

# Induced rotational excitation of the fluoromethylidyne $^{12}\text{CF}^+$ and $^{13}\text{CF}^+$ through collision with helium

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## ABSTRACT

**Aims.** The present paper focuses on the calculation of the collision rate coefficients for rotational excitation of the  $^{12}\text{CF}^+$  and its isotopologue  $^{13}\text{CF}^+$  by He for temperature ranging from 10 to 300 K.

**Methods.** A two-dimensional (2D) potential energy surface (PES) of the  $\text{CF}^+(\text{X}^1\Sigma^+)-\text{He}(^1\text{S})$  system is calculated at the ab initio coupled cluster with single, double, and perturbative triple excitation level of theory with the aug-cc-pV5Z basis set. The basis set superposition errors were taken into account in our computation. Dynamical calculations of state-to-state rotational integral cross sections of the  $\text{CF}^+$  by collision with He were performed using the close-coupling method.

**Results.** The PES presents a global minimum of  $\sim 212\text{ cm}^{-1}$  below the  $\text{CF}^+-\text{He}$  dissociation limit. Collisional cross sections among the first 11 rotational levels of  $\text{CF}^+$  were calculated for total energies up to  $1500\text{ cm}^{-1}$ . Downward rate coefficients between the rotational levels were calculated for temperature ranging from 10 to 300 K. A propensity toward an even parity of  $\Delta J$  is observed.

**Key words.** molecular data – molecular processes – ISM: molecules

## 1. Introduction

It was reported that the *Herschel*, *SOFIA*, and *ALMA* observatories gave high spectral resolution observations on molecular emission in the submillimeter and far-infrared domains. These observations, supplemented by molecular modeling, are powerful tools to investigate the physical and chemical conditions of astrophysical objects. Most of these observations require accurate knowledge about collisional processes that occur in the interstellar medium (ISM). To achieve the best precision required in astrophysics, a fully quantum mechanical treatment of the collision dynamics is recommended, in addition to experimental investigations. Many experimental and theoretical studies of the collision-inducing rotational energy transfer have been performed in the last four decades. Particularly, the collisional rate coefficients with the most abundant interstellar species, H,  $\text{H}_2$ , and He, have been shown to be of great astrophysical importance (Wernli et al. 2006; Kłos et al. 2007; Lique & Spielfiedel 2007; Guillon et al. 2008; Buffa et al. 2009; Lique et al. 2009, 2010; Dubernet et al. 2009; Najjar et al. 2009; Sarrasin et al. 2010).

The significant abundance of  $\text{H}_2$  in the ISM implies that this molecule is the primary collision partner for any other species. The major gas component in ISM,  $\text{H}_2(j=0)$ , is electronically equivalent to the He atom. Astronomers usually estimated the rate coefficients for the collisions with para- $\text{H}_2(j=0)$  from those obtained by collision with He (Schöier et al. 2005). The studies reported by Wernli et al. (2006), Lique et al. (2008), and Dumouchel et al. (2010) indicated that the use of the scaled factor of 1.4 to deduce the rate coefficients of the collision with para- $\text{H}_2(j=0)$  from those corresponding to the collision with He provides the correct magnitude order. This was shown to be

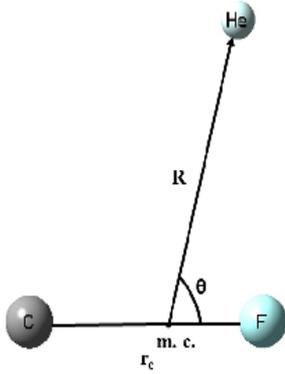
unlikely for charged species. For instance, for the  $\text{HCO}^+$  system, the last approximation can be used to estimate the collisional rates with  $\text{H}_2$  from those with He, but the factor scaling will be between 2 and 4 (Monteiro 1985).

The results of the study on the chemistry of fluorine, which was reported by Neufeld et al. (2005), predicted that  $\text{CF}^+$  ion is the second most abundant fluorine-bearing molecule in the ISM after HF; its formation from the reaction of HF with  $\text{C}^+$  (the dominant reservoir of gas-phase carbon) follows these two equations:



The first detection of  $\text{CF}^+$  in the photo-dissociation regions (PDR) was toward the Orion Bar (Neufeld et al. 2006), showing spatially extended emission in the 1–0, 2–1, and 3–2 rotational transitions. The observations of Nagy et al. (2012) extended the observed  $\text{CF}^+$  transitions in this region up to the 5–4 transition and the line intensity is consistent with the previously observed transitions.

The C-containing species were also demonstrated to be of great astrophysical significance because they may provide information on the  $^{13}\text{C}/^{12}\text{C}$  ratio. To improve the knowledge on the fluorine interstellar chemistry, Cazzoli et al. (2010) recorded accurate rest frequencies for future radioastronomical observations. In their studies, they improved the accuracy of the  $\text{CF}^+$  spectroscopic parameters available in the literature. They also provided the spectroscopic parameters of  $^{13}\text{CF}^+$  for the first time. Recently, they extended their previous work using THz measurements to provide accurate and reliable higher frequencies



**Fig. 1.** Definition of the body-fixed Jacobi coordinates system for the  $\text{CF}^+\text{-He}$  complex.

(Cazzoli et al. 2012). Their measurements enabled the prediction of rotational transitions with a good accuracy, up to 2.0–2.5 THz.

