

Constraints for the accretion disk evaporation rate in AGN from the existence of the Broad Line Region[★]

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Received 21 March 2004 / Accepted 2 July 2004

Abstract. We analyze the consequences of the hypothesis that the formation of the Broad Line Region is intrinsically connected to the existence of the cold accretion disk. We assume that the Broad Line Region radius is reliably estimated by the formula of Kaspi et al. (2000, ApJ, 533, 631). We consider three models of the disappearance of the inner disk that limit the existence of the Broad Line Region: (i) the classical ADAF approach, i.e. the inner hot flow develops whenever it can exist; (ii) the disk evaporation model of Meyer & Meyer-Hofmeister (2002, A&A, 392, L5); (iii) the generalized disk evaporation model of Róžańska & Czerny (2000b, A&A, 360, 1170). For each of the models, we determine the minimum value of the Eddington ratio and the maximum value of the broad line widths as functions of the viscosity parameter α and the magnetic field parameter β . We compare the predicted parameter space with observations of several AGN. Weak dependence of the maximum value of the *FWHM* and minimum value of the Eddington ratio on the black hole mass in our sample is noticeable. It seems to favor the description of the cold disk/hot inner flow transition as in the classical ADAF approach rather than with the model of disk evaporation due to conduction between the disk and accreting corona.

Key words. accretion, accretion disks – galaxies: active – galaxies: Seyfert – X-rays: galaxies – quasars: emission lines

1. Introduction

One of the most important issues in studying accretion onto compact objects is to understand the process that causes some fraction of the accreting material to be heated sufficiently strongly to form a hot optically thin, predominantly thermal plasma in the vicinity of a black hole (see e.g. Narayan et al. 1998; Collin et al. 2001; Czerny 2003).

Observations of the X-ray emission from this plasma do not uniquely constrain the geometry of the plasma. Several phenomenological models are under consideration; those include magnetic flares above an accretion disk extending always down to the marginally stable orbit (Galeev et al. 1979; Haardt et al. 1994), or the solutions of accretion disk structure with inner optically thin (possible advection-dominated) flow (Ichimaru 1977; Narayan & Yi 1994; Abramowicz et al. 1995). The geometry possibly depends on the luminosity to the Eddington luminosity ratio in a given object. Detailed XMM-Newton and Chandra studies of the X-ray reflection (both continuum and iron K_{α} line) suggest that at high Eddington ratios the disk extends to the marginally stable orbit and its surface appears strongly ionized (e.g. Róžańska et al. 2004 for Ton S180; Janiuk et al. 2001 and Pounds et al. 2003 for PG 1211+143;

Sako et al. 2003 for MCG -6-30-15 and Markarian 766) while in low Eddington ratio sources the spectra are well-described as being due to cold reflection from the outer part of the accretion disk (e.g. O'Brien et al. 2003).

Those observations motivate the development of models in which the material slowly evaporates from the cold disk into a hot corona as the black hole is approached (Liu et al. 1999, 2002; Róžańska & Czerny 2000b; Meyer & Meyer-Hofmeister 2002; Meyer-Hofmeister & Meyer 2003). All such models predict that at high Eddington ratios the evaporation effect is relatively inefficient so the cold optically thick disk survives all the way down to the black hole while for low Eddington ratio sources the evaporation leads to a complete evacuation of the disk and formation of an inner optically thin, hot flow.

However, the physical description of the evaporation rate involves a number of complicated processes, and various models rely on several underlying assumptions so it is very important to verify the models against observational constraints. In this paper we use the constraint based on the measured width of the broad emission lines. The exact nature of the broad line region (BLR) is not known but most models connect the formation of low ionization lines like H_{β} with the wind developing close to the disk surface (Collin-Souffrin et al. 1988; Dultzin-Hacyan et al. 2000; Laor 2003a). If such an approach is adopted, the existence of the broad lines at a certain range of

[★] Table 1 and Appendix A are only available in electronic form at <http://www.edpsciences.org>

radii is possible only if the cold disk extends also at least to the same radial range, and regions of the efficient line/wind formation are related to specific phenomena taking place within the disk. For example, such an approach led Elvis (2000) to propose a general, consistent scheme for quasar structure.

The details of the processes, including disk/BLR coupling, are by no means clear but the large amount of the existing data opens possibilities to test various hypotheses of the nature of this relation. Laor (2003b) noticed that there appears to be an upper limit to the broad line width of about $25\,000\text{ km s}^{-1}$ which apparently sets a lower limit for the luminosity of the broad line object. He postulated that a significant population of AGN exists that intrinsically do not have broad lines. Further developing this idea, Nicastro et al. (2003) found the division between the AGN with and without broad lines occurs at the Eddington ratio of ~ 0.001 , and interpreted this result as an argument for a connection between the onset of a wind from the disk surface and the transition from a gas dominated to a radiation pressure dominated part of the cold disk.

In this paper we assume that the outer cold disk turns into an inner hot, optically thin and radiatively inefficient flow. We further assume that the BLR may form above a cold disk, in its atmosphere or outflowing wind, but not above a hot inner flow. These assumptions allow us to qualitatively test the theoretical predictions for the location of such a transition. We consider three specific models: the classical condition for the existence of ADAF (Abramowicz et al. 1995), the evaporation model of Meyer & Meyer-Hofmeister (2002) and the evaporation model of Róžańska & Czerny (2000) generalized for the case of a non-negligible magnetic field.

2. Method

2.1. Size of the BLR

The size of the broad line region depends predominantly on the luminosity of the active nucleus. The most accurate results are based on the reverberation method. Delays of the H_β response with respect to the changes of the continuum lead to the relation (Kaspi et al. 2000)

$$R_{\text{BLR}} = 32.9 \left(\frac{\lambda L_\lambda(5100 \text{ \AA})}{10^{44}} \right)^{0.7} \text{ It days}, \quad (1)$$

with a relatively high correlation coefficient in the luminosity range covering over three decades (with most sources between 10^{42} and $10^{45} \text{ erg s}^{-1}$).

The value of the monochromatic luminosity at 5100 \AA is surprisingly closely related to the bolometric luminosity of an AGN

$$L_{\text{bol}} = 9 \lambda L_\lambda(5100 \text{ \AA}). \quad (2)$$

(e.g. Kaspi et al. 2000; Collin et al. 2002).

The bolometric luminosity can be measured in dimensionless Eddington units, where

$$L_{\text{Edd}} = \frac{4\pi G M m_p c}{\sigma_T}. \quad (3)$$

We express the mass in units of $10^8 M_\odot$ (i.e. $M_8 = M/10^8 M_\odot$). Finally, we give the BLR radius in the units of Schwarzschild radius, $R_{\text{Schw}} = 2GM/c^2$, since theoretical estimates usually refer to such a quantity:

$$R_{\text{BLR}} = 1.8 \times 10^4 \left(\frac{L_{\text{bol}}}{L_{\text{Edd}}} \right)^{0.7} M_8^{-0.3} R_{\text{Schw}}. \quad (4)$$

2.2. Line width

The determination of the black hole mass by Kaspi et al. (2000) was based on the assumption that the motion of the BLR clouds is predominantly Keplerian. This approach was supported by a separate analysis of the several emission lines in NGC 5548 by Peterson & Wandel (1999). To determine the *FWHM* from the Keplerian velocity the correction factor $2/\sqrt{3}$ is needed, which accounts for velocities in three dimensions and for the full width being two times higher than the velocity dispersion, i.e.:

$$FWHM = \frac{2}{\sqrt{3}} \sqrt{\frac{GM}{R_{\text{BLR}}}}. \quad (5)$$

Here, we reverse the approach of Kaspi et al. (2000), and we express the width of the H_β line as a function of the black hole mass and its luminosity

$$FWHM = 1824 M_8^{0.15} \left(\frac{L_{\text{bol}}}{L_{\text{Edd}}} \right)^{-0.35} [\text{km s}^{-1}]. \quad (6)$$

2.3. Evaporation radius

The location of the transition from the optically thick disk embedded in a hot corona into a single phase inner ADAF depends on the assumptions underlying the evaporation process. The transition radius, in Schwarzschild units, depends on the dimensionless accretion rate defined as

$$\dot{m} = \frac{\dot{M}}{\dot{M}_{\text{Edd}}}; \quad \dot{M}_{\text{Edd}} = \frac{4\pi G M m_p}{\sigma_T c \eta_0}, \quad (7)$$

where $\eta_0 = 1/12$ is the efficiency of disk accretion in the Newtonian approximation.

In classical papers about the advection dominated flows (ADAFs), where the process of disk evaporation was not considered, the estimate of the truncation radius was simply based on the absence of a strong ADAF solution above this radius (Abramowicz et al. 1995; Honma 1996; Kato & Nakamura 1998):

$$R_{\text{evap}}^A = 2.0 \dot{m}^{-2} \alpha_{0.1}^4 R_{\text{Schw}}. \quad (8)$$

The unique relation between truncation radius and mass accretion rate can be determined when evaporation of the cold disc is taken into account. In the model of a single-temperature accreting corona with the evaporation efficiency determined by the conduction between the cold disk and a hot corona described as is customarily done for the solar corona, this transition takes place at the evaporation radius:

$$R_{\text{evap}}^* = 18.3 \dot{m}^{-0.85} R_{\text{Schw}} \quad (9)$$

(Liu et al. 1999). This relation is derived for a single value of the viscosity parameter $\alpha = 0.3$.

