The stratified two-sided jet of Cygnus A

Acceleration and collimation

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Received 17 July 2015 / Accepted 7 September 2015

ABSTRACT

Aims. High-resolution Very-Long-Baseline Interferometry (VLBI) observations of relativistic jets are essential for constraining the fundamental parameters of jet formation models. At a distance of 249 Mpc, Cygnus A is a unique target for such studies, since it is the only Fanaroff-Riley Class II radio galaxy for which a detailed subparsec scale imaging of the base of both jet and counter-jet can be obtained. Observing at millimeter wavelengths unveils those regions that appear self-absorbed at longer wavelengths and enables an extremely sharp view toward the nucleus to be obtained.

Methods. We performed 7 mm Global VLBI observations, achieving ultra-high resolution imaging on scales down to 90 µas. This resolution corresponds to a linear scale of only ~400 Schwarzschild radii (for $M_{BH} = 2.5 \times 10^9 M_\odot$). We studied the kinematic properties of the main emission features of the two-sided flow and probed its transverse structure through a pixel-based analysis.

Results. We suggest that a fast and a slow layer with different acceleration gradients exist in the flow. The extension of the acceleration region is large ($\sim 10^2 R_s$), indicating that the jet is magnetically driven. The limb brightening of both jet and counter-jet and their large opening angles ($\theta_{\phi} \sim 10^\circ$) strongly favour a spine-sheath structure. In the acceleration zone, the flow has a parabolic shape ($r \propto \rho^{\frac{3}{2}} z^{\frac{1}{2}}$). The acceleration gradients and the collimation profile are consistent with the expectations for a jet in “equilibrium”, achieved in the presence of a mild gradient of the external pressure ($p \propto c^{-4}, k \lesssim 2$).

Key words. galaxies: jets – galaxies: active – instrumentation: high angular resolution

1. Introduction

The physics of extragalactic relativistic jets is one of the most exciting and challenging topics in astrophysics. Considerable progress has been made in understanding it during recent decades. By interpreting jets as fluid phenomena, their properties on parsec and kilo-parsec scales are quite well explained by applying the laws of relativistic hydrodynamics. However, a fundamental problem is still unsolved: how can jets be accelerated up to Lorentz factors of tens and how can they be so sharply collimated? The answer to these questions must be intimately related to the mechanism of jet launching. The necessity of having light jets that are able to reach relativistic speeds gradually led to excluding a purely hydrodynamic launching, i.e. exploiting the gas pressure gradient in the accretion disk, since this implies too high a mass loading. The most successful models are those that involve the extraction of rotational energy from the accretion disk (Blandford & Payne 1982) or of the black hole itself (Blandford & Znajek 1977) through the magnetic field. Some numerical simulations (McKinney & Gammie 2004; De Villiers et al. 2005) have suggested that launching from the accretion disk can only produce jets with moderate Lorentz factors ($\Gamma < 3$), while a process involving the black hole rotation can achieve $\Gamma \sim 10$ more easily (McKinney 2006). However, it is not ruled out that the inner disk can launch relativistic jets as well (Vlahakis & Königl 2004; Komissarov et al. 2007). The possibility of reaching a certain terminal Lorentz factor depends strictly on the details of the process which converts the initially magnetically dominated jet into a kinetically dominated one.

In theoretical models describing the conversion of Poynting flux, the mechanisms of acceleration and collimation of the flow show a strong interplay. The magnetic field structure is, in this context, a fundamental parameter, but certainly not the only one. In jets missing a large scale (poloidal) magnetic field, i.e. featuring a purely toroidal field (Lynden-Bell 1996), an efficient magnetic self-collimation seems unlikely (Spruit et al. 1997), and confinement from an external medium appears to be the only possibility. The pressure from a poloidal magnetic field, on the other hand, can effectively confine the flow. However, an additional contribution from the external medium is necessary for preventing the terminal speed and collimation of the flow to be reached on unreasonably large scales (Tomimatsu 1994; Beskin et al. 1998). In accreting systems like active galactic nuclei (AGN), this medium is likely to be the magnetized slow wind ejected by the edges of the accretion disk.

