gas would be closer to the group. The observed geometry is just the opposite. The same is true for the merger shock scenario since in this case, the shock should be farther away from the Coma cluster (in the direction of the initial infall) than the group. For instance, it could be located at the position of the radio relic.

With the above scenarios having been discarded, we are left with two other possibilities: (i) there are two (or more) mergers happening now in Coma or (ii) only one important merger (with the NGC 4839 group) is responsible for the bulk of the X-ray substructure.

A plausible scenario, which predicts that two shocks (one far away from the core and another one close to the core) are produced by a single merger is discussed in Zhang et al. (2021). Namely, during the first passage through the core, the smaller subcluster drives the bow/merger shock, which displaces the gas in the main cluster core. While the merger shock continues to propagate toward cluster outskirts, this gas eventually falls back to the core and settles (eventually) to hydrostatic equilibrium. While this is largely a scenario that is often invoked to explain gas sloshing in the core, the internal waves and global oscillations of the gas are not the only outcomes of this process. In addition, a “mini accretion shock” can be formed, when the primary merger shock is already far away from the center.

Examples of such shocks are given in the numerical simulations of Zhang et al. (2021), which are specifically focused on this issue (see the right panel in Fig. 11). One can also identify similar structures in publicly available generic simulations of cluster mergers. For instance, in the library of cluster mergers by ZuHone (2011), the secondary shocks are particularly visual for the mass ratio $R \sim 1:10$, the impact parameter $b = 500$ kpc at $t \sim 3$ Gyr⁴. Yet another example, is the idealized simulation of a plane shock traversing the core of the cluster in Churazov et al. (2003; see their Sect. 4) when both sloshing motions and shocks are formed. In the double shock scenario, both shocks are the natural outcome of a single merger and no extra perturbations are needed. One has to observe the cluster at a particular moment of the merger, namely when the subcluster is close to the apocenter during its first passage.

Apart from the merger and mini-accretion shocks, the merger should generate sloshing motions, which naturally generate contact discontinuities (a.k.a. cold fronts, see Markevitch & Vikhlinin 2007, and reference therein). It is therefore not surprising that some of the sharp edges in the Coma image correspond to contact discontinuities. The most prominent one is the sharp edge to the east of the core (labeled “C.D.” in Fig. 11), for which the spectral analysis (see Sect. 3.3) shows that the brighter/dense side is cooler, as expected for a genuine contact discontinuity.

In the above discussion, we are trying to attribute most of the morphological features observed in the X-ray band, in particular, the W-shock, to the NGC4839 group. However, optical and X-ray data suggest additional ongoing mergers in the Coma cluster. One example is a chain of galaxies in the NGC4911-NGC4921 group (e.g., Vikhlinin et al. 1997; Andrade-Santos et al. 2013) and another is the presence of two D galaxies NGC4889 and NGC4874 in the core of the cluster (e.g., Biviano et al. 1996; Adami et al. 2005). The contribution of these mergers to the formation of structures visible in X-ray images, e.g., of the W-shock, cannot be excluded a priori. However, we believe that NGC4839 is still a primary driver of this shock. Indeed, the NGC 4911-NGC 4921 group is less massive (e.g., Adami et al. 2005)

³ Here we make a distinction between the bow shock which is currently driven by a moving group during its accelerated motion toward the center of the main cluster and the merger shock, which runs away from the moving group when it decelerates after passing through the pericenter (see, e.g., Zhang et al. 2019).