The same model, but generalized for the presence of magnetic field within the accreting corona can be roughly parameterized as

$$R_{\text{evap}}^B = 18.3 \dot{m}^{-0.85} \beta^{2.5} R_{\text{Schw}}, \quad (10)$$

which is based on the numerical results presented by Meyer & Meyer-Hofmeister (2002). Here β is the ratio of the gas pressure to the total (gas + magnetic) pressure in the corona. Therefore, the ratio of gas to the magnetic pressure used in Meyer & Meyer-Hofmeister (2002) is $P_g/P_m = \beta/(1-\beta)$.

In the two-temperature model of accreting corona with the evaporation efficiency calculated under a constant pressure assumption with conduction self-consistently determined from radiative processes (Róžańska & Czerny 2000a), this transition is predicted to be at

$$R_{\text{evap}}^{**} = 19.5 \dot{m}^{-0.53} \alpha_{0.1}^{0.8} R_{\text{Schw}}. \quad (11)$$

This relation shows a different dependence on the viscosity parameter than that predicted in Róžańska & Czerny (2000b), due to an error in the original paper.

We also generalize this model for the case of the contribution of the magnetic pressure to the total pressure (see Appendix A). We repeat the analysis of Róžańska & Czerny (2000b). Numerical results for the case of low accretion rate (i.e. negligible condensation) can be approximated analytically as

$$\dot{m}_z = \dot{m}_z^0 \beta \quad (12)$$

and consequently the evaporation radius changes to

$$R_{\text{evap}}^C = 19.5 \dot{m}^{-0.53} \alpha_{0.1}^{0.8} \beta^{-1.08} R_{\text{Schw}}. \quad (13)$$

2.4. Accretion efficiency

The bolometric luminosity is in turn related to the accretion rate through the accretion efficiency

$$L_{\text{bol}} = \eta \dot{M} c^2. \quad (14)$$

In Eq. (7) we used the efficiency η_0 which is appropriate for the description of outer parts of the flow well represented by a classical disk accretion. However, the actual efficiency of the conversion of the mass accretion into observed luminosity in the innermost part of the flow may be much lower due to advection. Therefore, we consider the efficiency η in a general form

$$\eta = \eta_0 \mathcal{F}, \quad (15)$$

and we later specify \mathcal{F} as a function of model parameters. In such a general case the bolometric luminosity depends on the dimensionless accretion rate as:

$$\frac{L_{\text{bol}}}{L_{\text{Edd}}} = \dot{m} \mathcal{F}. \quad (16)$$

The existence of the evaporation radius affects the efficiency of the accretion. Without an inner advection-dominated flow the

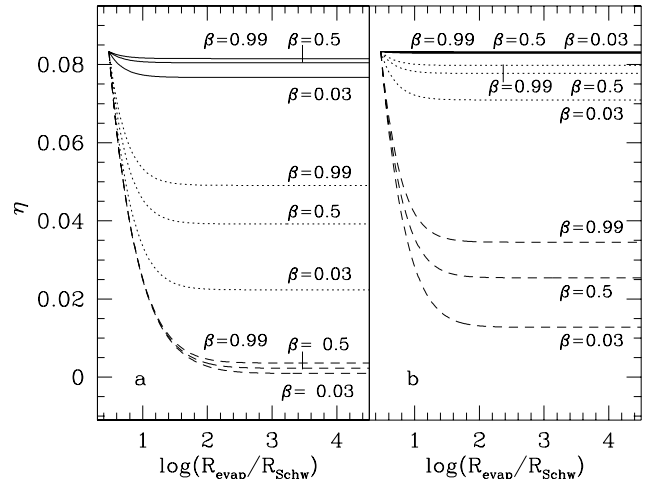


Fig. 1. The dependence of accretion efficiency on evaporation radius according to Eq. (18) for two different viscosity parameters $\alpha = 0.1$ (panel **a**), and $\alpha = 0.04$ (panel **b**). Solid lines represent the case of $\dot{m} = 0.3$, dotted lines – $\dot{m} = 0.03$, and the dashed lines – $\dot{m} = 0.003$.

correction factor to the efficiency \mathcal{F} in Eqs. (4) and (6) is equal to 1, and the evaporation radius is equal to 3, in Schwarzschild units, for a non-rotating black hole. This efficiency drops with an increasing R_{evap} since the number of soft photons penetrating the hot region decreases with an increase of its radial optical depth. For large values of R_{evap} this efficiency finally saturates since there, the locally emitted synchrotron and bremsstrahlung photons are the only source of soft photons for Comptonization. According to the Monte Carlo computations of Kurpiewski & Jaroszyński (2000) this saturation value is on the order of ε , where:

$$\varepsilon = 170.99 \left(\frac{\dot{m}}{\alpha_{0.1}^2} \right)^{1.5} (1.25\beta + 0.375). \quad (17)$$

In order to approximate this complex behaviour we use a simple formula for the correction factor mentioned above, having in mind that $r_{\text{evap}} = R_{\text{evap}}/R_{\text{Schw}}$

$$\mathcal{F} = \frac{3}{r_{\text{evap}}} + \left(1 - \frac{3}{r_{\text{evap}}} \right) \frac{\varepsilon r_{\text{evap}}}{3 + \varepsilon r_{\text{evap}}} \left(\frac{\varepsilon}{\varepsilon + 1} \right), \quad (18)$$

which gives the correct asymptotic dependence for both small and large evaporation radii.

The dependence of the total accretion efficiency described by Eqs. (15) and (18) on the evaporation radius is shown in Fig. 1. As requested, this efficiency reduces to 1/12 if no evaporation takes place ($r_{\text{evap}} = 3$), it drops for increasing r_{evap} due to the decreasing contribution of the cold disk emission and finally it saturates at the value characteristic of the ADAF solution itself. This last value depends significantly both on the viscosity parameter (directly responsible for angular momentum transfer) and on the magnetic field strength parameter β (regulating the electron cooling through the synchrotron emission).

2.5. Minimum Eddington ratio and maximum line width for broad line objects

We assume that broad emission lines cannot form in the radial range inside the evaporation radius. Therefore the equality

$$R_{\text{evap}} = R_{\text{BLR}} \quad (19)$$

gives the minimum Eddington ratio for which the BLR can exist for a given black hole mass M , assuming a certain value of the viscosity parameter α and/or of the magnetic pressure contribution β .

The same condition, combined with Eq. (6) gives the maximum value of the $FWHM$ of $H\beta$, again for a given M , α and/or β .

Both $FWHM$ of $H\beta$ and the Eddington ratio can be obtained or estimated on the basis of the observational data. When complemented with black hole mass estimates for each source, the measured values provide constraints for α and/or β .

3. Results

3.1. BLR radii and disk evaporation radii in three models

The plots of R_{BLR} and R_{evap} as functions of the Eddington ratio for the considered models are shown in Fig. 2. The position of the straight line representing R_{BLR} is the same for all models and depends only on the mass of the object (see Eq. (4)). The evaporation radius depends on the model.

In the upper panel of Fig. 2 we show the results based on the *strong ADAF principle* (model A) for three values of the viscosity parameter α and two extreme values of the parameter β . Lowering the value of the viscosity strongly decreases the inner ADAF region (see Eq. (8)). The weak dependence on β is caused by the change in accretion flow efficiency in the ADAF part (see Eq. (17)).

The intersection of R_{tr}^A and R_{BLR} determines the minimum Eddington ratio, for a given α and β , for which the BLR exists: below this value the BLR would form in the ADAF zone. Therefore, again for a given α , the size of the BLR as a function of accretion rate is defined as a fragment of the R_{BLR} line above the crossing point. For a $10^8 M_\odot$ object and $\alpha \sim 0.03$, this minimum Eddington ratio of a broad line object is about 0.005, and the minimum value of R_{BLR} is about $400 R_{\text{Schw}}$, corresponding to the maximum value of the $FWHM$ equal to $12\,200 \text{ km s}^{-1}$. The minimum Eddington ratio increases and the $FWHM$ maximum decreases with increasing α .

In the middle panel of Fig. 2 we plot the results for Model B, varying the parameter β . In this case the effect of β is much stronger than in the ADAF approach since the magnetic field affects the evaporation efficiency directly (see Eq. (10)), apart from the change of hot flow efficiency. A weaker magnetic field (higher β) allows the disk to extend closer in. The minimum Eddington rate of a broad line object is predicted to be ~ 0.003 for low magnetic field and $\sim 10^{-4}$ for $\beta = 0.1$. The lack of dependence on α is caused by the arbitrary assumption of $\alpha = 0.3$ made by Meyer & Meyer-Hofmeister (2002), with no results available for other values of the viscosity parameter.