Exact analytic solutions for these problems are difficult to obtain if one takes the high degree of complexity of the system adequately into account. While numerical simulations can considerably improve our knowledge, direct observations of the fundamental parameters of the flow on small scales are equally decisive. With the development of VLBI techniques at millimeter wavelengths and of space-VLBI, the spatial resolution achievable in observations of radio loud AGN has dramatically improved over the past few years, allowing us to zoom into the innermost regions of extragalactic jets. Besides the possibility of obtaining explicit measurements of speeds, scale of the acceleration, and shape of the flow, high resolution VLBI observations also allow the internal structure of the flow to be examined.
Recent parsec and subparsec scale imaging has revealed that relativistic jets are far from the simple assumption of homogeneous conical outflows, and instead they show a complicated transverse structure. Among other characteristics, limb brightening was observed both in some nearby FRI radiogalaxies, such as M 87 (Kovalev et al. 2007) and 3C 84 (Nagai et al. 2014), and in blazars, as in the case of Mrk 501 (Giroletti et al. 2004) and 3C 273 (Lobanov & Zensus 2001). Limb brightening has often been interpreted as the result of a spine-sheath structure of the jet, i.e., one made of a fast and light ultra-relativistic spine embedded in a cylindrical flow of slower and denser material (Sol et al. 1989). Such a scenario provides a good explanation for some inconsistencies between observations and the standard unified model for AGN (Barthel 1989), such as the lower Lorentz factors and lower intrinsic jet powers derived in FRI galaxies (sheath-dominated) with respect to BL Lac objects (spine-dominated) (Hovatta et al. 2009; Xu et al. 2000). Also, a spine-sheath interaction seems to be an essential ingredient for spectral energy distribution (SED) modeling of TeV BL Lacs, where the high energy emission can hardly be reconciled with the low Lorentz factors deduced from VLBI studies (Ghisellini et al. 2005). The origin of such stratification is, however, unclear. A two-component jet with the described properties could arise directly (Hardie et al. 2007; Xie et al. 2012) from a jet launching process in which the external sheath is ejected from the accretion disk, while the central spine is fueled from the ergosphere. Alternatively, as shown in Lobanov & Zensus (2001) for 3C 273, a double-rail structure can also be effectively created by helical Kelvin-Helmholtz instabilities. In this case, if the emission is dominated by the pressure-enhanced regions of the instability, the observed motions will be those of the instability patterns, typically propagating at much lower speeds (0.1–0.5 c) compared to the flow or the shocks in the jet.

In the following we present a study of the jet transverse structure and kinematics of the Fanaroff-Riley II (FRII) radio galaxy Cygnus A, from Global VLBI observations at 43 GHz. At the source redshift \( z = 0.056 \), 1 mas \( \sim 1.084 \) pc, assuming a \( \Lambda \)CDM cosmology with \( H_0 = 70.5 \) km \( s^{-1} \) Mpc\(^{-1}\), \( \Omega_M = 0.27 \), \( \Omega_\Lambda = 0.73 \), these provide an angular resolution of \( \sim 400 \) Schwarzschild radii for \( M_{\text{BH}} = 2.5 \times 10^9 \) M\(_\odot\) (Tadhunter et al. 2003) and allow the immediate surroundings of the central engine to be imaged. In addition to the proximity, the choice of this target is motivated by further advantages. Firstly, the jet of Cygnus A is seen at a large viewing angle in the range \( 50^\circ - 85^\circ \) (Bartel et al. 1995, and references therein). This means that both geometrical and relativistic effects are much reduced, implying respectively that the intrinsic morphology and speed of the flow can be more easily inferred and that a counter-jet can be detected. Moreover, both the main jet and the counter-jet can be transversally resolved on subparsec scales, which is fundamental for studying the collimation. Ultimately, while much more such studies have been carried out on FRII radio galaxies (e.g., M 87, 3C 84, Cen A), few observational constraints have been provided for strong FRI objects, mainly because their jets are generally fainter on parsec scales. Cygnus A is in this respect a unique target.

The paper is organized as follows. In Sect. 2 we present the observational setup and data reduction; in Sect. 3 we describe the methods used for the kinematic analysis and the study of the transverse intensity profiles; in Sects. 4 and 5 we present and discuss the results, which are summarized in Sect. 6.

### 2. Observations and data reduction

The data set comprises four epochs at 7 mm (43 GHz) from Global VLBI observations made between 2007 and 2009 (Table 1). The long total on-source time of about eight hours, spanning a \( \sim 16 \)-h track, and the large number of antennas (varying between 13 and 15) produced good UV coverage. During observations, antennas were frequently switched between the target and the nearby calibrator 2013+370, in order to reduce pointing errors at the biggest dishes. For the first three epochs, data were recorded in dual polarization mode using four sub-bands (IFs) with a total bandwidth of 64 MHz per polarization (512 Mb/s recording rate). The last epoch, instead, was observed in single polarization, with 16 sub-bands and a total bandwidth of 128 MHz. Data were calibrated in AIPS (Astronomical Image Processing System) following the standard procedures, including fringe fitting, opacity correction for atmospheric attenuation, and bandpass calibration. The imaging and self-calibration of amplitude and phase were performed in DIFMAP (DIFFference MAPping).

### 3. Data analysis

#### 3.1. Model fitting and alignment of the images

Since the absolute position information is lost during phase self-calibration of VLBI data, one of the main difficulties in multi-epoch studies is image registration. This can be particularly challenging in the case of radio galaxies because, unlike in blazars, a prominent VLBI core to be taken as the stationary reference point is usually missing. To obtain a simplified model of the source, we have fitted circular Gaussian components to the complex visibilities using the MODELFIT subroutine in DIFMAP. The components were then cross-identified in the four epochs, taking their size, flux density, and the morphology of the region into account (Fig. 1 and Table 2). The images were finally shifted and aligned on the position of component N, which is assumed to be stationary. Although it may not coincide with the true jet base, this feature is the most compact, and it describes a region with negligible morphological changes. The same choice was
made in Krichbaum et al. (1998; there named J0), based also on a spectral analysis. By applying the aforementioned shift, the positions of a sharp gap of emission at 0.2 mas to the east of component N also become aligned. The nature of this feature, already noticed in Bach et al. (2008) is discussed in Sect. 5.6. According to the cross-identification described, a new component (J1) was ejected between October 2007 and March 2009, accompanied by a brightening by about 50% of the core and inner-jet region. The kinematics resulting from this alignment is presented in Sect. 4.1.