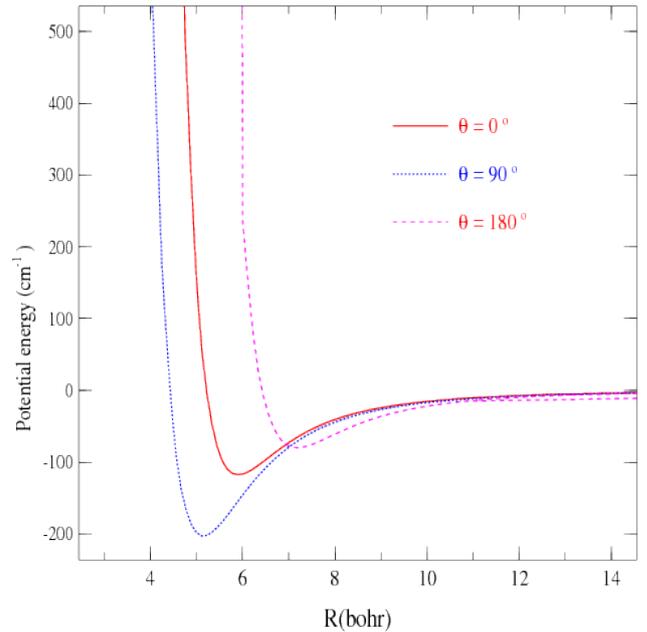
From a spectroscopic point of view, the most recent studies of  $\text{CF}^+$  did not consider the hyperfine structure because the experiments were not able to resolve the hyperfine components (Cazzoli et al. 2010). Recently, Guzmán et al. (2012a) detected the  $J = 1-0$  and  $J = 2-1$  rotational lines of  $\text{CF}^+$  with a high signal-to-noise ratio toward the PDR and core positions in the Horsehead. In contrast to other mm lines in the Horsehead, the  $\text{CF}^+ J = 1-0$  (102.587 GHz) line is double-peaked. They applied a high-level quantum chemical calculation to determine the hyperfine splitting and pointed out a constant of  $7.6 \times 10^{-6} \text{ cm}^{-1}$  as a value for the fluorine spin rotation (Guzmán et al. 2012b). This low computed value of the spin rotation constant confirmed the nonobservations of the hyperfine splitting in the experiments performed by Cazzoli et al. (2010).

In the present work, we focus on the study of the rotational (de-)excitation rate coefficients of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  by collision with He using quantum mechanical calculations. A new accurate ab initio two-dimensional potential energy surface (PES) is provided. The computation of pure rotational cross sections is performed using the close-coupling (CC) method for rotational levels below  $J = 10$  and for total energy up to  $1500 \text{ cm}^{-1}$ . The collisional rate coefficients are obtained by averaging these cross sections over a Maxwell-Boltzmann velocity distribution at low temperatures ranging from 10 to 300 K. In our calculations, the hyperfine structure is neglected.

This paper is organized as follows: Sect. 2 describes the ab initio calculations of the PES. The dynamical calculation results are presented and discussed in Sect. 3. A comparison between  $^{12}\text{CF}^+\text{-He}$  and  $^{13}\text{CF}^+\text{-He}$  collisional data is included in the last subsection. Concluding remarks are given in Sect. 4.

## 2. Potential energy surface

In this work the vibrational excitation is expected to be negligible because we are interested in studying low-temperature collisions. As a consequence, the collision partners may be considered as rigid. To perform our calculations, we describe the van der Waals  $\text{CF}^+\text{-He}$  system by Jacobi coordinates  $(r, R, \theta)$ . As shown in Fig. 1,  $r$  is the internuclear distance of  $\text{CF}^+$  frozen at its experimental equilibrium geometry  $r = r_e = 2.1812 \text{ bohr}$  (Kawaguchi & Hirota 1985),  $R$  is the distance between the He atom and the mass center (m.c.) of  $\text{CF}^+$ , and  $\theta$  is the angle between the two distance vectors. The collinear  $\text{CF}^+\text{-He}$  corresponds to  $\theta = 0^\circ$ .



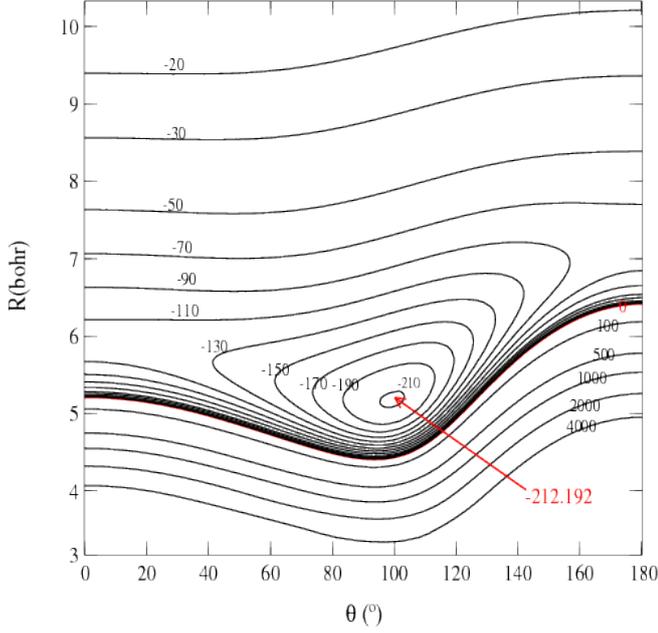
**Fig. 2.** Cuts of the PES for angle values  $\theta = 0^\circ$ ,  $\theta = 90^\circ$ , and  $\theta = 180^\circ$  as a function of the distance  $R$ .

The interaction energy of the  $\text{CF}^+\text{-He}$  system is calculated using the coupled cluster with single, double, and perturbative triple excitation (CCSD(T)) method (Hampel et al. 1992) as it is implemented in the MOLPRO molecular package (Werner et al. 2002) in connection with the aug-cc-pV5Z basis set of Dunning (1989). The use of the monoconfigurational CCSD(T) approach is verified because the weight of the dominant configuration ( $1a^22a'^23a'^24a'^25a'^21a'^26a'^27a'^2$ ) for the ground state is greater than 0.96 for all orientations. The basis set superposition errors (BSSE) were corrected in all geometries using the Boys & Bernardi (1970) counterpoise procedure. The distance  $R$  was varied by step of 0.25 bohr between 3 and 15 bohr and then by step of 1 bohr between 15 and 25 bohr. The value of  $\theta$  was varied from 0 to  $180^\circ$  with a uniform step size of  $15^\circ$ . The PES was constructed with 767 ab initio geometries treated in the  $C_s$  symmetry group.