⁴ http://gcmc.hub.yt/fiducial/1to10_b0.5/index.html

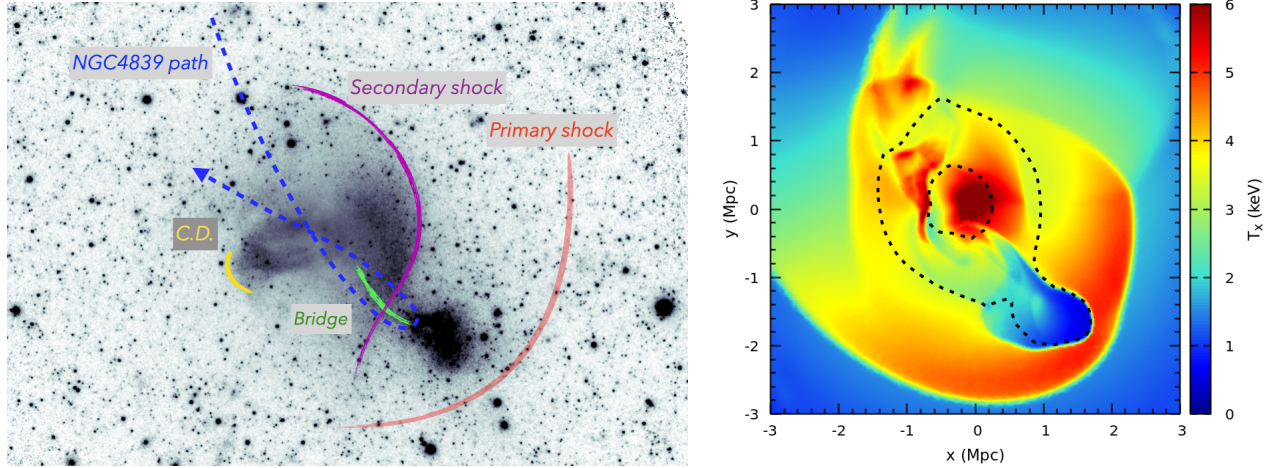


Fig. 11. Comparison of the most salient features in the X-ray images and in simulations. *Left:* flattened image of the Coma cluster field with labels schematically marking some of the features associated with the merger with the NGC4839 group. The blue dashed line is the suggested trajectory of the group (Lyskova et al. 2019; Sheardown et al. 2019; Zhang et al. 2019), which enters the Coma cluster from NE, and is currently close to the apocenter. The presumed position of the primary shock is shown with the red curve so that it goes through the radio relic SW from the NGC4839 group. The purple curve marks the secondary shock caused by settling the displaced ICM back to the hydrostatic equilibrium. This is the most salient feature directly seen in the image as the surface brightness edge. The green line shows the faint X-ray “bridge” connecting NGC4839 and the main cluster, which is a possible trace of the group through the Coma cluster. *Right:* projected temperature map from simulations (Zhang et al. 2021, see their Fig. 8 for the original version of the figure). The simulations qualitatively reproduce the morphology of the cold gas and the positions of the primary and secondary shocks. In the simulations, the inner region is a complex mixture of shocks and contact discontinuities. It is, therefore, not surprising that real observations have both types of structures.

and appears to be just approaching the central part of Coma. Given the extent of the W-shock, it appears unlikely that this group could already make such an impact on the Coma gas. On the other hand, NGC4889 and NGC4874 are located close to the geometrical center of the main cluster, have a small line-of-sight velocity difference of $\sim 720 \text{ km s}^{-1}$, and do not currently possess very massive cool gaseous atmospheres, characteristic for a group not yet stripped by the ram pressure. Such an atmosphere would act as a working surface, which drives a shock wave. Therefore, if one of the two galaxies is responsible for the W-shock (see Biviano et al. 1996; Adami et al. 2005, for the discussion of various scenarios) then it should have had the atmosphere less than $\sim 400 \text{ Myr}$ ago (an upper limit based on the distance to the W shock from the center ($\sim 33' \sim 930 \text{ kpc}$ and the current Mach number of the shock). The group also had to move fast at that time in order to drive the shock. This scenario would then require fine-tuning of the merger geometry and/or a very efficient dynamic friction to explain the current positions and velocities of NGC4889 and NGC4874. At the same time, we do not see any fundamental problems with a scenario when the cool/dense atmosphere(s) was lost a few gigayears ago and two galaxies are now spiraling into the core. Given these arguments, it seems that the scenario involving NGC4839 is more natural.

5.4. Coma radio halo

The Coma radio halo has been intensively studied over several decades (see, e.g., Brown & Rudnick 2011; Bonafede et al. 2021, and references therein). If the merger scenario and our identification of various features in the X-ray map are correct, this might have interesting implications for the formation of the radio halo in the Coma core on the downstream side of the western shock. Since in this scenario the western shock is the “secondary shock” (or “mini-accretion shock”), the gas upstream of the shock has already passed through the primary shock soon after the NGC4839 group passage through the core about a Gyr

ago. We assume that the primary shock was strong enough to accelerate (or reaccelerate) particles that can potentially emit synchrotron radiation (see, e.g., Bykov et al. 2019, for a review). The question arises of whether these particles survive for a gigayear and eventually been compressed (and re-accelerated) by the secondary shock. For a power law distribution of isotropic relativistic electrons in a randomly oriented magnetic field, the Lorentz factor γ_{max} that provide the largest contribution to the flux emitted at frequency ν is

$$\gamma_{\text{max}} = \zeta_{\text{max}} \gamma_c, \quad (10)$$

where γ_c is set by the condition

$$\nu = \nu_c \equiv \frac{3}{4\pi} \frac{eB}{m_e c} \gamma_c^2. \quad (11)$$

Here, B , e , m_e and c are magnetic field, electron charge, electron mass and the speed of light, respectively. ζ_{max} is the function of the electron spectrum slope, which is linked to the observed spectral index of synchrotron emission α . For $\alpha \sim 2$, $\zeta_{\text{max}} \sim 0.57$ (see Appendix E). Moreover, the turbulent character of the cluster magnetic field may further reduce the value of ζ_{max} .