Concerning the errors associated with the each parameter of the Gaussian components, reported in Table 2, a rigorous method taking the local signal-to-noise (S/N) in the image around each feature into account was applied (see Lobanov 2005; Schinzel et al. 2012, for the details of the method). Since the positional errors obtained are quite small compared to the beam size, conservative values equal to 10σ for the radial separation (Col. 3) and 5σ for the transverse size (Col. 5) were assumed.

### 3.2. Transverse structure

For analyzing the transverse structure of the jets in Cygnus A, the four CLEAN images were convolved with a common circular beam of 0.15 mas, which is approximately intermediate between the major and minor axes of the natural beams (Table 1). Therefore, a slight super resolution in the transverse direction was applied. The analysis was performed both on the single epoch maps and on a stacked image (Fig. 2), created after aligning the four maps as described in Sect. 3.1. To facilitate the study, the images were first rotated by 16 degrees clockwise, so that the mean jet axis was parallel to the x axis, and sliced pixel-by-pixel (1 px = 0.03 mas) using the AIPS task SLICE in the transverse direction. Then, the transverse intensity distributions of each slice were fitted with Gaussian profiles using the task SLFIT. This task was ran twice for the entire length of the jets, first fitting a single Gaussian and then fitting two Gaussian profiles.

### 4. Results

#### 4.1. Kinematic analysis and components light-curves

The proper motions μ of the features described in Fig. 1 were calculated by fitting their radial separations z (Table 2, Col. 3) from component N with time t, as shown in Fig. 3. The motion of components J2 and J3 is described best by second-order polynomial fits. The results are presented in Table 3. The slope parameters of the second-order polynomial fits, calculated by fitting their radial separations z (Table 2, Col. 3) from component N with time t, are shown in Table 4. The values of the intermediate epoch 2008.79 are also included.