In Fig. 2 we represented three cuts of the PES, which are  $V(r_e, R_{\text{CF}^+\dots\text{He}}, \theta = 0^\circ)$ ,  $V(r_e, R_{\text{CF}^+\perp\text{He}}, \theta = 90^\circ)$ , and  $V(r_e, R_{\text{He}\dots\text{CF}^+}, \theta = 180^\circ)$ , where  $R_{\text{CF}^+\dots\text{He}}$  is the value of  $R$  for an approach of He towards F atom and  $R_{\text{He}\dots\text{CF}^+}$  is that for He towards C atom. For  $\theta = 0^\circ$  the minimum is located at  $R_{\text{CF}^+\dots\text{He}} \sim 6 \text{ bohr}$  with a depth well of  $-116.55 \text{ cm}^{-1}$ ; for  $\theta = 90^\circ$  the minimum is at  $R_{\text{CF}^+\perp\text{He}} \sim 5.25 \text{ bohr}$  with a depth of  $-201.099 \text{ cm}^{-1}$ , and for  $\theta = 180^\circ$  it is found to be  $-79.55 \text{ cm}^{-1}$  at  $R_{\text{He}\dots\text{CF}^+} \sim 7.25 \text{ bohr}$ . Thus, the global minimum is placed near the perpendicular position. The He approach on the F side leads to a deeper minimum than on the C side. In fact, the electronic cloud of the  $\text{CF}^+$  molecule is shifted to the fluorine atom as it is more electronegative than that of carbon. Figure 3 displays the contours plot of this potential. The interaction energy has a global minimum of  $-212.192 \text{ cm}^{-1}$  at  $R = 5.17 \text{ bohr}$  and  $\theta = 99.4^\circ$ .

We are interested in comparing our PES with that of  $\text{CH}^+\text{-He}$  system studied by Hammami et al. (2008a). This comparison is based on three aspects:

1. The interaction of two ions ( $\text{CF}^+$  and  $\text{CH}^+$ , which both have the carbon atom in common) by collision with the He atom.



**Fig. 3.** Contour plot of the PES (in  $\text{cm}^{-1}$ ) of  $\text{CF}^+(\text{X}^1 \Sigma^+)-\text{He}(1\text{S})$  as a function of  $R$  and  $\theta$  ( $r_e = 2.1812$  bohr). The zero of energy is taken as that of the  $\text{CF}^+-\text{He}$  asymptote.

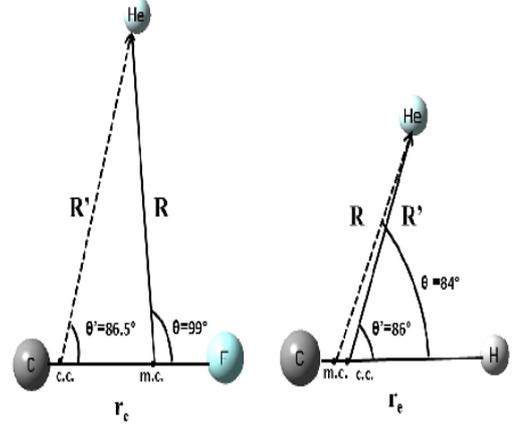
**Table 1.** Distribution of positive charge on the  $\text{CF}^+$  and  $\text{CH}^+$  molecules.

Molecule	$\text{CF}^+$		$\text{CH}^+$	
Atom	C	F	C	H
Charge	0.90116	0.09884	0.85684	0.14316

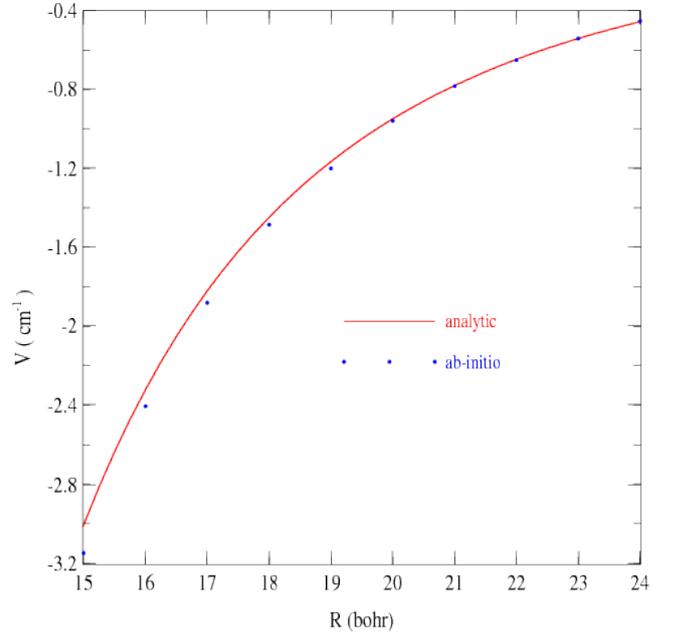
- The repartition of the positive charge in  $\text{CF}^+$  and  $\text{CH}^+$  molecules is concentrated on the carbon atom.
- The shapes of  $\text{CF}^+-\text{He}$  and  $\text{CH}^+-\text{He}$  PESs are very similar.

Indeed, more than 85% of the positive charge for both ions is almost concentrated on the carbon atom (see Table 1). Moreover, the  $\text{CH}^+-\text{He}$  PES owns a minimum of  $537 \text{ cm}^{-1}$  at the position of  $R = 4.05$  bohr and  $\theta = 84^\circ$  (Hammami et al. 2008a), which is a very similar minimum position to that of  $\text{CF}^+-\text{He}$ . To compare these minimum positions, we represent in Fig. 4 the Jacobi coordinates referring to the mass center ( $R, \theta$ ) and the charge center ( $R', \theta'$ ) of  $\text{CF}^+-\text{He}$  (left-hand panel) and  $\text{CH}^+-\text{He}$  (right-hand panel) van der Waals systems at their global minimum positions. Here,  $r_e$  is the internuclear distance of  $\text{CF}^+$  and  $\text{CH}^+$  fixed at their equilibrium values of the ground state,  $r_e(\text{CF}^+) = 2.1812$  bohr, and  $r_e(\text{CH}^+) = 2.1371$  bohr. From this figure, one can clearly see that both minima occur at a very similar Jacobi angle ( $\theta'(\text{CF}^+-\text{He}) = 86,5^\circ$  and  $\theta'(\text{CH}^+-\text{He}) = 86^\circ$ ) if we refer to the molecules' charge centers. Not surprisingly the  $R'$  coordinates are in the order  $R'_{\text{CF}^+-\text{He}} > R'_{\text{CH}^+-\text{He}}$ ; this stems from the fact that  $\text{CH}^+$  much strongly attracts the atom He than does  $\text{CF}^+$ . This behavior is also observed when comparing the well depths of the two PES. In fact, the  $\text{CH}^+-\text{He}$  potential well is deeper than the  $\text{CF}^+-\text{He}$  one.