The life time of a relativistic electron with the Lorentz factor γ_{max} against synchrotron and Inverse Compton losses is

$$t_{\text{cool}} = -\frac{\gamma}{\dot{\gamma}} = \frac{1}{\zeta_{\text{max}}} \left(\frac{\nu}{\frac{3}{4\pi} \frac{eB}{m_e c}} \right)^{-1/2} \left(\frac{4}{3} \frac{\sigma_T}{m_e c} \right)^{-1} \times \left(\frac{B^2}{8\pi} + U_{\text{CMB}} \right)^{-1}, \quad (12)$$

where σ_T is the Thomson cross section, and U_{CMB} is radiation field energy density (dominated by the Cosmic Microwave Background, CMB). At redshift $z \approx 0$, U_{CMB} is equivalent to the

magnetic field energy density $\frac{B^2}{8\pi}$ for $B \approx 3.25 \mu\text{G}$. The cooling time t_{cool} reaches the maximum for $B \sim 2 \mu\text{G}$. Conveniently, Faraday Rotation measurements suggest $B \sim 1\text{--}2 \mu\text{G}$ at the distance of ~ 700 kpc from the Coma center (Bonafede et al. 2010). Therefore, the life time of electrons is not far from its maximum value (plugging $B = 2 \mu\text{G}$ in the above expression)

$$t_{\text{max}} = 1.3 \cdot 10^8 \frac{1}{\zeta_{\text{max}}} \left(\frac{\nu}{1.4 \text{ GHz}} \right)^{-1/2} \approx 1.7 \cdot 10^8 \left(\frac{\nu}{1.4 \text{ GHz}} \right)^{-1/2} \text{ yr.} \quad (13)$$

For 150 and 350 MHz, the cooling time is 5.3×10^8 and 3.5×10^8 yr, respectively. While long enough, these timescales are still shorter than $\sim \text{Gyr}$ elapsed since the passage of the primary shock through the gas, which is now close to the secondary shock. However, downstream of a spherical merger shock (the primary shock), the compressed region is followed by a rarefaction, where the density falls below the initial density of a given gas parcel (see Fig. 5 in Zhang et al. 2019). This rarefaction is caused by the expansion of the gas that is pushed by the shock to larger radii. This means that for a significant fraction of time between the passages through the primary and the secondary shocks, the electrons have lower Lorentz factors than just behind the primary shock, and the magnetic field is also lower. The radiative losses are therefore relatively small (except for the period right after the passage of the primary shock). The electrons then spend a long time in a “freezer,” until the gas passes through the secondary shock (mini-accretion shock), when its density increases back to the initial state (at least approximately). The electrons’ Lorentz factor and the strength of the magnetic field increase accordingly. As a result, the synchrotron emissivity is boosted by a factor $F = C^{\frac{2}{3}p+1}$ (e.g., Markevitch et al. 2005), where p is the slope of the relativistic electrons energy spectrum and C is the volume compression factor. In terms of the spectral index $\alpha = (p - 1)/2$ in the radio band, the boost factor is $C^{\frac{4\alpha}{3} + \frac{5}{3}}$. This expression is based on the assumption that the magnetic field is enhanced by a factor $C^{2/3}$. For the shock with $M \sim 1.5$, the compression is $C \approx 1.7$. For $\alpha = 2$, the corresponding boost of the radio flux purely due to adiabatic compression is $F \approx 10$. Unlike the “runway” merger shock, the mini-accretion shock does not feature a rarefaction region downstream and, therefore, the radio emission is controlled by radiative losses. Once again the question arises of whether the short radiative times pose a problem. The distance over which the secondary shock front can travel during t_{max} is $l_{\text{max}} \sim c_s t_{\text{max}} \lesssim 180$ kpc (for $\nu = 1.4$ GHz), assuming that the shock moves with the sound speed⁵. At $\nu = 150$ MHz, this distance will be ~ 500 kpc. This is smaller than the size (radius) of the radio halo of some 700 kpc (not by a huge factor, though), which used to be an argument against the single shock acceleration scenario. However, in the scenario, where secondary shocks are responsible for the compression and, possibly, reacceleration of electrons, this problem can be alleviated. The electron reacceleration scenario implies that there is a pool of nonthermal relativistic electrons produced by MHD shocks and turbulence due to the cluster merging history and fast moving galaxies in the cluster. Then the diffusive shock acceleration (DSA) mechanism would reproduce the slope of the pool electron spectrum in a shock downstream if the pool