<table>
<thead>
<tr>
<th>ID</th>
<th>Ep.</th>
<th>z [mas]</th>
<th>S [Jy]</th>
<th>r [mas]</th>
<th>σapp</th>
</tr>
</thead>
<tbody>
<tr>
<td>C1</td>
<td>1</td>
<td>0.504 ± 0.043</td>
<td>68 ± 14</td>
<td>0.240 ± 0.043</td>
<td></td>
</tr>
<tr>
<td></td>
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<td></td>
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<td>78 ± 15</td>
<td>0.243 ± 0.041</td>
<td></td>
</tr>
<tr>
<td></td>
<td>4</td>
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<td>79 ± 17</td>
<td>0.222 ± 0.046</td>
<td>0.00 ± 0.06</td>
</tr>
<tr>
<td>N</td>
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<td>0.087 ± 0.002</td>
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<td>223 ± 24</td>
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<tr>
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<td>0</td>
<td>313 ± 31</td>
<td>0.101 ± 0.003</td>
<td></td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>0</td>
<td>212 ± 14</td>
<td>0.080 ± 0.002</td>
<td></td>
</tr>
<tr>
<td>J0</td>
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<td>0.131 ± 0.002</td>
<td>212 ± 15</td>
<td>0.124 ± 0.002</td>
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<td>2</td>
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<td>473 ± 39</td>
<td>0.125 ± 0.003</td>
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<td>0.098 ± 0.004</td>
<td>201 ± 25</td>
<td>0.083 ± 0.004</td>
<td></td>
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<tr>
<td></td>
<td>4</td>
<td>0.118 ± 0.003</td>
<td>341 ± 27</td>
<td>0.117 ± 0.003</td>
<td>-0.03 ± 0.03</td>
</tr>
<tr>
<td>J1</td>
<td>1</td>
<td>...</td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>2</td>
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<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.226 ± 0.005</td>
<td>446 ± 40</td>
<td>0.151 ± 0.005</td>
<td></td>
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<tr>
<td></td>
<td>4</td>
<td>0.357 ± 0.026</td>
<td>359 ± 55</td>
<td>0.228 ± 0.026</td>
<td>0.75 ± 0.04</td>
</tr>
<tr>
<td>J2</td>
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<td>0.278 ± 0.004</td>
<td>53 ± 7</td>
<td>0.060 ± 0.004</td>
<td></td>
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<td></td>
<td>2</td>
<td>0.342 ± 0.028</td>
<td>44 ± 11</td>
<td>0.066 ± 0.028</td>
<td></td>
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<tr>
<td></td>
<td>3</td>
<td>0.429 ± 0.039</td>
<td>31 ± 9</td>
<td>0.060 ± 0.039</td>
<td></td>
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<tr>
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<td>4</td>
<td>0.621 ± 0.013</td>
<td>34 ± 6</td>
<td>0.062 ± 0.013</td>
<td>0.96 ± 0.05</td>
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<tr>
<td>J3</td>
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<td>0.385 ± 0.005</td>
<td>212 ± 17</td>
<td>0.199 ± 0.005</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>0.467 ± 0.040</td>
<td>143 ± 27</td>
<td>0.257 ± 0.040</td>
<td></td>
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<tr>
<td></td>
<td>3</td>
<td>0.629 ± 0.026</td>
<td>140 ± 21</td>
<td>0.252 ± 0.026</td>
<td></td>
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<tr>
<td></td>
<td>4</td>
<td>0.789 ± 0.014</td>
<td>84 ± 13</td>
<td>0.138 ± 0.014</td>
<td>1.15 ± 0.04</td>
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<tr>
<td>J4</td>
<td>1</td>
<td>0.731 ± 0.051</td>
<td>108 ± 21</td>
<td>0.310 ± 0.051</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>0.805 ± 0.121</td>
<td>92 ± 26</td>
<td>0.332 ± 0.121</td>
<td></td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.896 ± 0.048</td>
<td>90 ± 17</td>
<td>0.291 ± 0.048</td>
<td></td>
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<tr>
<td></td>
<td>4</td>
<td>0.907 ± 0.078</td>
<td>94 ± 22</td>
<td>0.395 ± 0.078</td>
<td>0.37 ± 0.07</td>
</tr>
<tr>
<td>J5</td>
<td>1</td>
<td>1.129 ± 0.113</td>
<td>50 ± 12</td>
<td>0.411 ± 0.113</td>
<td></td>
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<tr>
<td></td>
<td>2</td>
<td>1.230 ± 0.245</td>
<td>59 ± 21</td>
<td>0.432 ± 0.245</td>
<td></td>
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<tr>
<td></td>
<td>3</td>
<td>1.315 ± 0.170</td>
<td>66 ± 20</td>
<td>0.414 ± 0.170</td>
<td></td>
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<tr>
<td></td>
<td>4</td>
<td>1.345 ± 0.248</td>
<td>64 ± 23</td>
<td>0.425 ± 0.248</td>
<td>0.44 ± 0.05</td>
</tr>
<tr>
<td>J6</td>
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<td>71 ± 20</td>
<td>0.461 ± 0.171</td>
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<td>59 ± 25</td>
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<tr>
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<td>2.058 ± 0.438</td>
<td>64 ± 27</td>
<td>0.566 ± 0.438</td>
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<tr>
<td></td>
<td>4</td>
<td>1.943 ± 0.209</td>
<td>53 ± 17</td>
<td>0.470 ± 0.209</td>
<td>0.00 ± 0.10</td>
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<tr>
<td>J7</td>
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<td>2.641 ± 0.152</td>
<td>57 ± 16</td>
<td>0.436 ± 0.152</td>
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<td>71 ± 20</td>
<td>0.395 ± 0.270</td>
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<tr>
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<td>2.923 ± 0.127</td>
<td>89 ± 23</td>
<td>0.414 ± 0.127</td>
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<tr>
<td></td>
<td>4</td>
<td>2.990 ± 0.176</td>
<td>56 ± 17</td>
<td>0.379 ± 0.176</td>
<td>0.67 ± 0.07</td>
</tr>
</tbody>
</table>


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Fig. 1. 43 GHz modelfit maps of CygA. Images were tapered and convolved with a common beam with FWHM of 0.2 × 0.1 mas, pa = −15°. Contours represent isophotes at 1.8, 3.6, 7.2, 14.4, 28.8, 57.6, and 115.2 mJy/beam. The reference point for the alignment is component N, assumed to be stationary.
polynomials, indicating an acceleration. An estimate of the kinematic parameters was obtained by fitting a simple parabola of the form \( z(t) = at^2 + c \). The motion of the remaining features, instead, appears more uniform, and a linear fit was performed. The apparent speed \( \beta_{\text{app}} = v_{\text{app}}/c \) can be calculated as \( \beta_{\text{app}} = (\mu D_L)/(c(1+Z)) \), where \( D_L \) is the luminosity distance, \( c \) the speed of light, and \( Z \) the redshift. In the case of the accelerating features, \( v_{\text{app}} \) is the speed calculated for the last epoch, November 2009. The values obtained for the apparent speed of each component are reported in Col. 6 of Table 2.

In the approaching jet we observe an acceleration up to \( \beta_{\text{app}} = 1.15 \pm 0.04 \) within ~0.8 mas of the core. Then the speed drops significantly, and increases again in the outer jet, but remaining largely subluminal. Three components do not show any significant proper motion: C1 (\( \beta_{\text{app}} = 0.00 \pm 0.06 \)), J0 (\( \beta_{\text{app}} = -0.03 \pm 0.03 \)), and J6 (\( \beta_{\text{app}} = 0.00 \pm 0.10 \)). Given that the entire nuclear region, represented by component N and by the adjacent J0 and C1, appears stationary, a slightly different choice of the reference point for the kinematic study would not change the results; therefore, the exact core registration is not crucial in this case.