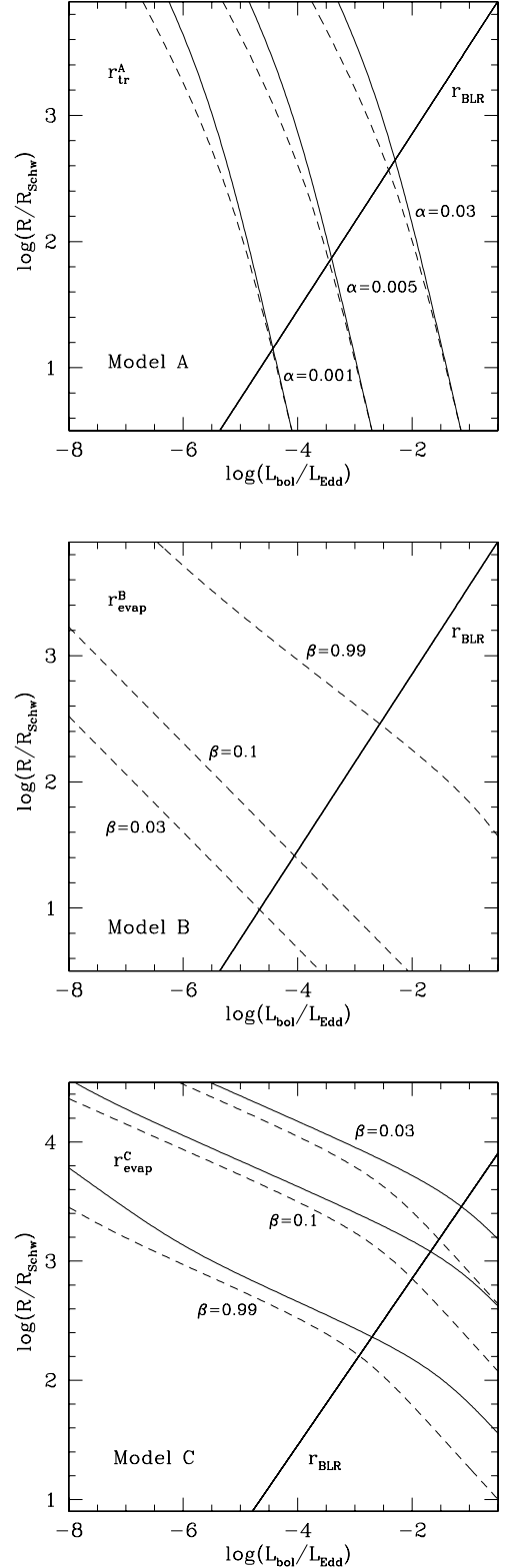


Fig. 2. The dependence of the BLR radius (thick continuous line) and the transition radius (thin lines) on the external accretion rate in model A (upper panel), model B (middle panel) and model C (lower panel) for the black hole mass $10^8 M_\odot$. Model A parameters: $\beta = 0.99$ (continuous thin lines), and $\beta = 0.03$ (dashed thin lines). Model B parameters: $\alpha = 0.3$ (dashed lines). Model C parameters: $\alpha = 0.1$ (continuous thin lines), and $\alpha = 0.02$ (dashed thin lines). The intersection determines the minimum Eddington ratio for a broad line object and the minimum BLR radius.

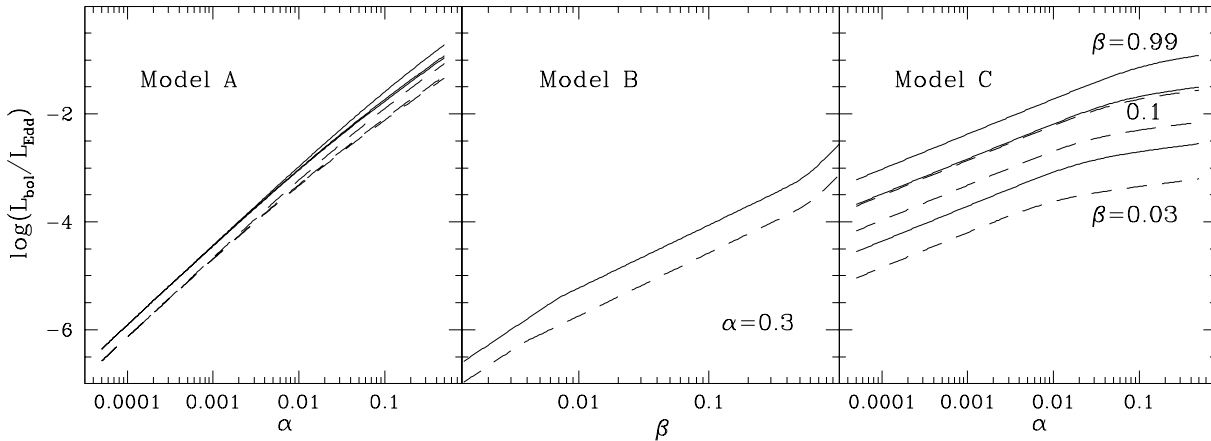


Fig. 3. The dependence of the minimum of the Eddington rate for three models A (*left*), B (*middle*), and C (*right panel*) on viscosity and magnetic parameters. Note that model B is computed only for $\alpha = 0.3$ (see text). Solid lines represent the case of $M_{\text{BH}} = 10^8 M_{\odot}$, while dashed lines – $10^6 M_{\odot}$.

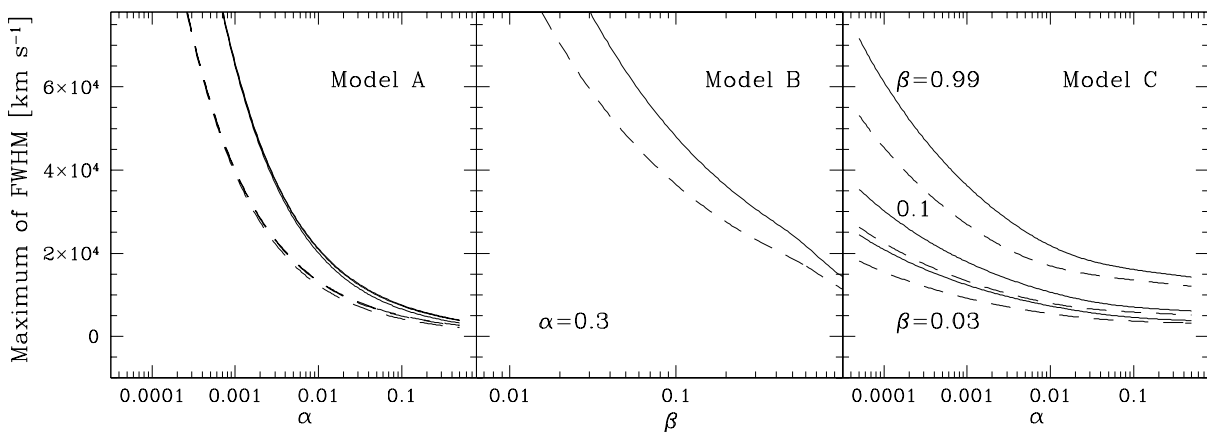


Fig. 4. The dependence of the maximum of *FWHM* for three models A (*left*), B (*middle*), and C (*right panel*) on viscosity and magnetic parameters. Note that model B is computed only for $\alpha = 0.3$ (see text). Solid lines represent the case of $M_{\text{BH}} = 10^8 M_{\odot}$, while dashed lines – $10^6 M_{\odot}$.

The results for the model C are shown in the lower panel of Fig. 2. Here we have a strong dependence on both α and β since again the magnetic field plays an active role in the process of the disk evaporation (see Eq. (13) and the Appendix). Generally, larger magnetic field leads to more efficient disk evaporation and consequently the formation of the BLR closer to the black hole is strongly limited.

3.2. Minimum Eddington rate of a broad line object

The minimum Eddington rate of a broad line object is defined by the line crossings in Fig. 2. It depends on the black hole mass, viscosity and the magnetic field. We summarize some of these relations in Fig. 3.

The values obtained from the classical ADAF solution are very low unless the viscosity parameter is of the order of 0.01 or larger, and the dependence on the magnetic field is negligible (see Fig. 3, left panel). Derived limits formally depend on the assumed black hole mass (Fig. 2 was constructed for $M_{\text{BH}} = 10^8 M_{\odot}$, but the analysis can be repeated for other black

hole masses). However, in the case of the ADAF model, this dependence is rather weak.

The values obtained from model B also span the whole range, increasing significantly with an increase of the magnetic field. Larger black hole mass results in a larger value of the minimum bolometric luminosity of a BLR object.

In the case of model C the dependence on all parameters, α , β and the black hole mass is important. The Eddington ratio plot is generally flatter, and even for very low viscosity and a strong magnetic field the minimum Eddington ratio is larger than $\sim 10^{-5}$.

3.3. Maximum line width of a broad line object

The size of the BLR corresponds to the *FWHM* of the H_{β} line (see Eq. (5)), so we can replace the radius with the values of *FWHM* which is directly measured from observations. Therefore, the allowed region in the $R - L/L_{\text{Edd}}$ diagram translates into the equivalent region in the *FWHM* – L/L_{Edd} diagram according to Eq. (6). Alternatively, to represent these limits we

can plot the maximum $FWHM$ as a function of the adopted parameters.

The resulting maximum of the $FWHM$ as a function of α or β is shown in Fig. 4. All models show clear dependence of the limits on the black hole mass (dashed and continuous lines for $10^6 M_\odot$ and $10^8 M_\odot$, correspondingly)

Classical ADAF solution allows for very broad lines if the viscosity is small. Model B also displays large parameter range coming from adoption of weak or strong magnetic field. In the case of model C the dependence of the $FWHM$ is shallower and very broad lines are expected only for very low viscosity and very weak magnetic field; otherwise, evaporation is too efficient for a cold disk to survive close to a black hole.

4. Comparison with observations

Theoretical constraints for the properties of the broad line objects can be compared with the observed properties. We attempt to perform such a comparison using the sample of objects collected from the literature. The measured quantities as well as estimated black hole masses and Eddington rates for these objects are summarized in Table 1. These objects, taken from various samples, do not form an unbiased sample of AGN so the conclusions cannot be firm. Nevertheless, such an analysis shows the effectiveness of the method and offers some indicative results.

4.1. Data

Optical/UV spectra of LBQS (large Bright Quasar Survey) objects included in the sample of Forster et al. (2001) were studied with MMT and du Point telescopes. We selected objects for which reliable MgII line measurements were performed, supplemented by the measurement of the continuum at 2800 Å, rest frame. The measured flux was corrected for the Galactic reddening.