distribution had a power-law spectrum of index $p < \frac{C+2}{C-1}$. Otherwise, the spectrum in the shock downstream would have the standard test particle DSA index $p = \frac{C+2}{C-1}$ if the slope of the pool distribution has a steeper spectrum (see e.g., Blandford et al. 1987). Therefore, the shock with $M \sim 1.5$, and the compression ratio $C \approx 1.7$ propagating in the cluster plasma regions without the prominent preexisting nonthermal population have $p = 5.2$ and the synchrotron radio emission index $\alpha = 2.1$. On the other hand, energetic particle acceleration by intensive MHD turbulence and multiple shocks may produce a long-lived pool of relativistic particles (see e.g., Schlickeiser et al. 1987; Bykov et al. 2000; Brunetti et al. 2001; Petrosian & Bykov 2008; Brunetti & Lazarian 2011; van Weeren et al. 2019). Namely, a time-dependent nonlinear model of electron acceleration by the shock ensemble with long-wavelength MHD turbulence predicts the time asymptotic particle spectra with power-law indexes $p \geq 3$ providing synchrotron radio emission of indexes $\alpha \sim 1$ (see Fig. 7 in Bykov et al. 2019) which is consistent with that is observed in the extended regions of the cluster core (see Brown & Rudnick 2011, and references therein).

Although the multiple shocks operate in different parts of the cluster core, they are, however, synchronized by the initial merger shock. To some extent, these “coordinated” shocks could provide a similar effect as the reacceleration by the turbulence in the core, which was invoked as an alternative mechanism to keep the radio halo alive (see, e.g., Brunetti et al. 2001; Bonafede et al. 2021). Given the long-living perturbed state of the core predicted by simulations, a combination of both scenarios could be at work in the Coma core. We also note that the sloshing of the gas in the core, when big lumps of gas temporarily move away from the core and expand, essentially quenching the radio emission, could be another reason for the appearance of a sharp boundary of the halo, like observed to the east of the Coma center.

One can think of various observational tests that can support or falsify the above scenario (or at least parts of it). First of all, the spatial coincidence of the radio halo edge and the shock clearly shows that the compression (or compression + acceleration or reacceleration) is happening right at the position of the W shock. As discussed above, a weak shock would not alter the slope of the particles’ distribution, unless the distribution is very steep. Therefore, if sensitive low-frequency observations (e.g., LOFAR, GMRT) could detect diffuse radio emission outside the W shock and compare slopes inside and outside the shock, the role of the preexisting population and the revival scenario can be clarified. The same slope and correct intensity ratio would support a pure compression scenario. Further inside the radio halo, the “volumetric” acceleration mechanisms and spectral aging might be important and their roles could be revealed by measuring the radial gradients of the spectral indices at low and high frequencies. In the absence of volumetric acceleration, the spectral aging (at high frequencies) should become more prominent toward the center, while the lowest-frequency part might show an opposite trend, which reflects the high Mach number of the shock that went through the fluid element close to the center. Furthermore, in the outgoing shock scenario (see also the discussion in the previous subsection), the expansion downstream of the shock could contribute to steepening of the high-frequency end of the spectrum.

If the above scenario is correct, a typical post-merger configuration might include two radio-bright structures. The outer one (radio relic), located close to the position of the primary shock – is formed due to particle acceleration and/or compression at the shock, followed by adiabatic expansion and radiative losses

⁵ We note in passing that the velocity of a mini-accretion shock relative to the Coma center can be slightly lower than the sound speed.

at high frequencies (see, e.g., Fig. 7 in Zhang et al. 2019). The inner one, inside the mini-accretion shock, is a more diffuse and extended radio halo. These two radio-bright regions should be separated by a radio faint “ring,” which corresponds to a rarefaction region between the mini-accretion shock and the primary shock.