The hypothesis that the inner-jet components are crossing an acceleration region is supported by their light curves (Fig. 4). The flux densities of J1, J2, and J3 decrease with time, while those of the outer features (J4-J7) are approximately constant or increase in some cases. As the jet expands, a decrease in the energy emitted by the traveling features may be expected because of adiabatic losses. We argue, however, that this effect has little impact in our case. The distance traveled by each component during the period of the monitoring is in fact short enough that they do not experience significant changes in the jet width. As shown in Table 2 (Col. 5), either the sizes of the components are approximately constant in time or they vary slightly without showing a clear trend. Instead, differential Doppler (de)-boosting may explain the observed properties better. It is important to keep in mind that the Doppler factor \( \delta \) is a monotonically increasing function of speed \( \beta \) only for a tiny range of viewing angles, approximately between 0 and 2 degrees. At larger angles, higher speeds often imply a lower boosting or even a de-boosting (\( \delta < 1 \)). The latter means that the narrow boosting cone of the emission can point away from the observer not only in the counter-jet, but also on the approaching side, at a sufficiently high speed exceeding the critical speed \( \beta_{\delta=1} \):

\[
\beta_{\delta=1} = \frac{2 \cos \theta}{1 + \cos^2 \theta} \tag{1}
\]

Flows featuring Lorentz factors as high as 50 are already de-boosted if oriented at an angle of \( \geq 11^\circ \), while a Lorentz factor of \( \sim 1.1 (\beta \sim 0.49) \) is sufficient at an angle of \( 75^\circ \). Since the viewing angle of Cygnus A is certainly large, we find it plausible
that the quick and strong decrease in flux density of the inner-jet components is instead due to a decrease in their Doppler factors, which strengthens the scenario suggested by the kinematic analysis. In this framework, the detection of the new feature J1 in March 2009 gives us the opportunity to calculate the Doppler factor of the flow at the position occupied by J1 in November 2009. $z = 0.36$ mas, and therefore to obtain an estimate for the jet viewing angle $\theta$. Assuming that the flux density of J1 is close to the intrinsic one in March 2009 (due to the low intrinsic speed we expect at that position) the decrease in flux density constrains $\delta$ according to

$$\delta = \left(\frac{S_{\text{obs}}}{S_{\text{int}}}\right)^{\frac{1}{\alpha}} ,$$

(2)

where $\alpha$ is the spectral index, $S_{\text{obs}}$ the flux density of J1 in November 2009, and $S_{\text{int}}$ the flux density in March 2009. With a classical synchrotron spectral index $\alpha = -0.7$ ($S \propto \nu^\alpha$), we obtain $\delta = 0.92$. A second constraint on the apparent speed $\beta_{\text{app}} = 0.75$ of J1 in November 2009 allows us to solve a system of two equations for deriving the viewing angle $\theta$ and the intrinsic speed $\beta$ at $z = 0.36$ mas,

$$\beta_{\text{app}} = \frac{\beta \sin \theta}{1 - \beta \cos \theta} , \quad \delta = \frac{\sqrt{1 - \beta^2}}{1 - \beta \cos \theta} ,$$

(3)

obtaining $\beta(z = 0.36) = 0.65$ and $\theta = 74.5^\circ$. The value of the viewing angle obtained can be considered an upper limit, because if the change of Doppler factor is not the only cause for the decrease in flux, a smaller viewing angle is required.

### 4.2. Ridge line

The pixel-based analysis of the transverse intensity profiles shows that they are double peaked for most of the length of the source (Fig. 5). The limb brightening is most pronounced in the inner jet, while a single ridge is visible farther out at a separation from the core between 2 and 4 mas. In the counter-jet we also find evidence of a limb-brightened structure: the two ridge lines are closer compared to the main jet, but still well separated after accounting for positional errors, which are assumed to be equal to one fifth of each FWHM. An error bar that also takes account of the S/N of the profile (as described in Fomalont 1989) was calculated for comparison. The latter yields unreasonably small errors in the brightest regions, while in the faint ones they are anyhow smaller compared to the first method of calculation. Therefore the most conservative error bars were chosen. In the central ~0.5 mas, the poor resolution does not allow a double profile to be clearly traced, and results from a single Gaussian fit are plotted. The same is done in the other regions of the jet where a well-defined double ridge is missing (error bars of the two peaks overlapping or bad fit). The disappearance of the double profile in the main jet (at $z > 2$ mas) is accompanied by an apparent bending of the jet axis toward the south and by a narrowing of the jet width, with the two ridges smoothly approaching each other. Interestingly, this position coincides with the location of the stationary component J6. While additional interpretations of this feature are proposed in Sect. 5.3, a more detailed analysis is needed to establish whether the observed structure can be ascribed to helical Kelvin-Helmoltz or to current-driven instabilities developing in the jet. However, following the previous discussion of the relativistic effects in flows seen at a large viewing angle (in summary: “the faster, the dimmer”), the most natural explanation for the observed limb brightening is the presence of a transverse gradient of the bulk Lorentz factor of a spine-sheath kind, i.e. with $\Gamma$ decreasing from the jet axis toward the edges.

### 5. Discussion

#### 5.1. Two-layer acceleration

The kinematic and light-curve analysis of the VLBI maps at 7 mm has revealed the existence of an acceleration region in...
the inner jet extending up to a deprojected distance of $\sim 0.9$ pc, assuming the viewing angle $\theta = 74.5^\circ$ derived in Sect. 4.1. In the outer jet, lower speeds are determined, in agreement with findings from VLBI at lower frequencies (Bach et al. 2003). The observed fading of the fast flow (Fig. 4) suggests that these lower speeds do not represent an intrinsic deceleration, but are simply the signature that the contribution to the emission from the slower external layers has become dominant in that region.