In the framework of the long-range approximation, the energy contribution to the interaction between the  $\text{CF}^+$  molecule with a permanent dipole moment  $\mu_{\text{CF}^+}$  and the apolar He atom



**Fig. 4.** Jacobi coordinates for the  $\text{CF}^+-\text{He}$  and  $\text{CH}^+-\text{He}$  systems at the global minimum positions m.c. and c.c. are, respectively, the mass and charge center of the diatomic molecules.



**Fig. 5.** Comparison between the long range ab initio and analytical potential energies for  $\theta = 90^\circ$ .

with a polarisability  $\alpha_{\text{He}} = 1.38$  D is reduced to the induction part, which is expressed as

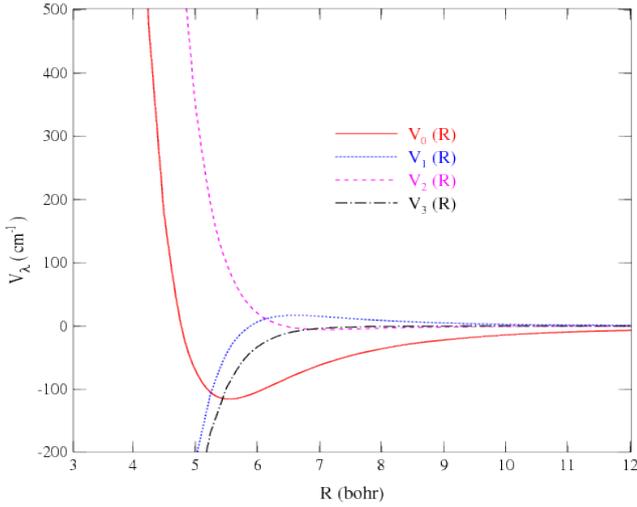
$$U_{\text{ind}}(R, \theta) = -\frac{1}{2} \frac{\alpha}{(4\pi\epsilon_0)^2} \left( \frac{e^2}{R^4} + \frac{2\mu^2}{R^6} \right) - \frac{2e\mu\alpha}{R^5(4\pi\epsilon_0)^2} \cos(\theta) - \frac{\alpha\mu^2}{2R^6(4\pi\epsilon_0)^2} (3 \cos^2(\theta) - 1) + \dots \quad (3)$$

The long-range part of our potential was studied by comparing the ab initio PES with the analytical expression (Eq. (3)). For  $\theta = 90^\circ$  this expression is reduced to

$$U_{\text{ind}}(R, \theta = 90^\circ) = -\frac{\alpha}{2R^4}. \quad (4)$$

Figure 5 depicts the variation of the long-range ab initio and analytical potential energies for  $\theta = 90^\circ$ , showing a good agreement between the two sets of data.

Before starting dynamical calculations, an analytic expansion of the PES is required as input for MOLSCAT package



**Fig. 6.**  $V_\lambda$  expansions of the interaction PES ( $\lambda = 0, 1, 2, 3$ ) as a function of the Jacobi coordinate  $R$ .

(Hutson et al. 1994). Thus, our PES is expanding in terms of Legendre polynomials and is expressed as

$$V(r = r_e, R, \theta) = \sum_{\lambda=0}^{\lambda_{\max}} V_\lambda(R) P_\lambda(\cos \theta). \quad (5)$$

From an ab initio grid containing 13 values of  $\theta$ , we were able to include terms up to  $\lambda_{\max} = 12$ . To test the potential expansion, we started from the 13 values of  $\theta$  for each radial distance  $R$  and deduced 19 ones using the cubic spline subroutine. These values were then fitted with the same procedure using 19 terms of  $V_\lambda(R)$ . The dependence on  $R$  of the dominant coefficients  $V_\lambda(R)$  are showed in Fig. 6. Over the entire grid, the mean relative difference between the fitted and ab initio data is lower than 1% (see Table 2).

From all the foregoing results, we deduced that the collisional calculations may be carried out for  $R$  starting from 3 bohr, which provides sufficiently repulsive potential for all orientations. During the scattering calculations, an interpolation was performed to obtain  $V_\lambda(R)$  at other values of  $R$  using the POTENL routine implemented in the MOLSCAT program. For large distances  $R > 25$  bohr, this routine extrapolates  $V_\lambda(R)$  parameters by an inverse exponent expansion such as

$$V_\lambda(R) = \frac{C_\lambda}{R^m}. \quad (6)$$

It takes into account the latest values of  $V_\lambda(R)$  to obtain the  $C_\lambda$  and  $\eta_\lambda$  coefficients for each  $\lambda$  value. It gives, for example,  $\eta_{(\lambda=0)} = 4.14$ ,  $\eta_{(\lambda=1)} = 5.12$ , and  $\eta_{(\lambda=2)} = 6.19$ . These values are in good agreement with the expression of the long-range potential given in Eq. (3).

### 3. Dynamical calculations

#### 3.1. Cross sections

In this work, we are interested in studying the rotational excitation of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  by collision with He at low temperature ( $T \leq 300$  K) for values of  $J$  ranging from 0 to 10 and a total energy up to  $1500 \text{ cm}^{-1}$ , where  $J$  denotes the rotational angular momentum of the  $\text{CF}^+$  molecule. The rotational levels of

**Table 2.** Potential energies obtained from ab initio calculations and the corresponding fitted values obtained from the  $V_\lambda$  coefficients.