The broad-brush single-shock scenario (see, e.g., Markevitch 2010) tailored to the Coma case implies that the western edge of the halo is a merger shock with a moderate Mach number that reaccelerates electrons, while the bulk of the halo radio emission is due to turbulent reaccelerations. The scenario outlined above keeps these elements but adds two interesting ingredients. Firstly, it postulates that a genuine primary shock (with a higher Mach number) must be present ahead of the western (mini-accretion) shock. This alleviates the “preparation” of electrons for the western shock compression and, possibly, reacceleration. Secondly, in this scenario, the mini accretion shock has a complicated 3D shape (Zhang et al. 2021) and might envelope the entire cluster core (at least in projection), rather than boosting radio emission only over one side of the cluster, as the primary shock does. Moreover, the complex MHD flows associated with the secondary shocks would energize turbulence over the cluster volume similarly to the single-shock scenario. Indeed, turbulent re-acceleration has been considered in connection with the low polarization of the halo, the overall halo spectrum, and the volumetric correlation of X-ray-radio brightness (see, e.g., Govoni et al. 2001; Brunetti et al. 2013; Brown & Rudnick 2011). Detailed simulations of the double-shock scenario (to be reported elsewhere) might help to clarify the roles of the two shocks and the turbulence in explaining these radio halo properties.

6. Conclusions

Observations of the Coma cluster with SRG/eROSITA revealed a rich substructure in the X-ray surface brightness distribution, extending to the cluster virial radius. Analyzing this substructure we came to the following conclusions:

- The overall morphology is consistent with the post-merger scenario described in Lyskova et al. (2019); Sheardown et al. (2019); Zhang et al. (2019), in which the NGC 4839 group has passed through the Coma cluster from the NE direction, reached the apocenter, and is now starting its second infall toward the main cluster;
- A faint X-ray bridge connecting the NGC 4839 with the main cluster provides convincing proof that the group has already crossed the Coma core;
- X-ray spectral analysis robustly classifies some of the most prominent structures as shocks or contact discontinuities. In particular, the steepest gradient in the X-ray surface brightness $\sim 30\text{--}40'$ to the west of the core appears to be a shock, while the steepest gradient to the east is a contact discontinuity;
- In the post-merger scenario, the most prominent “edge” to the west of the core is interpreted as a “mini-accretion” (or “secondary”) shock (see the simulation in Zhang et al. 2021), associated with the infall of the gas displaced by the merger with the NGC 4839 group on its first passage, and settling of this gas back into hydrostatic equilibrium. This scenario envisages that the primary merger shock is currently located at the position of the radio relic;
- The presence of two shocks leads to the following scenario of the radio halo formation in the Coma cluster. The gas

encompassed by the secondary shock has already passed through two shocks, both the primary and the secondary. The primary shock, which presumably is the main source of particle acceleration, is followed by a rarefaction that lowers particles’ Lorentz factors and extends their radiative lifetime. These particles begin radiating again only after crossing the secondary shock, which lacks the rarefaction. While the radiative lifetime of electrons emitting at hundreds of MHz–1 GHz is not very long, compared to, say, sound crossing time of the halo, the “synchronization” of secondary shocks in the core by the initial merger leads to the appearance of the extended and steep spectrum halo;

- The comparison of the X-ray and SZ (*Planck*) images leads to a 2D gas-density-weighted temperature map, which reveals a number of hot and cold spots, although the detailed structure might be affected by the different angular resolution in the X-ray and microwave bands and imperfection of the cluster 3D model. We have shown that pure entropy perturbations (the pressure is not affected) are expected to be robustly revealed by such maps. For shocks with low Mach numbers ($M \lesssim 3$), the “weighted” temperature depends on the relative contributions of SZ and X-ray signals from the perturbed region to the total signals along a given line of sight.

This study is intentionally restricted to features that are the most robust against remaining calibration uncertainties, in particular, the ones associated with the single-scattering stray light and careful calibration of the telescope effective area. The former is especially important for the outskirts of the cluster, namely R_{200} and the outer baryonic boundary of the Coma cluster. The latter is crucial for accurate temperature determination. A more detailed analysis will be reported in subsequent publications.

