The Geneva-Copenhagen survey of the Solar neighbourhood II*,**

New uvby calibrations and rediscussion of stellar ages, the G dwarf problem, age-metallicity diagram, and heating mechanisms of the disk

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ABSTRACT

Context. Ages, metallicities, space velocities, and Galactic orbits of stars in the Solar neighbourhood are fundamental observational constraints on models of galactic disk evolution. Understanding and minimising systematic errors and sample selection biases in the data is crucial for their interpretation.

Aims. We aim to consolidate the calibrations of uvbyβ photometry into Teff, [Fe/H], distance, and age for F and G stars and rediscuss the results of the Geneva-Copenhagen Survey (Nordström et al. 2004; GCS) in terms of the evolution of the disk.

Methods. We use recent V – K photometry, angular diameters, high-resolution spectroscopy, Hipparcos parallaxes, and extensive numerical simulations to re-examine and verify the temperature, metallicity, distance, and reddening calibrations for the uvbyβ system. We also highlight the selection effects inherent in the apparent-magnitude limited GCS sample.

Results. We substantially improve the Teff and [Fe/H] calibrations for early F stars, where spectroscopic temperatures have large systematic errors. A slight offset of the GCS photometry and the non-standard helium abundance of the Hyades invalidate its use for checking metallicity or age scales; however, the distances, redenning, metallicities, and age scale for GCS field stars require minor corrections only. Our recomputed ages are in excellent agreement with the independent determinations by Takeda et al. (2007), indicating that isochrone ages can now be reliably determined.

Conclusions. The revised G-dwarf metallicity distribution remains incompatible with closed-box models, and the age-metallicity relation for the thin disk remains almost flat, with large and real scatter at all ages (σintrinsc = 0.20 dex). Dynamical heating of the thin disk continues throughout its life; specific in-plane dynamical effects dominate the evolution of the U and V velocities, while the W velocities remain random at all ages. When assigning thick and thin-disk membership for stars from kinematic criteria, parameters for the oldest stars should be used to characterise the thin disk.


1. Introduction

Models for the evolution of spiral galaxy disks describe their star formation history, nucleosynthesis, chemical enrichment, and dynamical evolution. Traditional parameterised models yield single-valued relations for the increase in the (total or individual) heavy-element abundances of stars at a given position in the disk, radial gradients in elemental abundances, and the kinematic heating of the local disk, all as functions of time. The underlying paradigm is the efficient mixing and recycling of interstellar gas, such that mean values of abundances and kinematics as functions of time and radial position in the disk describe the underlying physical processes adequately (see Casuso & Beckman 2004; Naab & Ostriker 2006; or Cescutti et al. 2007, for recent examples). Any dispersion of the observed values around the mean relations is assumed to be due to observational error.

Under realistic conditions, however, local variations in the rate of chemical enrichment must have occurred (see e.g. Brook et al. 2007, for such an approach). The question of interest is therefore how well these relations and their intrinsic scatter can be determined from the observations.

The Milky Way is the one galaxy in which these predictions can be tested in detail. Thus, complete, accurate information on the stellar content of the Solar neighbourhood remains a fundamental observational constraint on any set of models. Much of the discussion focuses on the age-metallicity relation (AMR) for the Solar neighbourhood, and the key questions are two-fold (Twarog 1980; Carlberg et al. 1985; Meusinger et al. 1991; Edvardsson et al. 1993; Rocha-Pinto et al. 2000; Feltzing et al. 2001; and Nordström et al. 2004): (i) Does the average relation show the expected rise in metallicity from the formation of the (thin) disk to the present time? and (ii) how large is the intrinsic dispersion in metallicity at any given age? Given the wide-ranging ramifications of these questions, the observational data
used for the test must be prepared, selected, and discussed with the utmost care.

The most comprehensive recent study of nearby stars in the solar neighbourhood is the Geneva-Copenhagen Survey (Nordström et al. 2004; GCS in the following). The GCS provides metallicities, ages, kinematics, and Galactic orbits for a complete, magnitude-limited, all-sky sample of ∼14 000 F and G dwarfs brighter than V ∼ 8.3. The basic observational data are ubyβ photometry, Hipparcos/Tycho-2 parallaxes and proper motions, and some 63 000 new, accurate radial velocity observations, supplemented by earlier data. The best calibrations then available were used to derive \( T_{\text{eff}}, [\text{Fe}/\text{H}], \) and distances from the photometry. The astrometry and radial velocities were then used to compute space motions and identify binaries in the sample. Finally, unbiased ages and error estimates were computed from a set of theoretical isochrones by a sophisticated Bayesian technique (Jørgensen & Lindegren 2005), and Galactic orbits were computed from the present positions and velocity vectors of the stars and a Galactic potential model.

The GCS is large enough to yield adequate statistics for subsets of stars defined by age, metallicity, or abundance, and is essentially free of the kinematic and/or metallicity biases affecting most earlier samples. However, systematic selection effects may still remain in the data or be introduced by the calibrations used to derive astrophysical parameters from the observations. Accordingly, the purpose of the present paper is to critically re-examine the observational determination of \( T_{\text{eff}}, [\text{Fe}/\text{H}], \) and age for F- and G-type dwarf stars in the light of the most recent developments in the field. We also compare our results with those of the recent papers by Haywood (2006, H06 in the following), Valenti & Fischer (2005, VF05 in the following), and Takeda et al. (2007).