$\theta$ ( $^\circ$ )	$R$ (bohr)	Ab initio potential energy ( $\text{cm}^{-1}$ )	Potential energy ( $\lambda_{\max} = 12$ ) ( $\text{cm}^{-1}$ )	Potential energy ( $\lambda_{\max} = 18$ ) ( $\text{cm}^{-1}$ )
20	4	4054.680	4055.760	4055.752
	5	97.640	97.790	97.827
	7	-72.051	-72.007	-72.005
	10	-15.204	-15.300	-15.302
50	4	1934.968	1936.702	1935.406
	5	-63.556	-63.349	-63.331
	7	-70.219	-70.195	-70.195
	10	-15.308	-15.430	-15.431
100	4	656.051	652.360	654.926
	5	-204.923	-205.221	-205.221
	7	-84.609	-84.694	-84.686
	10	-17.877	-17.751	-17.748
160	4	18 672.380	18 671.181	18 725.889
	5	2519.388	2519.114	2522.812
	7	-87.513	-87.349	-87.321
	10	-21.762	-21.731	-21.732

**Table 3.** MOLSCAT parameters used in our calculations.

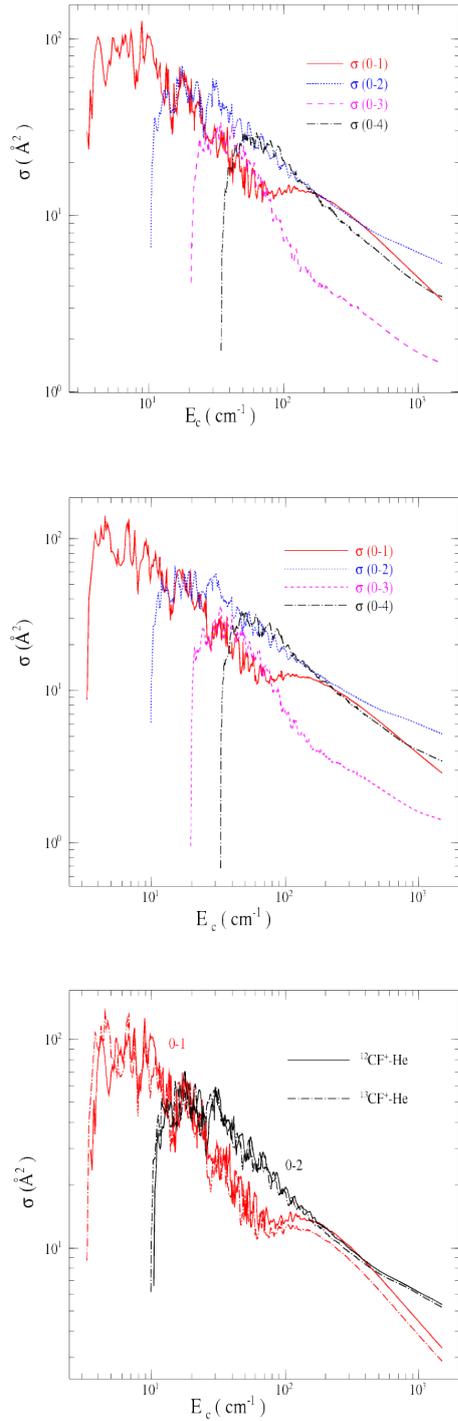
$B_e(^{12}\text{CF}^+) = 1.72 \text{ cm}^{-1a}$	$D_e(^{12}\text{CF}^+) = 6.18 \times 10^{-6} \text{ cm}^{-1a}$	$R_{\min} = 3 \text{ bohr}$
$B_e(^{13}\text{CF}^+) = 1.64 \text{ cm}^{-1b}$	$D_e(^{13}\text{CF}^+) = 5.70 \times 10^{-6} \text{ cm}^{-1b}$	$R_{\max} = 30 \text{ bohr}$
$\mu(^{12}\text{CF}^+ - \text{He}) = 3.5449 \text{ UA}$	$\mu(^{13}\text{CF}^+ - \text{He}) = 3.5576 \text{ UA}$	DTOL = 0.01
$J_{\max} = 15, 17, 20$	STEPS = 40, 20, 10	OTOL = 0.001

**Notes.** <sup>(a)</sup> Kawaguchi & Hirota (1985). <sup>(b)</sup> Cazzoli et al. (2010).

$\text{CF}^+$  may be computed with the usual expansion using the spectroscopic constants  $B_e$  and  $D_e$  reported in Table 3. To calculate the cross sections, we use the quantum mechanical CC approach of Arthurs & Dalgarno (1960) implemented in the MOLSCAT code. To account for resonances during the calculation, we carefully spanned the energy range as follows: for  $E < 100 \text{ cm}^{-1}$  the energy step was set to  $0.1 \text{ cm}^{-1}$ ; for  $100 \text{ cm}^{-1} \leq E < 200 \text{ cm}^{-1}$  to  $0.2 \text{ cm}^{-1}$ ; for  $200 \text{ cm}^{-1} \leq E < 500 \text{ cm}^{-1}$  to  $1 \text{ cm}^{-1}$ ; for  $500 \text{ cm}^{-1} \leq E < 1000 \text{ cm}^{-1}$  to  $5 \text{ cm}^{-1}$ , and for  $1000 \text{ cm}^{-1} \leq E \leq 1500 \text{ cm}^{-1}$  to  $10 \text{ cm}^{-1}$ . In addition, we set  $J_{\max} = 15$  for  $E < 200 \text{ cm}^{-1}$ ,  $J_{\max} = 17$  for  $200 \text{ cm}^{-1} \leq E < 500 \text{ cm}^{-1}$ , and  $J_{\max} = 20$  for  $E \geq 500 \text{ cm}^{-1}$ . These values were fixed after performing some convergence tests. The maximum value of the total angular momentum  $J_{\text{tot}}$  was set large enough to ensure the convergence of the cross sections to be within  $0.01 \text{ \AA}^2$  for elastic transitions and  $0.001 \text{ \AA}^2$  for inelastic ones; typically, at  $100 \text{ cm}^{-1}$ ,  $J_{\text{tot}} = 63$ , at  $500 \text{ cm}^{-1}$ ,  $J_{\text{tot}} = 133$ , at  $1000 \text{ cm}^{-1}$ ,  $J_{\text{tot}} = 175$ , and at  $1500 \text{ cm}^{-1}$ ,  $J_{\text{tot}} = 203$ . The coupled equations were solved using the propagator of Manolopoulos (1986).