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Appendix A: Provisional background model

To correct for the instrument intrinsic background, Galactic foreground and astrophysical background in the Coma field, we have used a “provisional” background model. We model the total background spectrum per unit solid angle B_t as

$$B_t = B_i + B_G + B_{\text{CXB}}, \quad (\text{A.1})$$

where B_i , B_G , B_{CXB} are the intrinsic detector background, Galactic foreground (mostly diffuse emission), astrophysical background (mostly AGN), respectively. In the survey or scan mode, the vignetting can be assumed constant over the studied region, which simplifies the treatment of the background. The advantage of the SRG observatory being at L2 point is the notable stability of the background. It implies that the background measured during one observation can be used for the analysis of another observation several months earlier or later (at long as background variations at the per cent level are not crucial for the problem at hand). Thus if only the total background rate matters, one can use any other field with similar Galactic hydrogen column density. However, in the Coma field, the sensitivity to compact sources, which have to be excised before evaluating the X-ray surface brightness, varies across the field. For that reason the remaining background has to be adjusted for the resolved fraction. To this end, we estimated the resolved part of the background by integrating the Log N-Log S curve taken from [Luo et al. \(2017\)](#). We have verified using several fields observed with eROSITA that we are getting consistent Log N-Log S and the conversion factors to our working energy bands is reasonable. With this approach, the evaluation of the background in a given energy band (and for a given flux level s_{min} of resolved and excised sources) reduces to:

$$B = B_t - \int_{s_{\text{min}}}^{\infty} \frac{dN}{ds} ds, \quad (\text{A.2})$$

where $\frac{dN}{ds}$ is derived from Chandra’s 0.5–2 keV Log N-Log S. The images used in this work were made in the 0.4–2 keV band. In this band, $B_t \sim 4.24 \cdot 10^{-4}$ counts $\text{s}^{-1} \text{ arcmin}^{-2}$ per one (out of 7) eROSITA telescopes, B_i makes about a quarter of it.

Appendix B: The model of the effective point spread function

In-flight calibration of the SRG/eROSITA’s effective PSF is ongoing. In particular, we performed a stacking of the properly aligned images of known point sources observed during the course of the all-sky survey. The selection of sources is based on their extragalactic position and X-ray brightness, which should not be too large to avoid the pile-up in the core and sufficiently high to maximize signal-to-background ratio in the PSF wings. These conditions are satisfied for instance by a sample of X-ray bright point sources from the *XMM-Newton* Slew Survey (Full Source Catalog, v2.0, [Saxton et al. 2008](#)) with the 0.2–2 keV flux from 3×10^{-12} to 10^{-11} erg $\text{s}^{-1} \text{ cm}^{-2}$.

The PSF computed in this way naturally includes averaging over the telescope’s field-of-view thanks to the multitude of the source offset angles sampled by the scan patterns. Via stacking, we produce images with 4 arcsec pixel size, which corresponds to the image binning used throughout the paper. In principle, somewhat better characterization of the PSF core might be achieved with finer binning of the data, thanks to the

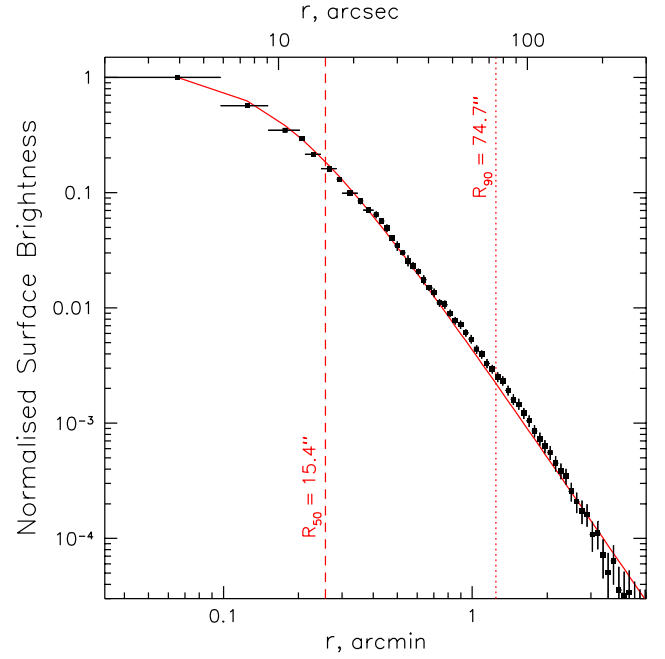


Fig. B.1. Model of the effective PSF (red curve) used throughout the paper and derived from the stacked images of bright sources (black points) in 0.4–0.2 keV energy band. The radii corresponding to 50% and 90% of the encompassed photons are marked as R_{50} and R_{90} .

sub-pixel algorithm employed in the initial reduction of the raw data ([Predehl et al. 2021](#)).