If we identify the two regions as representing the “fast” and the “slow” layers of the flow, respectively, we can study separately their kinematic properties. In Fig. 6 (top) we plot the calculated intrinsic speeds $\beta$ versus the deprojected distance from the core expressed in units of Schwarzschild radii $R_S$. We then note that the slow flow is also accelerating, but with a milder gradient compared to the fast one. In this case though, the range of speeds is such that the Doppler factor remains approximately constant, so we do not observe strong variations in the flux density. Both sections are accelerating over a large distance, at least of $\sim 10^3$--$10^4 R_S$. This is a characteristic signature of relativistic magnetically driven outflows (Begelman & Li 1994; Contopoulos 1995; Vlahakis & Königl 2004), in which the conversion from Poynting to kinetic flux is found to proceed quite slowly. The steeper gradient of speed that we measure for the fast flow (central spine) compared to the slow one (sheath) indicates that the conversion to kinetic energy proceeds faster for sections of the flow that are closer to the jet axis. By fitting a power law (Fig. 6, top), we find $\beta \propto z^{0.43 \pm 0.01}$ for the former and $\beta \propto z^{0.51 \pm 0.04}$ for the latter. This translates into very different behavior of the Lorentz factor (Fig. 6, bottom), whose dependence on the core separation is $\Gamma \propto z^{0.50 \pm 0.19}$ and $\Gamma \propto z^{0.11 \pm 0.04}$ for the two flows, respectively.

### 5.2. Mean opening angle

From our study, other important parameters of the flow, such as the shape and opening angle, can be estimated. From the analysis of the transverse structure (Sect. 3.2), we can infer the dependence of the jet width on the core separation. It is preferable in this case to consider not the stacked map but the single images, because this prevents the temporal evolution of the ridge line from affecting the results. Here we present our findings for the last epoch, November 2009, which is the one showing the double ridge line structure most prominently. The jet width was calculated for each slice as the separation between the edges of the two (deconvolved) FWHM. The results are shown in Fig. 7, where the deconvolved widths obtained from a single-Gaussian slice fit are plotted for comparison, and show good agreement. This indicates that the expansion of the two ridge lines coincides well with the overall expansion of the jet. We also plot the widths obtained from the model-fit analysis of all four observing epochs. With some exceptions (discussed below), there is again a substantial overlap. The jet width is clearly increasing both in jet and counter-jet up to approximately 2 mas from component N (at $z = 0$ in the plot). By performing a linear fit in this region ($|z| < 2$), we can calculate the mean apparent full opening angle $\phi_{app}$, increased relative to the intrinsic one $\phi$ by a factor.
1/\sin \theta$ due to projection. In jet and counter-jet, we respectively obtain
\[ \phi_j^{\text{pp}} = 10.2^\circ \pm 0.3^\circ, \quad \phi_{cj}^{\text{pp}} = 4.8^\circ \pm 0.4^\circ, \] (4)
which for $\theta = 74.5^\circ$ correspond to intrinsic opening angles:
\[ \phi_j = 9.8^\circ \pm 0.3^\circ, \quad \phi_{cj} = 4.7^\circ \pm 0.4^\circ. \] (5)

As also found in Krichbaum et al. (1998) at 22 GHz, the jet appears to be about two times broader than the counter-jet. Following the classical assumption of intrinsic symmetry, the apparent opening angle should in principle be the same in jet and counter-jet, unless they are strongly misaligned. Although a small misalignment is present on both pc and kpc scales, this is not enough to justify the observed difference. A possible explanation could be the different S/Ns of the approaching and receding sides, with the counter-jet being considerably dimmer than the jet at the same core separation and thus detectable over a narrower section. Also, we note that there is, in this case, a certain discrepancy between the model-fit size of C1 and the corresponding width of the intensity profile, with the first one larger and closer to the width of the jet side. This is probably an effect of the smaller beam used in the slicing, and it suggests that the counter-jet emission is less compact than the jet emission. However, the hypothesis of intrinsic asymmetry, which is indeed possible (e.g., Fendt & Sheikhnezami 2013), cannot be excluded.

Based on these results, the jets in Cygnus A can still be defined as relatively broad on the examined scale of $\sim 2$ mas. It is useful to note that the fast jet expansion cannot be clearly perceived by eye in the map in Fig. 2. This is first of all due to the beam convolution effect, causing especially the base of the jet to appear much wider than it actually is. The second reason is that, even after deconvolving the jet width, an apparent full opening angle of “only” $\sim 10^\circ$ is difficult to appreciate visually on the scale of the image. Despite the misleading appearance, however, the jets in Cygnus A are considerably broader than in blazars, in which intrinsic opening angles of $\sim (1-2)^\circ$ are typically measured (Pushkarev et al. 2009). This result, also found by examining other radio galaxies on a parsec scale, represents another piece of evidence for the spine-sheath scenario, in which sources seen at larger viewing angles become more and more sheath-dominated, hence broader, while the emission from blazars mostly comes from the strongly boosted, thin spine.