Dynamical calculations for the  $^{13}\text{CF}^+ - \text{He}$  system were performed at the same levels of theory using the  $^{12}\text{CF}^+$  PES, taking into account the displacement of the mass center with the change of the reduced mass and the spectroscopic constant  $B_e$  and  $D_e$ .

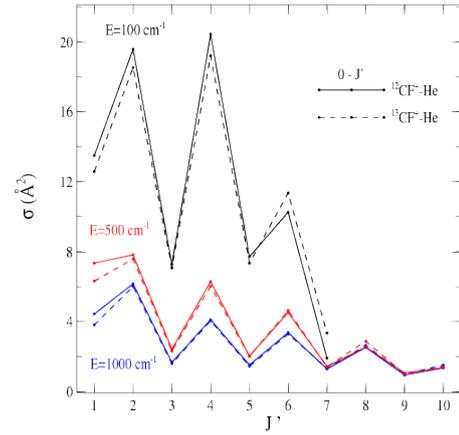
Figure 7 presents the collisional excitation cross sections of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  by He as a function of the kinetic energy for transitions from the ground level ( $J = 0$ ) to  $J' = 1-4$  rotational levels. As one can see, the cross sections present several resonances (shape and Feshbach), particularly at low kinetic energies. This typical behavior for cross sections was pointed out by different studies (Smith et al. 1979; Christoffel & Bowman 1983; Lique et al. 2007; Hammami et al. 2008a,b,c; Nkem et al. 2009). These resonances are precisely detected in our calculated cross



**Fig. 7.** Collision excitation cross sections of  $^{12}\text{CF}^+$  (upper panel) and  $^{13}\text{CF}^+$  (middle panel) by He as a function of the kinetic energy for transitions  $0-J'$  with  $J' = 1-4$ . The comparison is given in the lower panel.

sections. This can be attributed to the small value of the rotational constant  $B_c$  in comparison to that employed in the studies cited above. At high energy, we note the disappearance of these resonances: they do not exist for transitions involving energy levels with high  $\Delta J$ . The fine energy grid used at low energies was necessary for a good description of these resonances.

For propensity rules, we note that the  $0-1$  transition is dominant only at very low energies, i.e., from 0 to  $15 \text{ cm}^{-1}$ . It should be noticed that a strong propensity towards an even parity of  $\Delta J$



**Fig. 8.** Collisional excitation cross sections of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  by He as a function of  $J'$  for selected collision energies.

transitions is also observed for almost the entire range of energies. The same rules were found for the  $\text{CH}^+$ -He system. To compare the cross sections of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  by collision with He, we represented them in Fig. 7 (lower panel) as a function of kinetic energy for  $0-1$  and  $0-2$  transitions. This figure shows clearly that the cross sections exhibit almost the same trends for both systems, with a slight change due to the reduced mass and rotational constant difference between both isotopes. Figure 8 displays the dependance of cross sections on the rotational levels  $J'$  from the ground state ( $J = 0$ ) for both systems and for selected energies  $E = 100, 500, \text{ and } 1000 \text{ cm}^{-1}$ . From this figure, we deduced that the general trends discussed above remain valid.

### 3.2. Collision rate coefficients

The rate coefficients are obtained by averaging the cross sections over a Maxwell-Boltzmann distribution of kinetic energies expressed as

$$\tau_{J-J'}(T) = \left( \frac{8}{\pi\mu\beta} \right)^{\frac{1}{2}} \beta^2 \int_0^{\infty} E_c \sigma_{J-J'}(E_c) e^{-\beta E_c} dE_c. \quad (7)$$

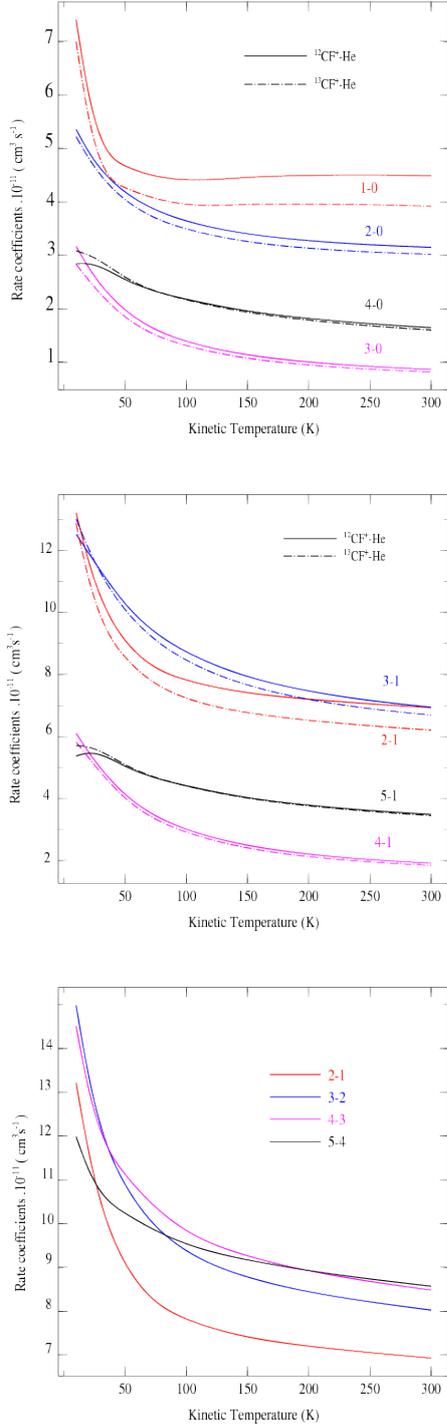
$\beta = \frac{1}{k_B T}$ , where  $k_B$  is the Boltzmann constant and  $T$  is the kinetic temperature,  $E_c$  is the relative kinetic energy (which is the difference between the total ( $E$ ) and rotational ( $E_J$ ) energies), and  $\mu$  is the reduced mass (its values for  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He systems are given in Table 3).