The mass of the central black hole was calculated from the relation found by Kaspi et al. (2000)

$$M = 4.817 \left(\frac{\lambda L_\lambda(5100 \text{ \AA})}{10^{44}} \right)^{0.7} FWHM^2 M_\odot. \quad (20)$$

We determined the $\lambda L_\lambda(5100 \text{ \AA})$ from the measured flux at 2800 Å by extrapolating the measured flux to 5100 Å, assuming a power law spectrum with a slope 0.5 (i.e. $F_\nu \propto \nu^{-0.5}$). The cosmological model used throughout the paper is $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $q_0 = 0.5$. We used Eq. (2) to determine the bolometric luminosity of an object, and subsequently its Eddington ratio, $L_{\text{bol}}/L_{\text{Edd}}$, with L_{Edd} defined by Eq. (3). The measured quantities ($FWHM$ and F_λ), the derived black hole mass and the Eddington ratio are given in Table 1.

Similarly, for objects from the sample of Kuraszkiwicz et al. (2002) and Kuraszkiwicz et al. (2004) the $FWHM$ of the MgII line was measured together with the continuum at 2800 Å, rest frame. The measurements were performed for HST data. The black hole mass of these sources and the Eddington ratio were derived as above.

For objects taken from Kaspi et al. (2000), as well as for those originally included in the study of Wandel et al. (1999), the measurements of $FWHM$ of H β lines are available, with the exception of PG 1351+640 for which an H α measurement was given, but corrected by 20% to account for a systematic difference between H α and H β line widths. The luminosity of the objects was provided in the form of λL_λ at 5100 Å, assuming the Hubble constant $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and the deceleration parameter $q_0 = 0.5$. The values of the black hole masses for these objects were derived from the reverberation measurements and were given by Kaspi et al. (2000), and we determine the Eddington ratio using the bolometric luminosity estimate of Eq. (2).

For the nearby quasars taken from Shang et al. (2003) the $FWHM$ of H β was given together with $L_\nu(1549 \text{ \AA})$. This last value was given for $H_0 = 50 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $q_0 = 0.5$ so it was necessary to recalculate it to $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ adopted in our paper. The black hole mass and the Eddington ratio were obtained as for Forster et al. and Kuraszkiwicz et al. objects.

We also include several more distant quasars from Brotherton et al. (1994a). We include in our sample only the radio-quiet sources. The MgII widths were measured for those sources, and the continuum in magnitudes measured at 2200 Å was provided by Steidel & Sargent (1991). The magnitude values were reversed into the flux measurement using the definition of Steidel & Sargent (1991), and subsequently the absolute flux at 2200 Å was derived assuming the same cosmological model as before. The black hole mass and the Eddington ratio were determined as for Forster et al. and Kuraszkiwicz et al. objects.

4.2. Results

The Eddington ratios of practically all objects from Table 1 are larger than 0.01. All these objects are classified as typical Broad Line objects: QSO, Seyfert 1 galaxies or Narrow Line Seyfert 1 galaxies. The maximum values of the $FWHM$ among the objects in our sample do not exceed $17\,000 \text{ km s}^{-1}$, well within the conservative upper limit for a Broad Line object adopted by Laor (2003b) in his discussion. Therefore, our sample supports the conclusion that Broad Line objects exist above a certain threshold in the Eddington ratio, and the widths of their broad lines are limited. Such an interpretation is consistent with an accretion scenario based on the evaporation of the inner cold disk in objects with a low Eddington ratio.

In order to determine which of the three specific models (see Sect. 2.3) better represents the allowed parameter space for the Broad Line objects we use two diagrams. In Fig. 5 we show the dependence between the line width and the Eddington ratio for objects from our sample. Objects coming from various subsamples are marked with different symbols but they all form a mostly uniform distribution. The black dot marking an object with a rather large $FWHM$ ($15\,000 \text{ km s}^{-1}$) and low Eddington ratio (0.0022) represents the source Arp 102B (the second to last source from Reference 3 in Table 1), which belongs to the

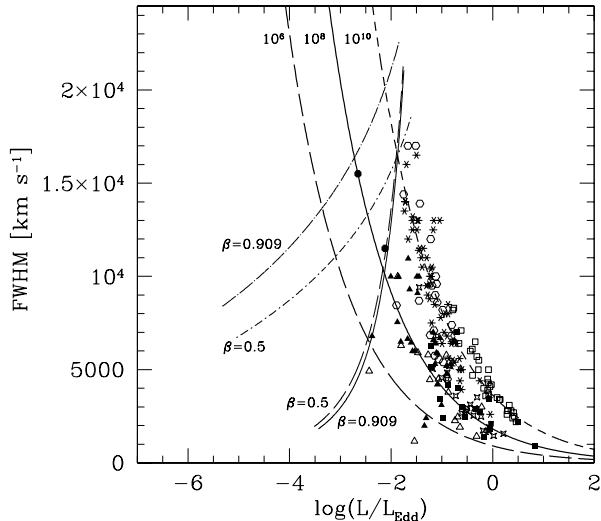


Fig. 5. The dependence of full width of half maximum of the broad line on bolometric luminosity. Observational points come from Table 1. Lines marked with the corresponding values of the black hole mass show the trends given by Eq. (6). Other lines constrain the parameter space of the Broad Line objects: continuous line and long-dash line represent the ADAF (model A) with the viscosity $\alpha = 0.04$ in the case of negligible magnetic field and for $\beta = 0.5$, correspondingly; dashed lines show the limits based on model C assuming viscosity parameter $\alpha = 0.02$ and again two values of β (0.909 and 0.5, correspondingly).

class of radio loud objects with double peaked broad emission lines (Chen & Halpern 1989).

We did not plot error bars in Fig. 5 since they are rather difficult to assess. The measurements of the $FWHM$ are performed with 20–30 percent accuracy; the Eddington ratio is in most cases derived on the basis of statistical correlations like those given by Eqs. (2) and (20) which show a certain intrinsic scatter.

The objects basically follow the relation between the line width and the Eddington ratio given by Eq. (6) marked in Fig. 5 for three specific values of the black hole mass. Therefore, the relation found by Kaspi et al. (2000) seems to describe the whole sample of objects quite well. The upper limits for the line width at a given Eddington ratio, estimated from two models, are marked as lines roughly perpendicular to the Kaspi et al. relations. A successful model should clearly separate the region occupied by objects from the avoidance region.

We plot four limiting lines coming from two models. The ADAF solution (model A) is represented by two lines: a continuous line for a negligible magnetic field and long dashed line for $\beta = 0.5$; $\alpha = 0.04$ in both cases. Evaporation model C is represented by two other lines: a long-dash-dot line (negligible magnetic field) and a short-dash-dot line ($\beta = 0.5$); $\alpha = 0.02$ in both cases.

Here it is apparent that all theoretical constraints for the line width are not universal, but show some dependence on the Eddington ratio: the line is allowed to be broader for an object with a lower mass/lower Eddington ratio. However, the strength of this coupling depends on the model. In the ADAF model the limiting line is quite steep and the upper limit from the line

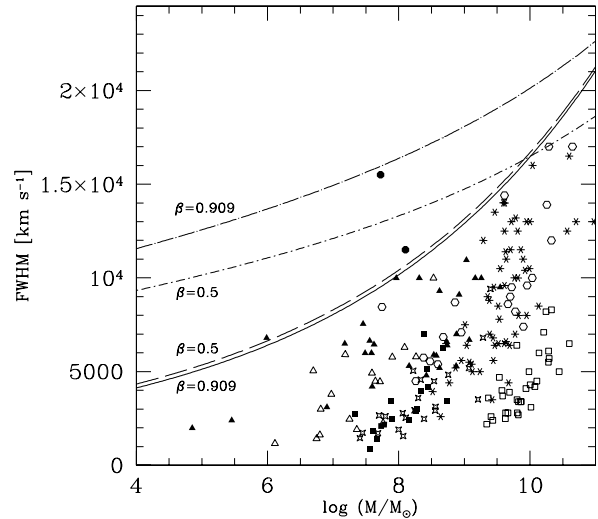


Fig. 6. The dependence of full width of half maximum on the black hole mass. Observational points come from Table 1. Continuous and long-dashed lines represent the limits based on model A, viscosity parameter $\alpha = 0.04$, $\beta = 0.909$ and $\beta = 0.5$, correspondingly. Short-dash-dot line and long-dash-dot lines are for $\beta = 0.5$ and $\beta = 0.909$.

width is almost universal while in the evaporation model C the line is flatter and the predicted limiting value for the line width depends considerably on the object mass and Eddington ratio. Meyer-Hofmeister & Meyer (2001) have shown some calculations of evaporation rate for different values of the viscosity parameter. They took into account a wind from the corona, which can affect the general solution. The effect of incorporation of the wind losses also depends on viscosity. Taking into account these results, it is apparent that the dependence of their model on viscosity is intermediate between the ADAF and our evaporation model C.

A change in the viscosity parameter results in essentially a parallel shift of a line, without significant change of the line slope. For example, increasing the viscosity parameter α results in moving the limiting line given by the model C closer to the data points but generally either some of the objects with the broadest lines are already above the threshold or there is a large region to the left of the line which should be populated by broad line objects but no data points are actually there. The steeper relation coming from ADAF seems to better represent the populated region. The best value of the viscosity parameter is around 0.04, as adopted in Fig. 5.