5.3. Narrowing of the jet at $z \sim 2$ mas
The increase in the jet width is not always smooth, but is characterized by some oscillations. Although an oscillating expansion can occur in jets (Daly & Marscher 1988), we cannot exclude that this is an image artifact, especially in the faint regions of the counter-jet. The narrowing at $\sim 2$ mas in the main jet and perhaps in the counter-jet, too, is, however, very prominent and coincides with the location of the stationary feature J6. Stationary features in jets can be related to instability patterns, as mentioned in Sect. 4.2, or may result from recollimation mechanisms. In the purely hydrodynamic case, recollimations naturally occur when the expanding flow becomes underpressurized compared to the medium (Daly & Marscher 1988). In MHD flows, collimation features can also appear when the jet ceases to be strongly magnetized and causally connected to the central engine (Meier 2012). The transition to the new regime is possibly accompanied by a saturation of the acceleration, which is nevertheless not observed in this region. Kinematic VLBI studies at lower frequencies (Bach et al. 2003, and references therein) have shown that the acceleration in the main jet extends at least to $\sim 5$ mas, where another prominent narrowing appears (Krichbaum et al. 1998). The nature of this collimation feature is ultimately not clear. It is interesting, though, that the narrowing is not present if we look at the model-fit widths (Fig. 7). In other words, the larger beam used in the model-fit analysis does not “see” the feature, indicating that whatever process is taking place, it must involve the flow on smaller scales.

5.4. Collimation regime
Theoretical models and simulations describing the conversion from Poynting flux to kinetic flux in magnetically driven jets have shown that the characteristics of the external medium represent a fundamental parameter (Komissarov et al. 2007; Tchekhovskoy et al. 2008; Lyubarsky 2009). Specifically, the gradient of the external pressure along the jet largely determines the shape of the jet and the acceleration rate, which are intimately connected. In an analytical study of the asymptotic structure of magnetically driven flows, Lyubarsky (2009) predicts the existence of two main regimes. In the first, the equilibrium regime, the pressure of the external medium $p$ decreases slowly as $p \propto z^{-\beta}$ with $\beta < 2$. In these conditions the magnetic field in the flow succeeds in keeping a strong poloidal component. The jet radius $r$ as a function of distance from the core is then given by a power law with index smaller than 0.5, the Lorentz factor increases as the radius ($\Gamma \propto r$), and the asymptotic shape of the jet is cylindrical. If the pressure gradient is steeper with index $k > 2$, the poloidal magnetic field becomes negligible, while the toroidal component cannot provide strong confinement to the flow, which then gets broader, accelerates more slowly ($\Gamma \propto z^{-1}$), and eventually reaches a conical shape. This is the non-equilibrium regime. The transition state between the two regimes occurs for $k = 2$. In this case, the asymptotic behavior of the flow is determined by the intensity of the magnetic field $B_0$ and by the external pressure $p_0$ at the base of the flow. Specifically, if the ratio $(6\pi p_0)/B_0^2$ is greater than 0.25, the flow has characteristics similar to the first regime and has a perfectly parabolic shape, i.e. with a radius $r$ increasing as $z^{\beta_1}$. A smaller ratio instead leads the flow to a state similar to the second regime.

In the following, we show that Cygnus A resembles the properties expected in the transition state ($p \propto z^{-2}$) and that the asymptotic regime is that of equilibrium. We now consider the shape of the jet. Because of the higher S/N, we focus our analysis on the approaching side. To reduce the impact of small scale

Fig. 7. Jet aperture versus core separation in November 2009 from the double ridge line analysis (magenta) and from a single Gaussian fit (green). Overplotted in blue are the sizes of the model-fit components from all epochs. Component J2 occupies only a portion of the jet in the transverse direction. To more clearly show the expansion, the $x$ and $y$ axes have different scales.
oscillations and to study the overall expansion of the jet, we consider the modelfit sizes in the four epochs up to the narrowing at ~2 mas. We exclude component J2 because, as shown in Fig. 7, this is clearly a feature occupying, transversally, only a portion of the jet. Results are shown in Fig. 8. The expansion can be described by a single power law of the form \( r \propto z^{0.55 \pm 0.07} \) up to \( \sim 10^4 R_S \); i.e., the jet has a parabolic shape. Two elements suggest that the flow collimates in the equilibrium regime. First, the Lorentz factor gradient of the fast component calculated in Sect. 5.1 (\( \Gamma \approx 0.50^{+0.19}_{-0.18} \)) is compatible with the prediction that \( \Gamma \) grows as \( r \), at least in the central body of the jet. Second, VLBI studies at 5 GHz (Carilli et al. 1991) have shown that the jet has a cylindrical shape between 4 and 20 mas, which is the asymptotic state in the equilibrium regime. Interestingly, 4–5 mas (\( \sim 2.5 \times 10^4 R_S \)) is also the maximum scale on which acceleration has been observed in this source (Bach et al. 2003) and where a second, prominent recollimation occurs (Krichbaum et al. 1998). Therefore this location can be identified as a good candidate for a region where the jet of Cygnus A ceases to be strongly magnetized and becomes causally disconnected from the central engine.