The downward rate coefficients for  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  by collision with He for  $J$  ranging from 0 to 10 at selected temperatures will be reported online at the BASECOL<sup>1</sup> (Dubernet et al. 2013) and LAMDA<sup>2</sup> (Schöier et al. 2005) data bases.

We displayed in Fig. 9 the collision rates of  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He as a function of the temperature. All curves in this figure are smoothly varying functions with the increase of kinetic temperature. There is a significant variation of rate coefficients at low temperatures. Figure 10 illustrates the variation of downward rate coefficients as a function of  $J$  for  $J-J'$  transitions with  $J' = 0$  (upper panel) and  $J' = 1$  (lower panel) for selected temperatures  $T = 20, 100, \text{ and } 300 \text{ K}$ . According to this figure, it is important to note that the rate of collision confirms the already

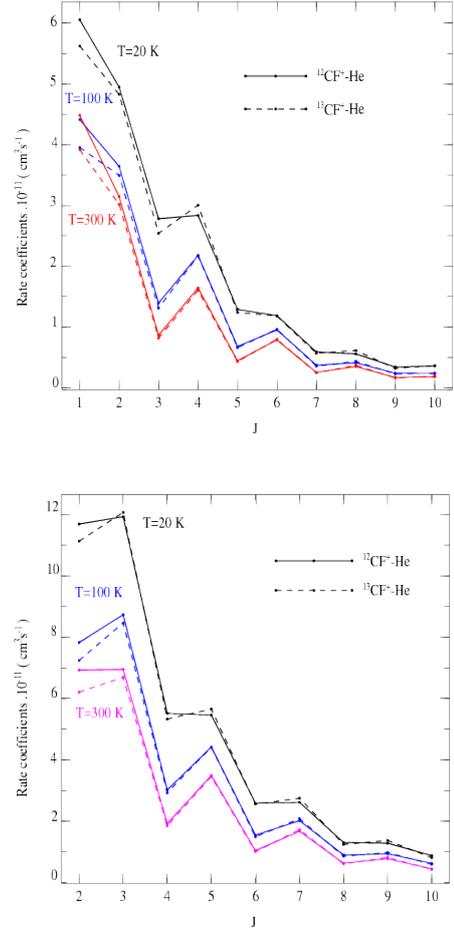
<sup>1</sup> <http://basecol.obspm.fr/>

<sup>2</sup> <http://www.strw.leidenuniv.nl/~moldata>



**Fig. 9.** Calculated downward rate coefficients as a function of kinetic temperature for the collision of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  with He for transitions  $J=0$  (upper panel) and  $J=1$  (middle panel), and for astronomical observed transitions for  $^{12}\text{CF}^+$  (lower panel).

noted propensity towards even parity of  $\Delta J$  transitions obtained with cross sections, except for 1–0 transition. In fact, the  $\text{CF}^+$ -He PES is practically symmetrical relative to  $\theta = 90^\circ$ , and the largest (in magnitude) of the anisotropic terms ( $\lambda > 0$ ) in the radial coefficients  $V_\lambda$  corresponds to  $\lambda = 2$ . Otherwise, as one can see from Table 4, the energy spacing between the ground state and the first rotational one is very small compared to the other ones. This may be the main effect that promotes 1–0 transition. This behavior confirms all the results discussed and concluded



**Fig. 10.** Calculated downward rate coefficients for the collisions of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  with He for  $J-J'$  transitions with  $J' = 0$  (upper panel) and  $J' = 1$  (lower panel) for selected kinetic temperature.

**Table 4.** Rotational levels of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  molecules.

Level	$J$	$^{12}\text{CF}^+$ Energy ( $\text{cm}^{-1}$ )	$^{13}\text{CF}^+$ Energy ( $\text{cm}^{-1}$ )
1	0	0.0000	0.0000
2	1	3.4407	3.2789
3	2	10.3221	9.8367
4	3	20.6439	19.6731
5	4	34.4055	32.7877
6	5	51.6064	49.1798
7	6	72.2459	68.8489
8	7	96.3230	91.7941
9	8	123.8367	118.0144
10	9	154.7859	147.5088
11	10	189.1692	180.2760

in cross sections indicated above. The even propensity rule was found to be similar to that obtained for the  $\text{CH}^+$ -He. This feature is due to the shape of  $\text{CH}^+$ -He PES, which is already similar to that obtained in our study.

### 3.3. Comparison between $^{12}\text{CF}^+$ and $^{13}\text{CF}^+$ collisional data

The Computation of collisional data for isotopologue species differs by the reduced mass, the rotational constants, and the position of the mass center. These effects significantly alter the data

**Table 5.** Comparison between  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He cross sections.

$J-J'$	$E = 100 \text{ cm}^{-1}$			$E = 500 \text{ cm}^{-1}$		
	$^{12}\text{CF}^{+a}$	$^{13}\text{CF}^{+b}$	$^{13}\text{CF}^{+c}$	$^{12}\text{CF}^{+a}$	$^{13}\text{CF}^{+b}$	$^{13}\text{CF}^{+c}$
1-0	13.497	13.950	12.584	7.342	7.370	6.317
2-0	19.584	18.900	18.528	7.819	7.784	7.581
0-1	4.659	4.807	4.337	2.464	2.472	2.119
2-1	12.754	12.485	11.500	5.926	5.950	5.204
3-1	21.101	20.504	20.297	7.502	7.452	7.209
5-0	7.706	7.510	7.339	2.032	2.028	2.009
7-0	1.916	3.380	3.349	1.431	1.408	1.408
0-5	1.447	1.343	1.313	0.206	0.204	0.202
1-5	8.722	8.630	8.643	1.688	1.677	1.660
4-5	17.359	15.706	15.227	4.620	4.618	4.12
0-7	3.474	2.747	2.721	0.118	0.115	0.114
1-7	16.285	11.914	12.529	0.894	0.886	0.938
5-7	87.532	53.921	52.993	4.887	4.830	4.824
6-7	45.576	36.979	36.588	5.024	5.030	4.472