Similarly, we can assess the dependence of the line width on the black hole mass. In Fig. 6 we plot the objects from our sample. Objects occupy predominantly the lower right corner of the diagram. The allowed region, according to a specific model, is shown with lines, as in Fig. 5. Limits for the line width in both models depend on the mass (objects with larger masses are allowed to have broader lines) but the exact shape of this dependence is different in the ADAF model and in the evaporation model. Changing the viscosity parameter α it is possible to move the lines up or down but without a strong change of the shape. Again it is apparent that the region populated by the objects from Table 1 is better described by the

classical ADAF than a more complex evaporation model, and the favored viscosity parameter $\alpha = 0.04$.

5. Discussion

Results presented in this paper support the existence of a connection between the BLR and the survival of the cold disk sufficiently close to the central black hole. This agrees with general conclusions of Nicastro et al. (2003) and Laor (2003b), but it takes this idea one step further.

Each specific mechanism of cold disk disruption/evaporation gives a specific shape of the allowed region for broad line objects in the line width-Eddington ratio and line width-black hole mass diagram. We considered three models of the inner cold disk disappearance and for two of them (classical ADAF and generalized disk evaporation model of Róžańska & Czerny 2000b) we constructed the detailed theoretical region boundaries for the broad line region objects in these two diagrams. We placed on this diagram a large sample of broad line AGN taken from the literature.

Perhaps surprisingly, the classical ADAF model represented the disk disappearance conditions better than the disk evaporation model. The value of the viscosity best representing the allowed parameter space ($\alpha = 0.04$) is quite reasonable, in view of estimates based on AGN variability (~ 0.02 , Starling et al. 2004) or on the results the MHD simulations of the MRI (magneto-rotational) instability now accepted as the physical source of viscosity (again, ~ 0.02 , Winters et al. 2003). However, the apparent superiority of the ADAF solution may be caused by selection effects. The avoidance region of broad line objects is characterized by small black hole masses and small Eddington ratio so these objects are actually very faint.

A consistent picture of an AGN activity emerges from recent papers, including our results. The key parameter governing the character of activity is indeed the Eddington ratio of an object. Specifically, the accretion flow in sources radiating above a per cent, or a few per cent, of the Eddington ratio proceeds predominantly in the form of a cold disk even quite close to the black hole. The continuum spectra of these sources show a prominent optical-UV Big Blue Bump, extending in some sources well into soft X-rays. The optical/UV emission lines are broad, and the iron K_α line is broadened (although not necessarily extremely broad). A natural conclusion is that all those features are related to the existence of the cold disk down to a few hundred - a few tens of the Schwarzschild radii, or less.

Accretion flow in sources radiating at the Eddington ratio below one per cent, or a few per cent of the Eddington ratio do not develop features such as a Big Blue Bump and broad emission lines (Tran 2001, 2003). At the same time they are unlikely to contain radiatively efficient inner flow (e.g. Merloni et al. 2003), and their emission may originate predominantly as a synchrotron emission of the jet (Merloni et al. 2003).

The properties are not just bi-modal but there is also clear effect of the Eddington ratio on all source properties even within its class, and perhaps a smooth transition between them. Many studies show a tight correlation of source properties with a single parameter (Boroson & Green eigenvector 1, Boroson & Green 1992; see also Marziani et al. 2003, and the

references therein) most probably representing the Eddington ratio.

As for the conclusion that the classical ADAF solution better represents the broad line objects, we treat this result as indicative rather than a proof of the failure of the other models since there are several issues which might have affected the analysis.

5.1. Accuracy of the theoretical relations

5.1.1. The size of the BLR

In the present paper we adopted the scaling from Kaspi et al. (2000), with $R_{\text{BLR}} \propto \lambda F_\lambda(5100 \text{ \AA})^{0.7}$. Extensive 20-year studies of NGC 5548 (Peterson et al. 2002) show that the situation is more complex due to the dependence of the shape of the spectrum on its luminosity in this object. Therefore, two good representations of the source behaviour were found: $R_{\text{BLR}} \propto \lambda F_\lambda(5100 \text{ \AA})^{0.95}$ and $R_{\text{BLR}} \propto \lambda F_\lambda(1350 \text{ \AA})^{0.53}$. The Kaspi et al. (2000) formula has an index intermediate between an optical and a UV law since perhaps statistically most objects show weaker dependence of the spectral shape on luminosity than NGC 5548. Since physically we expect a dependence of the BLR size on the ionizing flux (and not total bolometric luminosity) it is likely more appropriate to use UV flux, whenever possible, and perhaps a slightly smaller index in size-luminosity scaling, if statistically sound scaling is available.

5.1.2. Evaporation radius and the accretion flow efficiency

The version of solutions adopted in our considerations are the most basic and simple parametric dependences, either derived from analytical solutions or from analytical crude approximations to the numerical results. A more careful approach does not seem necessary at this stage since the physical assumptions behind the discussed models can be questioned. Therefore, the best support for the model came from as many observational tests as possible.

Liu & Meyer-Hofmeister (2001) compared the predictions of their model with the constraints for an inner disk radius from spectra analysis and they found a satisfactory agreement for most objects, but Low Luminosity AGN as for instance NGC 4579 (see also Sect. 5.2.4) and M 81 posed a problem for this paper. However, the effect of magnetic field by Meyer & Meyer-Hofmeister (2002) allowed for its solution.

5.2. Accuracy of the observational results

5.2.1. Intermediate line region

From careful studies of the UV quasar spectra, Brotherton et al. (1994b) suggested that the traditional BLR consists of two components: one of width $\sim 2000 \text{ km s}^{-1}$ and another very broad component of width $\sim 7000 \text{ km s}^{-1}$. These components also differ with respect to the net shift in comparison to the

systemic redshift. Brotherton et al. (1994b) suggested, that the first component forms an Intermediate Line Region (ILR) located further out and possessing a lower medium density and covering factor than the second component, forming a Very Broad Line Region. Similar ideas were suggested earlier by Baldwin et al. (1988) and Francis et al. (1992). As is apparent from the profile of the MgII line in the composite spectra obtained from SDSS (Fig. 5 of Richards et al. 2002), this line might well consist of a narrower core and broader shoulders.

Following those ideas, we assume that the Very Broad Line Region is related to the cold accretion disk, as the component originating closer in and originating in material moving at a faster speed. In the analysis of MgII lines by Forster et al. (2001) and by Kuraszkiwicz et al. (2002, 2004) both components were identified, and we used the *FWHM* of the VBLR component in our analysis. Such differentiation was not always done for other sources used in our paper which resulted in underestimation of some line widths.

5.2.2. MgII vs. H β lines

Both MgII and H β lines are Low Ionization Lines (LIL) and therefore are supposed to arise from the vicinity of accretion disks (Collin-Souffrin et al. 1988). However, it does not need to mean automatically that they form at the same distance from the central region. For instance, the time delay measured for MgII lines in NGC 5548 (Clavel et al. 1992) is larger by a factor of three than the time delay of H β in the same source (Peterson et al. 1999). The scaling law of Kaspi et al. (2000) (see Eq. (1)) is based on H β and the use of MgII lines in principle requires an adjustment of the approach. However, McLure & Jarvis (2002) find the BLR scaling $R_{\text{BLR}} \propto \lambda L_{\lambda}$, if MgII lines are used and the continuum is measured at 3000 Å but otherwise they do not find any systematic difference in *FWHM* of MgII and H β , as expected if both lines are emitted at the same distance from the central ionizing source.

Among the objects included in Table 1 there are two sources with independent measurements of MgII and H β by various authors. The measured MgII line is much broader than H β (PG 1211+143: 5400 km s $^{-1}$ vs. 1832 km s $^{-1}$; Mkn 335: 5300 km s $^{-1}$ vs. 1620 km s $^{-1}$). However, McLure & Jarvis give 2050 km s $^{-1}$ for the MgII *FWHM* of PG 1211+143. This difference illustrates the possible problems. On the one hand, the data of McLure & Jarvis (2002) taken with IUE is of lower quality than the FOS/HST data analyzed by Kuraszkiwicz et al. (2002, 2004) and no differentiation between the ILR and VBLR components could have been done by those authors. The Kuraszkiwicz et al. data were obtained with the HST, with good S/N. On the other hand, the modeling of MgII in NLS1 galaxies is possibly a subject of large systematic errors due to the presence of strong FeII emission. A specific template has to be used in order to account for FeII before MgII modeling can be done (I Zw1 has been used by Kuraszkiwicz et al., following the analysis of Vestergaard & Wilkes 2001) and therefore the measurement of the *FWHM* of MgII may depend on this choice.

5.2.3. Estimate of Eddington ratio

The estimate of the Eddington ratio in a given object relies both on estimates of the source bolometric luminosity as well as the black hole mass. The method used in our paper is the simplest but relies on a single measured parameter (λF_{λ} at some wavelength). Still, errors do not appear large if we compare for example the mass of the black hole determined in this way with masses from BLR monitoring. For example, logarithms of black hole masses for NGC 3227 and NGC 3516 carefully determined by Onken et al. (2003), equal to 7.56 and 7.23 respectively, are similar to the values used in our paper (see Table 1). However, in principle the use of a direct method of a black hole mass estimation would be more appropriate since the mass and the accretion are independent parameters, as stressed in the study of Woo & Urry (2002).