For the 0.4–2 keV band, the analysis of the stacked images allowed us to derive a simple approximating model for the effective PSF, namely the beta-model with $\beta \approx 0.7$ and $r_c \approx 10$ arcsec, which is valid up to radial distances of a ≈ 4 arcmin, namely within the PSF core (see Fig. B.1). At large radii, the contribution of the single reflections becomes increasingly noticeable. The derived shape of the core PSF slightly differs from the on-ground calibration measurements, although resulting in a very similar Half Power Diameter size, $\text{HPD} = 2R_{50} \approx 30$ arcsec. The aperture encompassing 90% of the photons has the radius of $R_{90} \approx 75$ arcsec. Throughout the paper, this model is used for the optimal detection and subtraction of the point sources and characterization of the extended emission.

Appendix C: Effective counts production rate for the ICM

The quantity ϵ_c in its simplest form is a convolution of the energy resolved thermal plasma emissivity $\Lambda(E, T)$ with the effective area of the instrument $A(E)$. Namely,

$$\epsilon_c = \frac{1}{1+z} \int_{E_1}^{E_2} \frac{\Lambda(E(1+z), T)}{E} A(E) dE, \quad (\text{C.1})$$

where E_1 and E_2 are the boundaries of the energy band. In practice, one has to take into account an energy redistribution matrix (as is done in Fig. C.1). It is well known that for hot ICM, ϵ_c in the soft band only weakly depends on temperature. This is also true for the 0.4–2 keV band of the eROSITA telescope, as shown in Fig. C.1. The effective area averaged over the eROSITA FoV was used for this plot. For the temperature range of interest, ϵ_c varies between $40\text{--}55 \times 10^{-14}$ counts $\text{s}^{-1} \text{ cm}^{-2}$.

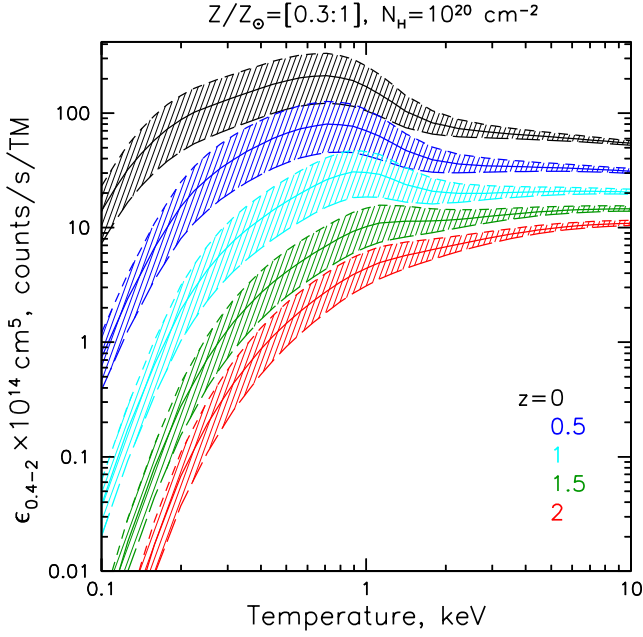


Fig. C.1. Effective ICM emissivity ϵ_c in terms of the 0.4–2 keV count rate per SRG/eROSITA telescope module (with the FOV-averaged effective area) as a function of the ICM temperature. The assumed spectral shape is given by the APEC model at redshifts $z = 0$ (black), 0.5 (blue), 1 (cyan), 1.5 (green), 2 (red) with the metals abundance varying from $Z/Z_\odot = 0.3$ (long-dashed) to $Z/Z_\odot = 0.6$ (solid) to $Z/Z_\odot = 1$ (short-dashed) with respect to the Solar metallicity $Z_\odot$. The applied foreground absorption column density equals to $N_H = 10^{20} \text{ cm}^{-2}$.

Appendix D: Comparison of the ROSAT and eROSITA radial X-ray surface brightness profiles

The measured Coma's X-ray surface brightness in the 0.4–2 keV band varies by more than four orders of magnitude over the radial range studied here, and beyond $\sim 30'$ it is smaller than the total background level. To demonstrate that the background subtraction and the account for the contribution of the singly-scattered photons are both corrected for reasonably well, we have compared the shapes of the radial profiles obtained by SRG/eROSITA and ROSAT in their respective all-sky surveys. For ROSAT all-sky survey (e.g., [Voges et al. 1999](#)), the data in the 0.4–2.4 keV band were used. For comparison with the eROSITA profile, the ROSAT data were renormalized to match at $\sim 10'$. The corresponding profiles are shown in Fig. D.1. The agreement is good over the entire range of radii and is fully sufficient for the goals of the present study.