**Notes.** The cross sections are in  $\text{\AA}^2$ . <sup>(a)</sup> Cross sections of  $^{12}\text{CF}^+$ -He system calculated with  $^{12}\text{CF}^+$ -He PES and  $^{12}\text{CF}^+$  rotational structure. <sup>(b)</sup> Cross sections of  $^{13}\text{CF}^+$ -He system calculated with  $^{12}\text{CF}^+$ -He PES and  $^{13}\text{CF}^+$  rotational structure. <sup>(c)</sup> Cross sections of  $^{13}\text{CF}^+$ -He system calculated with  $^{13}\text{CF}^+$ -He PES and  $^{13}\text{CF}^+$  rotational structure.

for the H/D substitutions, such as  $\text{H}_2/\text{D}_2$  (Flower & Roueff 1999; Flower 1999), NH/ND (Dumouchel et al. 2012),  $\text{H}_2\text{O}/\text{D}_2\text{O}$  (Faure et al. 2004, 2012), and  $\text{DCO}^+/\text{HCO}^+$  (Buffa 2012), but not for the  $^{12}\text{C}/^{13}\text{C}$ ,  $^{14}\text{N}/^{15}\text{N}$ , and  $^{16}\text{O}/^{18}\text{O}$  ones (Wickham-Jones et al. 1987; Yang et al. 1992; Reid et al. 1997). In the present work we have taken into account the displacement of the mass center in the calculation of the PES and used the  $^{13}\text{CF}^+$  rotational constant and its corresponding reduced mass. To show the influence of each effect on the collisional data, we calculated the  $\text{CF}^+$ -He cross sections using the  $^{12}\text{CF}^+$ -He PES with the  $^{12}\text{CF}^+$  rotational structure, the  $^{12}\text{CF}^+$ -He PES with the  $^{13}\text{CF}^+$  rotational structure, and the  $^{13}\text{CF}^+$ -He PES with the  $^{13}\text{CF}^+$  rotational structure. The results are presented in Table 5 for  $E = 100$  and  $500 \text{ cm}^{-1}$ . From Table 5, it can be seen that cross sections are very sensitive to the displacement of mass center and to the change of the rotational structure because the results obtained by the different sets of calculations differ significantly. In contrast, the cross sections calculated with the same rotational structure and two different PESs are increasingly close. This confirms that the displacement of mass center has an effect on collisional data. The latter, however, is not as important as the change of the rotational structure. Indeed, for most of the transitions the relative average error between the calculated cross sections using  $^{12}\text{CF}^+$ -He PES and two different rotational structures of  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  molecules ( $\sim 12\%$ ) is almost higher than those calculated with the same rotational structure of  $^{13}\text{CF}^+$  and two different  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He PESs ( $\sim 3.8\%$ ), mainly for transitions with high rotational levels  $J$ , when the energy spacings between the  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  rotational levels is large (see Table 4).

From this table it can be seen that the small spacing between  $^{12}\text{CF}^+$  and  $^{13}\text{CF}^+$  levels leads to a small difference in the cross section values and the rate coefficients ones. This behavior is clearly seen in Fig. 7 (lower panel), which shows the same intensity and trends detected for the energy variation of  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He cross sections. A good agreement between both isotopologues rate coefficients is observed in the two upper panels of Figs. 9 and 10. The slight difference obtained can be mainly due to the three effects cited above.

The  $^{13}\text{CF}^+$ -He rates are found to be slightly lower than those of  $^{12}\text{CF}^+$ -He. This may be due to the energy spacing between the rotational levels of each molecule affected by the difference of the rotational constants. Indeed, for a given energy and transition the  $E_c e^{-\beta E_c}$  factor in (Eq. (7)) is found to be weaker in the case of  $^{13}\text{CF}^+$ . Furthermore, the difference between  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He rate coefficients can be attributed to the small effect of the reduced mass values in the Boltzmann factors (Eq. (7)). From Figs. 8 and 10, one can see that the propensity rules are found to be identical for both isotopologues.

#### 4. Summary and conclusion

In the present study, a reliable ab initio PES for the  $\text{CF}^+$ -He complex is computed using the CCSD(T) method with the aug-cc-pV5Z basis set for all atoms. A comparison of our PES with that of Hammami et al. (2008a) is mentioned, e.g., the shape of the  $\text{CF}^+$ -He PES is found to be very similar to that of the  $\text{CH}^+$ -He system. The results of a quantum mechanical CC calculation of integral cross sections for transitions between the lower rotational levels of  $\text{CF}^+$  induced by collision with He are reported. For  $^{13}\text{CF}^+$ -He system, dynamical calculations were performed from a translation of  $^{12}\text{CF}^+$  mass center.

Up to  $T = 300 \text{ K}$ , downward rate coefficients were obtained by averaging the cross sections over a Maxwell-Boltzmann distribution of the kinetic energy. The comparison between the  $^{12}\text{CF}^+$ -He and  $^{13}\text{CF}^+$ -He collisional data indicates the same trends and a very close order of magnitude. The slight discrepancies between both sets of data are explained mainly by the difference in the rotational structure and the displacement of the associated potential interaction with He.

A strong propensity towards even  $\Delta J$  transition is observed for cross sections and rate coefficients. Similar conclusions were found in the study of the  $\text{CH}^+$ -He complex.

These results are very useful for astrophysical observations as well as for experiments. The use of our rates to interpret  $\text{CF}^+$  observations could have important consequences on the understanding of fluorine chemistry in the ISM.

From rotational rate coefficients obtained in this work, it will be feasible to compute the hyperfine rate coefficients using the approach described by Faure & Lique (2012). This approach is well adapted to both closed- and open-shell linear rigid rotors with  $^1\Sigma$  or  $^2\Sigma$  electronic symmetry colliding with electrons, He, or para  $\text{H}_2(j = 0)$ .

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