5.2.4. Low luminosity AGN

Low Luminosity AGN do not seem to pose a problem for the picture. Our sample contains a few such objects. The well studied case of NGC 4579 is a good example. Classified as a LINER, this object shows a broad component in its H α line (Barth et al. 2001) with FWZI of 18 000 km s $^{-1}$, and the *FWHM* can be roughly estimated as ~ 8000 km s $^{-1}$ (see their Fig. 1). We have this object in our sample (see Table 1), with the *FWHM* of the MgII line of 6800 km s $^{-1}$. The mass estimate ($10^6 M_{\odot}$ in our paper; $4 \times 10^6 M_{\odot}$ suggested by Barth et al. 1996) locates this object relatively far to the left in our diagrams (black filled triangle), but still within the allowed region for broad line objects. However, if the mass is actually much larger (Barth et al. 2001 suggest a mass an order of magnitude higher based on black hole mass – bulge velocity dispersion relation) the object will move outside the allowed parameter space as defined by the ADAF model. However, it will remain consistent with a disk evaporation model. Iron line analysis in this source indicates, however, that the standard disk is present in this source and the source radiates at the Eddington ratio of 2×10^{-3} (Terashima et al. 2000), only by a factor of 2 lower than obtained in our analysis. Therefore, studies of more low luminosity objects with good mass determination would be particularly valuable.

5.3. Other samples/objects

5.3.1. Low luminosity objects from the SDSS survey

In the low luminosity broad/double peak H α sample from SDSS analyzed by Strateva et al. (2003), the tail of the distribution extends up to $\sim 16 000$ km s $^{-1}$. These objects cannot be included in our study and analyzed in the same manner as the other objects since these AGN usually do not show a Big Blue Bump so Eq. (20) does not apply. However, the measured width of the lines can be compared with constraints presented in Fig. 4. The maximum value of the *FWHM* of 16 000 km s $^{-1}$ indicates that, according to the standard ADAF and a black hole mass $M > 10^8 M_{\odot}$ (Model A, see Fig. 4) the corresponding value of the viscosity parameter α is about 0.02. If we adopt model B with $\alpha = 0.3$ we obtain a strong limit for the strength of the

magnetic field: the parameter β (gas pressure to total pressure ratio) must be larger than 0.7, i.e. the plasma must be gas pressure dominated. The constraints from model C give the minimum value of the viscosity α as a function of β : α about 0.1 for gas pressure dominated plasma and that could be lower if the magnetic field is important.

5.3.2. Objects considered by Nicastro et al. (2003)

The upper limits for the Eddington ratio in Broad line objects, 0.001, obtained by Nicastro et al. (2003) locate them in Figs. 5 and 6 possibly somewhere between the limits obtained from ADAF and from disk evaporation. However, the measurements of the *FWHM* of the hidden BLR was not provided by Tran (2001) who conducted the spectro-polarimetric measurements for the sample discussed by Nicastro et al. (2003).

6. Conclusions

Tran (2001, 2003) and Laor (2003b) argue that in a fraction of AGN, broad lines are not detected – but not because they are hidden from our line of sight, but because those objects do not develop a BLR. Recent X-ray observation of NGC 6251 supports this view (Gliozzi et al. 2004).

Our study shows that the existence of this class of objects is a natural consequence of the evaporation of the cold disk close to a black hole and the transition of the accretion flow into a hot optically thin phase, if the BLR formation is intimately connected with the cold disk. The transitions happens far away for low Eddington ratio objects, at distances where the ionization conditions would be correct for broad line formation, and the BLR apparently lose the needed disk “support”.

Quantitatively, the allowed parameter space (in $\log L/L_{\text{Edd}}$ vs. $\log FWHM$ and $\log M$ vs. $\log FWHM$; see Figs. 5 and 6) for broad line objects in our sample seems to be better represented by the *strong ADAF principle* than by the more physical disk evaporation model.

Acknowledgements. We are grateful to Michał Jaroszyński, Jean-Pierre Lasota and Zbyszek Loska for very helpful discussions, and to Greg Madejski for comments to the manuscript. This work was supported in part by grant 2P03D 003 22 of the Polish State Committee for Scientific Research (KBN).

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Online Material

Appendix A: Disk-corona mass exchange in the corona model with magnetic pressure component

Disk evaporation due to conductive heating of the disk interior by the hot accreting corona was proposed by Meyer & Meyer-Hofmeister (1994) in the context of the cataclysmic variables. This approach was further generalized in a number of papers (Meyer-Hofmeister & Meyer 1999; Turolla & Dullemond 2000; Róžańska & Czerny 2000a). The evaporation rate is calculated on the basis of the computations of the conduction flux between the disk and the corona. The effect depends both on the description of the conduction and the description of the corona heating/cooling and a detailed approach to its vertical structure. In accreting corona models discussed in this context, the standard assumption was that the heating is described by the viscosity parameter α and the gas pressure in the corona, as in the description of the purely hot (ADAF) flows. In the context of ADAF a generalization is frequently made to include the magnetic pressure in addition to the disk pressure, since in those models the magnetic field is needed to provide synchrotron photons for the Compton cooling. In corona models, the synchrotron photons are relatively unimportant since the soft disk photons are abundant but nevertheless the magnetic component of the total pressure can also be present. Such an effect was recently included in their model by Meyer & Meyer-Hofmeister (2002).

Here we generalize the model developed by Róžańska & Czerny (2000b) in order to include this additional magnetic pressure component.

We describe the local disk vertical structure as in Róžańska & Czerny (2000b), Sect. 2.2, but we assume now a more general formula for the pressure, P :

$$P = \frac{k}{m_{\text{H}}\rho T_i} + P_m = \frac{1}{\beta} \frac{k}{m_{\text{H}}\rho T_i}, \quad (\text{A.1})$$

where β is the gas pressure to the total (gas + magnetic) pressure ratio. Gas pressure includes only the ion component, as before.

We determine the local disk evaporation rate \dot{m}_z as a function of the total (disk + corona) accretion rate, coronal accretion rate, the black hole mass and the parameters α (viscosity) and β (magnetic field) from the Eq. (15) of Róžańska & Czerny (2000b). Modifying the code we found a numerical error in the program. New results for $\beta = 1$ (no magnetic pressure) and $\alpha = 0.1$ are shown in Fig. A.1. The dependence on the viscosity is now much weaker than in Róžańska & Czerny (2000b).

The local evaporation rate shown in Fig. A.1 increases with a decrease of the viscosity parameter and decreases with an increase of the magnetic field contribution to the pressure. These trends can be understood by considering the relative contributions to the total pressure. Specifically, the total pressure at the base of the corona is determined by the coronal accretion rate under consideration and the viscosity α . The gas pressure there is thus proportional to β/α . Since the ion temperature is not significantly lower than the virial temperature in the coronal part of the flow, the density is mostly determined by the pressure. The electron temperature is given by the equilibrium be-

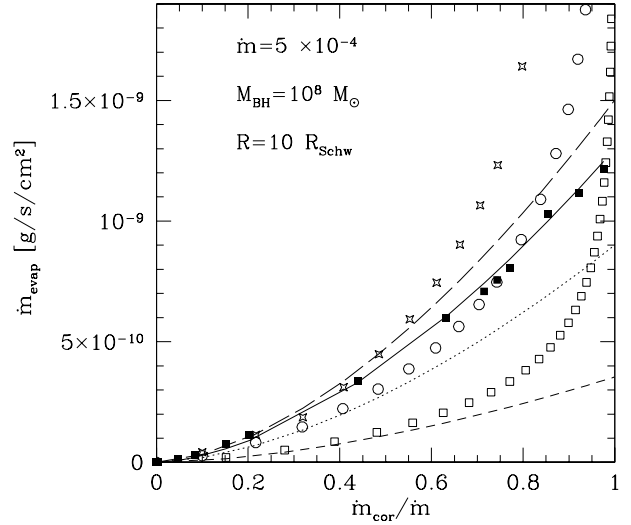


Fig. A.1. The local relation between the accretion rate in the corona and the evaporation rate of the disk at $10R_{\text{Schw}}$ for the total accretion rate $\dot{m} = 5 \times 10^{-4}$ and black hole mass $10^8 M_{\odot}$. Filled squares are from Róžańska & Czerny (2000), open circles are new results for $\alpha = 0.1$, $\beta = 1$, open squares are for $\alpha = 0.1$, $\beta = 0.5$ and stars are for $\alpha = 0.05$, $\beta = 1$.

tween the electron heating and cooling, and it increases with the rise in the density. Therefore, the electron temperature increases with β and decreases with α . This trend determines the trend of the integral determining \dot{m}_z (Eq. (15) of Róžańska & Czerny 2000).

Numerical solutions can be roughly represented by the analytical formula:

$$\dot{m}_{\text{evap}} = 1.64 \times 10^{-3} \alpha_{0.1}^{-1} \beta^{1.35} M_8^{-1} \dot{m}_{\text{cor}}^{5/3} R^{-3/4}. \quad (\text{A.2})$$

This formula combined with the need for the mass conservation in the flow (total accretion rate = coronal accretion rate + disk accretion rate) gives the solution for the dependence of the coronal accretion rate on the radius:

$$\dot{m}_{\text{cor}} = 2.62 \times 10^2 \alpha_{0.1}^{3/2} \beta^{-2.025} R^{-15/8}. \quad (\text{A.3})$$

The condition $\dot{m}_{\text{cor}} = \dot{m}$ determines the evaporation radius (Eq. (11) in this paper). Here we neglected the issue of the coronal condensation in the innermost region, discussed by Róžańska & Czerny (2000).

Table 1. Broad line objects: measured line widths and luminosities, estimates of central black holes masses and Eddington ratios, as described in the text, and the references.