Appendix E: Lorentz factors of electrons providing the largest contribution to the synchrotron emission at a given frequency

For isotropic electrons with a given Lorentz factor γ in a randomly oriented but uniform magnetic field, a useful approximation of the emergent spectrum frequency dependence is given by [Aharonian et al. \(2010\)](#), via the function $G(x)$, where $x = \nu/\nu_c$ and $\nu_c = \frac{3}{4\pi} \frac{eB}{m_e c} \gamma^2$. For a power law distribution of electrons $dN/d\gamma \propto \gamma^{-p}$, the maximum contribution to the flux near frequency ν is provided by electrons with the Lorentz factor $\sim \gamma_{\text{max}}$ such, that $F(\gamma) = \gamma^{-p} G(1/\gamma^2) \gamma$ is maximal. It is convenient to

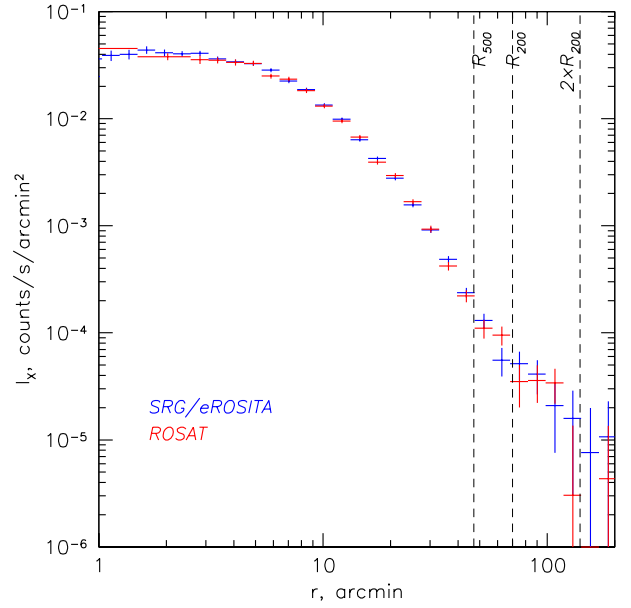


Fig. D.1. Comparison of the ROSAT and eROSITA radial profiles of the Coma cluster. In both cases, the data from the all-sky surveys are shown. For ROSAT (red points), the data in the 0.4–2.4 keV were used. As in Fig. 5, the 90 degrees wedge to the SW (containing NGC4839 group) has been excluded. The eROSITA points (blue crosses) are the same as in Fig. 5. The ROSAT profile has been renormalized to match the eROSITA data. The shapes of the two profiles agree well.

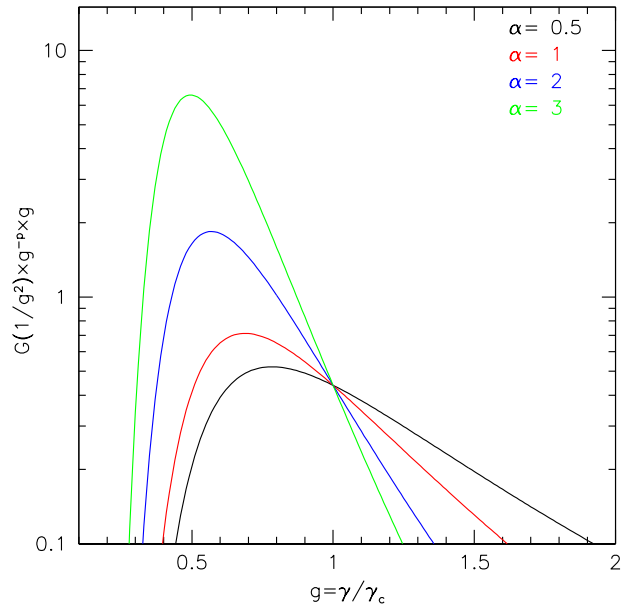


Fig. E.1. Lorentz factor γ of electrons providing the most important contribution to the synchrotron emission at a given frequency for a power spectrum of electrons and random orientation of the magnetic field. Here, γ_c is set by the condition $\nu = \frac{3}{4\pi} \frac{eB}{m_e c} \gamma_c^2$.

use the spectral index α of the observed synchrotron spectrum instead of p , where $\alpha = (p - 3)/2$ ([Longair 2011](#)). Figure E.1 shows the function $F(\gamma)$ for several values of the spectral index. For our case of interest ($\alpha \sim 2$), the function reaches the maximum at $\gamma/\gamma_c \approx 0.57$ (see also [Cummings 1973](#), page 164). This value $\zeta_{\text{max}} = \gamma/\gamma_c$ is used in this study to estimate the life time electrons emitting at a given frequency.