5.5. Comparison with M87

In the previous section we have shown that the prototypical FRII radio galaxy Cygnus A is collimated and accelerated on a scale of \( \sim 2.5 \times 10^5 R_S \), with the jet being parabolic in this region and cylindrical farther downstream. It is interesting to compare these properties with those inferred for M87, the most studied FRI object. Asada & Nakamura (2012) have shown that the jet of M87 is also parabolic up to a scale of \( \sim 10^5 R_S \) with \( r \propto z^{0.59} \) thus with a power law index very close to the one we measure for Cygnus A. However, after the HST-1 feature, the jet becomes conical rather than cylindrical, as expected in the non-equilibrium regime. An important difference between the equilibrium and non-equilibrium regimes resides in the efficiency of conversion of Poynting flux. While in the former case the Poynting flux will mostly be converted into kinetic flux, until equipartition is reached, a jet in non-equilibrium will remain magnetized up to large distances without reaching very high Lorentz factors. The high-power, thin jets of the FRI sources and the lower power, broader jets of the FRIs appear to fit well into the two categories, indicating that the FRI/FRII dichotomy might result from different environmental conditions. The discovery of sources with hybrid morphologies (Gopal-Krishna & Wiita 2002), the so-called HYMORS, supports the same scenario.

5.6. Nature of the gap in emission

Finally, we comment on the nature of the sharp gap in the emission situated at \( \sim 0.2 \) mas east of component N and of \( \sim 0.1 \) mas in size. Figure 7 shows that, although the zero in the x axis is set to coincide with the location of component N, this is not the narrowest region of the jet. Instead, both jet and counter-jet appear to emanate exactly from that gap, which features the absolute minimum width. It is then likely that the gap marks the true location of the central engine, which would then be located \( \sim 800 R_S \) upstream of the jet base, represented by component N.

Given the amount of evidence that the jet is magnetically driven, it is interesting to wonder how the jet would appear when it is still completely magnetically dominated, i.e. with a magnetization parameter much larger than 1. Owing to the very low speed the flow would have, it would also be faint and may appear as a gap. Other explanations are of course possible. The gap could alternatively be the effect of strong absorption by a molecular torus, which is certainly present and obscures part of the counter-jet (Struve & Conway 2010). Another possibility is that this is simply a self-absorbed region. A detailed spectral analysis using higher frequency data is required and in progress.

6. Conclusions

We performed a high resolution VLBI study at 7 mm of the kinematic properties and transverse structure of the two-sided jet in Cygnus A. Results can be summarized as follows.

- We detected an acceleration of the flow up to superluminal speeds (\( \beta_{\text{app}} = 1.15 \pm 0.04 \)) in the first parsec of the jet. The outer jet exhibits lower speeds, in agreement with studies at lower frequencies. We suggested that a fast and a slow component exist in the flow and interpret the slower speeds in the outer jet as an effect of the deboosting of the fast component, naturally occurring at a large viewing angle.
- The acceleration region of both the fast and slow components is extended (\( \sim 10^2–10^3 R_S \)), as characteristically predicted for magnetically driven outflows.
- Both the jet and counter-jet are limb-brightened. In the presence of a transverse gradient of the bulk Lorentz factor, the limb brightening is evidence of a spine-sheath structure of the jet, because any fast flow appears faint at a large viewing angle.
- The mean opening angles in the two sides are large (the full angle in the jet is \( \sim 10^\circ \)) compared to typical values inferred for blazars (\( 1^\circ–2^\circ \)). This can be explained by the possibility, in radio galaxies, of observing not only the thin inner spine but also the outer sheath.
- The shape of the flow is parabolic (\( r \propto z^{0.55 \pm 0.07} \)). The acceleration gradients and the collimation regime can be reproduced well by assuming an external pressure \( p \) that scales with distance from the central engine \( z \) as \( p \propto z^{-2} \), and the ratio (\( \sigma z r_{\text{app}}^2 \))/\( B^2 \) is larger than 0.25 at the base of the flow, as described in Lyubarsky (2009).
- The jet possibly stops being strongly magnetized on a scale of \( \sim 2.5 \times 10^5 R_S \), where it enters the asymptotic cylindrical shape (Carilli et al. 1991), the bulk of the acceleration saturates (Bach et al. 2003), and a recollimation occurs (Krichbaum et al. 1998).
Acknowledgements. B.B. is a member of the International Max Planck Research School (IMPRS) for Astronomy and Astrophysics at the Universities of Bonn and Cologne. B.B. thanks Andrei Lobanov for substantially triggering the ideas of this paper, and Richard Porcas for reading the manuscript and for his constant help. The author is also grateful to Vassilis Karamanavis, Gabriele Bruni, Tuomas Savolainen, Manel Perucho, and Robert Laing for stimulating discussions. E.R. acknowledges partial support by the MINECO grant AYA-2012-38491-C02-01 and Generalitat Valenciana grant PROMETEOII/2014/057. The European VLBI Network is a joint facility of European, Chinese, South African, and other radio astronomy institutes funded by their national research councils. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc.

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