Name	Spectrum	Redshift	$FWHM(MgII)$	$F_{\lambda}(2800 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
LBQS 0010+0146	0010+0146la	0.587	13 000.	-15.3856	9.72	-1.58	1
LBQS 0018-0252	0018-0252la	0.618	5600.	-15.4883	8.96	-0.86	1
LBQS 0022-0140	0022-0140la	0.776	8500.	-15.4825	9.51	-1.14	1
LBQS 0028-0101	0028-0101la	0.543	12 000.	-15.8062	9.29	-1.67	1
LBQS 0042-2750	0042-2750la	0.741	6400.	-15.7581	9.04	-0.99	1
LBQS 0047-3059	0047-3059la	0.559	8000.	-14.5679	9.83	-0.93	1
LBQS 0048-0133	0048-0133la	0.763	8500.	-14.5792	10.13	-0.88	1
LBQS 0055-2948	0055-2948la	0.663	3940.	-15.7641	8.52	-0.61	1
LBQS 0056-0009	0056-0009la	0.717	7000.	-14.7753	9.77	-0.79	1
LBQS 0057+0000	0057+0000la	0.776	8000.	-14.7906	9.95	-0.88	1
LBQS 0102-2713	0102-2713la	0.780	5400.	-15.5035	9.11	-0.75	1
LBQS 0102-0147	0102-0147la	0.571	10 000.	-14.9600	9.76	-1.24	1
LBQS 0103-2622	0103-2622la	0.776	7000.	-15.4250	9.39	-0.95	1
LBQS 0107-0235	0107-0235la	0.958	10 500.	-15.3280	9.99	-1.20	1
LBQS 0252+0141	0252+0141la	0.621	13 000.	-15.1197	9.95	-1.48	1
LBQS 0253-0138	0253-0138la	0.879	16 500.	-14.9133	10.60	-1.50	1
LBQS 0257+0025	0257+0025la	0.532	6400.	-14.7526	9.46	-0.81	1
LBQS 0301+0010	0301+0010la	0.638	6600.	-14.7610	9.63	-0.78	1
LBQS 0303-0132	0303-0132la	0.606	6500.	-14.7173	9.61	-0.77	1
LBQS 0303-0241	0303-0241la	0.686	5000.	-15.0694	9.24	-0.60	1
LBQS 0305+0222	0305+0222la	0.590	10 400.	-14.8150	9.93	-1.21	1
LBQS 0307-0015	0307-0015la	0.770	6400.	-14.8683	9.69	-0.71	1
LBQS 1027-0149	1027-0149la	0.754	11 500.	-15.5531	9.70	-1.43	1
LBQS 1137+0051	1137+0051la	0.874	9500.	-15.8626	9.45	-1.31	1
LBQS 1138+0003	1138+0003la	0.500	14 000.	-15.4346	9.61	-1.72	1
LBQS 1205+1729	1205+1729la	0.548	16 000.	-15.0968	10.04	-1.70	1
LBQS 1211+0841	1211+0841la	0.585	8800.	-15.3781	9.38	-1.24	1
LBQS 1222+1640	1222+1640la	0.549	9600.	-15.0785	9.61	-1.25	1
LBQS 1222+0901	1222+0901la	0.535	13 000.	-13.4831	10.97	-1.04	1
LBQS 1224+1604	1224+1604la	0.533	7500.	-15.6004	9.01	-1.20	1
LBQS 1236+1802	1236+1802la	0.517	14 000.	-15.4997	9.60	-1.72	1
LBQS 1237+0950	1237+0950la	0.736	11 000.	-15.1948	9.89	-1.30	1
LBQS 1240+0224	1240+0224la	0.790	13 000.	-15.3358	10.00	-1.46	1
LBQS 1240+1745	1240+1745la	0.549	11 500.	-14.9485	9.86	-1.37	1
LBQS 1243+1456	1243+1456la	0.582	10 500.	-15.3523	9.55	-1.39	1
LBQS 1244+1329	1244+1329la	0.512	2600.	-14.7649	8.64	-0.05	1
LBQS 1245+1719	1245+1719la	0.752	10 000.	-15.2126	9.82	-1.21	1
LBQS 1250+0109	1250+0109la	0.792	13 200.	-15.6707	9.78	-1.57	1
LBQS 1313-0228	1313-0228la	0.704	5200.	-15.6822	8.86	-0.81	1
LBQS 1315+0150	1315+0150la	0.539	12 500.	-15.0981	9.81	-1.49	1
LBQS 1319+0033	1319+0033la	0.530	11 400.	-15.2236	9.63	-1.45	1
LBQS 1322-0204	1322-0204la	0.573	7800.	-14.9842	9.53	-1.03	1
LBQS 1323+0205	1323+0205la	0.641	4400.	-15.4965	8.77	-0.64	1
LBQS 1326+0206	1326+0206la	1.442	13 000.	-15.1133	10.70	-1.16	1
LBQS 1326-0257	1326-0257la	0.743	5000.	-15.3303	9.12	-0.65	1
LBQS 1328+0205	1328+0205la	0.692	3500.	-14.3684	9.43	-0.08	1
LBQS 1340-0020	1340-0020la	0.786	11 000.	-15.6413	9.64	-1.41	1
LBQS 1433+0011	1433+0011la	0.583	9000.	-15.4353	9.36	-1.28	1
LBQS 1440-0234	1440-0234la	0.678	4400.	-14.2734	9.67	-0.26	1
LBQS 1445+0222	1445+0222la	0.775	6800.	-15.3117	9.44	-0.90	1

Table 1. continued.

Name	Spectrum	Redshift	$FWHM(MgII)$	$F_{\lambda}(2800 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
LBQS 2132–4228	2132–4228la	0.569	6500.	–15.9061	8.72	–1.15	1
LBQS 2142–4318	2142–4318la	1.118	5500.	–16.0346	9.07	–0.79	1
LBQS 2154–2105	2154–2105la	0.575	6500.	–14.7796	9.52	–0.81	1
LBQS 2203–2134	2203–2134la	0.576	13 500.	–15.7686	9.46	–1.74	1
LBQS 2244+0020	2244+0020la	0.973	12 500.	–14.7397	10.57	–1.17	1
LBQS 2350–0012	2350–0012la	0.561	5600.	–14.6781	9.44	–0.65	1
LBQS 2353+0032	2353+0032la	0.558	12 500.	–15.4269	9.61	–1.58	1
HST/FOS PRE-COSTAR:							
III ZW 2	0010+1058ra	0.089	8700.	–14.1559	8.86	–1.45	2
I ZW 1	0053+1241ra	0.061	5550.	–13.7892	8.48	–1.06	2
Fairall 9	0123–5848ra	0.047	5750.	–13.7382	8.38	–1.14	2
PKS 0403–13	0405–1308ra	0.571	8600.	–14.9150	9.66	–1.09	2
3C 207	0840+1312ra	0.681	9500.	–15.1675	9.72	–1.19	2
3C 215	0906+1646ra	0.412	14 400.	–15.2551	9.61	–1.75	2
B2 0923+392	0927+3902ra	0.695	12 000.	–14.6144	10.33	–1.22	2
B2 0923+392	0927+3902rb	0.695	13 900.	–14.8952	10.26	–1.43	2
3C 263	1139+6547ra	0.646	17 000.	–14.5002	10.65	–1.51	2
PG 1211+143	1214+1403ra	0.081	5400.	–13.8469	8.60	–0.97	2
MRK 205	1221+7518rb	0.071	6850.	–13.9038	8.68	–1.23	2
PG 1226+023	1229+0203ra	0.158	7400.	–13.0137	9.90	–0.80	2
3C 277.1	1252+5634ra	0.321	7100.	–15.0441	8.95	–1.16	2
3C 279	1256–0547ra	0.536	17 000.	–14.7935	10.29	–1.67	2
NGC 5548	1417+2508ra	0.017	8450.	–14.2071	7.75	–1.89	2
PG 1415+451	1417+4456ra	0.114	4500.	–14.4230	8.26	–0.89	2
3C 334	1620+1736rb	0.555	9600.	–14.5985	9.96	–1.10	2
3C 345	1642+3948ra	0.593	10 000.	–14.6169	10.03	–1.12	2
B2 2201+315A	2203+3145ra	0.295	8200.	–13.9539	9.78	–0.98	2
4C 11.72	2254+1136ra	0.326	9000.	–14.2875	9.70	–1.13	2
HST/FOS POST-COSTAR:							
MRK 335	0006+2012oa	0.026	5300.	–13.4173	8.16	–1.14	3
PG 0026+129	0029+1316ob	0.142	6700.	–13.9626	9.08	–1.03	3
MRK 348	0048+3157oa	0.015	2400.	–15.8095	5.45	–1.31	3
I ZW 1	0053+1241oa	0.061	5850.	–13.7184	8.57	–1.08	3
0318–196	0320–1926oa	0.104	10 000.	–15.7505	7.96	–2.01	3
AKN 120	0516–0008oa	0.033	9100.	–13.2105	8.92	–1.48	3
PG 0947+396	0950+3926oa	0.206	5300.	–14.3277	8.88	–0.83	3
PG 1001+054	1004+0513oa	0.161	4800.	–14.6082	8.42	–0.90	3
B2 1028+313	1030+3102oa	0.178	10 000.	–14.5558	9.17	–1.49	3
ZW 212.025	1034+3938oa	0.042	3100.	–14.9705	6.91	–1.01	3
NGC 3516	1106+7234oa	0.009	6450.	–13.4862	7.63	–1.61	3
NGC 3516	1106+7234ob	0.009	6000.	–13.5925	7.49	–1.58	3
NGC 3516	1106+7234oc	0.009	6650.	–13.6224	7.56	–1.68	3
NGC 3516	1106+7234od	0.009	6000.	–13.4524	7.59	–1.53	3
NGC 3516	1106+7234oe	0.009	7550.	–13.9228	7.46	–1.88	3
PG 1114+445	1117+4413oa	0.144	7000.	–14.3122	8.88	–1.17	3
PG 1114+445	1117+4413ob	0.144	6600.	–14.4533	8.73	–1.16	3
MC 1118+12	1121+1236oa	0.685	9500.	–15.4223	9.55	–1.26	3
GQ COMAE	1204+2754oa	0.165	12 000.	–14.8342	9.08	–1.76	3

Table 1. continued.

Name	Spectrum	Redshift	$FWHM(MgII)$	$F_{\lambda}(2800 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
1219+047	1221+0430ob	0.094	10 000.	-15.1540	8.31	-1.86	3
QSO1219+057	1219+0545oa	0.114	3300.	-15.5099	7.23	-0.95	3
1220+1601	1223+1545ob	0.081	6500.	-16.1004	7.18	-1.81	3
NGC 4579	1237+1149oa	0.005	6800.	-15.3764	5.99	-2.38	3
PG 1322+659	1323+6541oa	0.168	10 000.	-14.3634	9.26	-1.45	3
MRK 270	1341+6740oa	0.009	2000.	-15.9921	4.85	-1.34	3
PG 1352+183	1354+1805oa	0.152	5200.	-14.3633	8.62	-0.91	3
PG 1415+451	1417+4456oa	0.114	5900.	-14.3667	8.53	-1.11	3
MRK 478	1442+3526oa	0.079	6400.	-13.8295	8.74	-1.12	3
MR 2251-178	2254-1734oa	0.068	10 950.	-13.9389	9.03	-1.66	3
NGC 7469	2303+0852oa	0.016	4200.	-13.5032	7.59	-1.09	3
IRAS13349+2438	1337+2423ob	0.108	9300.	-14.7569	8.62	-1.64	3
ARP 102B	1719+4858oa	0.024	15 500.	-15.2975	7.72	-2.65	3
CYGNUS A	1959+4044oa	0.056	11 500.	-15.1480	8.10	-2.12	3
Name			$FWHM(H\beta)$	$\lambda F_{\lambda}(5100 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
3C 120	1910.	0.73000	7.36	-0.64	4
3C 390.3	10 000.	0.64000	8.53	-1.87	4
Akn 120	5800.	1.39000	8.26	-1.27	4
F9	5780.	1.37000	7.90	-0.91	4
IC 4329A	5050.	0.16400	6.70	-0.63	4
Mrk 79	4470.	0.42300	7.72	-1.24	4
Mrk 110	1430.	0.38000	6.75	-0.31	4
Mrk 335	1620.	0.62200	6.80	-0.15	4
Mrk 509	2270.	1.47000	7.76	-0.74	4
Mrk 590	2470.	0.51000	7.25	-0.69	4
Mrk 817	4490.	0.52600	7.64	-1.07	4
NGC 3227	4920.	0.02020	7.59	-2.43	4
NGC 3783	3790.	0.17700	6.97	-0.87	4
NGC 4051	1170.	0.00525	6.11	-1.54	4
NGC 4151	5910.	0.07200	7.18	-1.47	4
NGC 5548	6300.	0.27000	8.09	-1.80	4
NGC 7469	3000.	0.55300	6.81	-0.22	4
Name			$FWHM(H\beta)$	$\lambda F_{\lambda}(5100 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
PG 0026+129	2100.	7.00000	7.73	-0.03	5
PG 0052+251	3990.	6.50000	8.34	-0.68	5
PG 0804+761	2984.	6.60000	8.28	-0.60	5
PG 0844+349	2730.	1.72000	7.33	-0.25	5
PG 0953+414	2885.	11.90000	8.26	-0.34	5
PG 1211+143	1832.	4.93000	7.61	-0.06	5
PG 1226+023	3416.	64.40000	8.74	-0.08	5
PG 1229+204	3440.	0.94000	7.88	-1.05	5
PG 1307+085	4190.	5.27000	8.45	-0.87	5
PG 1351+640	1404.	4.38000	7.66	-0.17	5
PG 1411+442	2456.	3.25000	7.90	-0.54	5
PG 1426+015	6250.	4.09000	8.67	-1.21	5
PG 1613+658	7000.	6.69000	8.38	-0.70	5
PG 1617+175	5120.	2.37000	8.44	-1.21	5
PG 1700+518	2180.	27.10000	7.78	0.51	5
PG 1704+608	890.	35.60000	7.57	0.84	5
PG 2130+099	2410.	2.16000	8.16	-0.97	5
Name		Redshift	$FWHM(H\beta)$	$\log L_{\nu}(1549 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
PG 0947+396	...	0.2056	4830.	30.33	8.76	-0.89	6
PG 0953+414	...	0.2341	3130.	30.59	8.56	-0.44	6

Table 1. continued.

Name	Spectrum	Redshift	$FWHM(MgII)$	$F_{\lambda}(2800 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
PG 1001+054	...	0.1603	1740.	29.73	7.45	-0.19	6
PG 1114+445	...	0.1440	4570.	29.80	8.34	-1.01	6
PG 1115+407	...	0.1541	1720.	30.08	7.68	-0.07	6
PG 1116+215	...	0.1759	2920.	30.67	8.56	-0.36	6
PG 1202+281	...	0.1651	5050.	29.51	8.22	-1.18	6
PG 1216+069	...	0.3319	5190.	30.69	9.07	-0.85	6
PG 1226+023	...	0.1575	3520.	31.37	9.21	-0.31	6
PG 1309+355	...	0.1823	2940.	30.21	8.24	-0.50	6
PG 1322+659	...	0.1675	2790.	30.02	8.06	-0.51	6
PG 1352+183	...	0.1510	3600.	30.04	8.30	-0.73	6
PG 1402+261	...	0.1650	1910.	30.40	8.00	-0.07	6
PG 1411+442	...	0.0895	2670.	29.56	7.70	-0.61	6
PG 1415+451	...	0.1143	2620.	29.72	7.80	-0.55	6
PG 1425+267	...	0.3637	9410.	30.42	9.40	-1.45	6
PG 1427+480	...	0.2203	2540.	30.20	8.11	-0.38	6
PG 1440+356	...	0.0773	1450.	29.90	7.41	0.02	6
PG 1444+407	...	0.2670	2480.	30.63	8.39	-0.23	6
PG 1512+370	...	0.3700	6810.	30.66	9.28	-1.09	6
PG 1543+489	...	0.4000	1560.	30.75	8.07	0.21	6
PG 1626+554	...	0.1317	4490.	30.11	8.54	-0.90	6
Name		Redshift	$FWHM(MgII)$	$M(2200 \text{ \AA})$	$\log M$	$\log L/L_{Edd}$	Ref.
0009-0138	...	2.0000	3500.	-28.0	10.04	0.24	7
0013-0029	...	2.0860	2200.	-27.0	9.37	0.53	7
0019+0107	...	2.1340	5700.	-28.0	10.48	-0.18	7
0058+0155	...	1.9590	4200.	-28.0	10.19	0.08	7
0150-2015	...	2.1470	2800.	-28.0	9.86	0.44	7
0206+0008	...	1.8900	4100.	-28.0	10.16	0.09	7
0348+0610	...	2.0600	3400.	-29.0	10.30	0.39	7
0848+1623	...	2.0090	6100.	-28.0	10.52	-0.24	7
0856+4649	...	0.9240	6400.	-27.0	10.08	-0.49	7
0920+5800	...	1.3760	3600.	-27.0	9.68	0.05	7
0932+5006	...	1.8800	6500.	-28.0	10.56	-0.31	7
0946+3009	...	1.2160	3700.	-28.0	9.95	0.13	7
0957+5542	...	2.1000	2500.	-28.0	9.76	0.54	7
1206+4557	...	1.1580	4300.	-28.0	10.07	0.00	7
1222+0223	...	2.0500	3100.	-28.0	9.94	0.35	7
1228+0750	...	1.8130	2400.	-28.0	9.68	0.55	7
1245+3431	...	2.0680	2800.	-27.0	9.57	0.31	7
1246+3746	...	2.2120	5500.	-27.0	10.18	-0.26	7
1248+4007	...	1.3030	3400.	-27.0	9.62	0.09	7
1254+0443	...	1.0240	8300.	-27.0	10.33	-0.71	7
1317+5203	...	1.0220	4700.	-27.0	9.84	-0.21	7
1321+2925	...	1.3300	5000.	-26.0	9.68	-0.36	7
1338+4138	...	1.2190	3900.	-28.0	10.00	0.09	7
1407+2632	...	0.9440	8200.	-27.0	10.30	-0.71	7
1416+0906	...	2.0000	2800.	-28.0	9.84	0.43	7
1421+3305	...	1.9040	2700.	-28.0	9.80	0.46	7
1522+1009	...	1.3210	6000.	-28.0	10.39	-0.28	7
1634+7037	...	1.3340	3400.	-29.0	10.18	0.34	7
1704+7101	...	2.0000	4500.	-28.0	10.26	0.02	7
1715+5331	...	1.9290	5000.	-29.0	10.62	0.04	7
1718+4807	...	1.0840	2600.	-28.0	9.62	0.43	7
2302+0255	...	1.0440	7100.	-27.0	10.20	-0.57	7
2340-0019	...	0.8960	4000.	-27.0	9.67	-0.09	7

Note. – References: 1. Forster et al. (2002); 2. Kuraszkiewicz et al. (2002); 3. Kuraszkiewicz et al. (2004); 4. Kaspi et al. (2000), after Wandel et al. (1999); 5. Kaspi et al. (2000); 6. Shang et al. (2003); 7. Brotherton et al. (1994a). All luminosities are for $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $q_0 = 0.5$.