We begin the paper by briefly describing the possible impact of systematic and random errors in these parameters on the overarching theme of spiral galaxy evolution in Sect. 2. The reader mostly interested in our new ubyβ calibrations in terms of effective temperature, metallicity, distance, reddening, and age computations will find these discussed in Sects. 3–7. The reader primarily interested in the evolution of the Galactic disk may skip directly to Sect. 8, where we discuss the end-to-end simulations we have used to verify the robustness of the results reached with the new calibrations. We re-discuss the “G dwarf problem” – metallicity, and age-velocity relations for the Solar neighbourhood in Sects. 9–11 and compare the thick and thin disks in Sect. 12. Finally, we summarise our findings and conclusions in Sect. 13.

2. Astrophysical implications of calibration errors

The key parameters to be compared with models are the masses (i.e. main-sequence lifetimes), ages, heavy-element abundances, spatial distributions, and space velocities or Galactic orbits for sufficiently large samples of stars that are representative of the general population of disk stars. However, except for positions and velocities, these parameters cannot be determined by direct observation.

Typical observational data are multiband colour indices and perhaps spectra, from which \( T_{\text{eff}}, [\text{Fe}/\text{H}], \) and absolute magnitude or \( \log g \) are derived, using theoretical or empirical calibrations. From \( T_{\text{eff}}, [\text{Fe}/\text{H}], \) and \( M_V \), in turn, the age and mass of each star can be derived by comparison with stellar models.

This is straightforward in theory. In practice, it is highly non-trivial because the problem is very non-linear, and significant uncertainties in the calibrations remain. In particular, uncertainties in the theory of stellar atmospheres continue to play a major role, both for the predicted effective temperatures of stellar models and for the transformations between \( T_{\text{eff}}, [\text{Fe}/\text{H}], \) and \( \log g \) and the observed colour indices. Because of the strong correlations between these parameters, calibration errors in one may bias the determination of another and lead to spurious correlations between the derived quantities, and incorrect conclusions about the evolution of the Galactic disk.

As one example, assume that the adopted calibration yields too high \( T_{\text{eff}} \) for the hotter stars (as indeed we find below), \([\text{Fe}/\text{H}]\) as determined from equivalent widths of spectral lines will then be overestimated. The hotter \( T_{\text{eff}} \) corresponds to a lower age, the higher \([\text{Fe}/\text{H}]\) to cooler models and thus an even lower derived age for the observed star. A spurious age-metallicity relation results.

As another example, assume that the \( T_{\text{eff}} \) scale of the models is correct for the solar abundance, but too hot at lower \([\text{Fe}/\text{H}]\), as was found in GCS. This will lead to overestimated ages for the metal-poor stars, i.e. again a spurious age-metallicity relation. A similar – or additional – error is introduced if the enhanced \([\alpha/\text{Fe}]\) ratio of metal-poor stars (e.g. Edvardsson et al. 1993) is ignored; if the heavy-element abundance parameter \( Z \) of the models is assumed to scale simply as \([\text{Fe}/\text{H}]\), too hot models are selected, and the resulting age is overestimated again.

Finally, the importance of a clear understanding of the definition of the stellar sample cannot be over-emphasised: taking the AMR as the prototype again, the choice of stellar sample can determine the outcome even before a single observation is made. E.g., the F-dwarf sample studied by Edvardsson et al. (1993) excluded any old, metal-rich stars that might exist and a priori decided the shape of their AMR – a fact emphasised in the paper, but largely ignored in later references. More complete and accurate observational data are always useful, but temperature calibrations, the choice and verification of stellar models, and the methods used to compute ages and their uncertainties are far more urgent issues at present.

3. Temperature calibration

\( T_{\text{eff}} \) is the most critical parameter in the determination of isochrone ages, but also affects the spectroscopic metallicity determinations. Two qualitatively different methods to determine \( T_{\text{eff}} \) exist, based on measurements of spectral lines or on colour indices. When using spectra, the determination of \( T_{\text{eff}} \) is usually based on the excitation balance of iron, but depth ratios of sets of spectral lines have also been used. When using photometry, the determination of \( T_{\text{eff}} \) is usually tied to the infrared flux of the stars as estimated from models (the IRFM technique).

For a fundamental test, we return to the basic definition of \( T_{\text{eff}}: f_{\text{bol}} = \frac{2}{\sigma} \sigma T_{\text{eff}}^4, \) where \( f_{\text{bol}} \) is the bolometric flux and \( \phi \) the angular diameter of the star. The practical problem in applying the formula is that solar-type main-sequence stars have very small angular diameters that are difficult to measure accurately. The situation is quickly improving, however, as new interferometers enter operation, notably the ESO VLTI. Kervella et al. (2004) summarise the situation and give diameters for 20 A-M main-sequence stars and 8 A-K0 sub-giants. The angular diameters are of excellent quality, especially those from the VLTI, which have errors down to 1%.

Ramírez & Meléndez (2005a) combined these diameters with bolometric flux measurements to derive \( T_{\text{eff}} \) directly for 10 dwarfs and 2 sub-giants. Propagating the errors in the diameters and fluxes through to the temperatures, the mean error is
57 K. Ramírez & Meléndez (2005a) also give (IRFM) estimates for these stars, with a mean difference \( (T_{\text{eff,IRFM}} - T_{\text{eff,dir}}) = 10 \) K, dispersion 98 K, and mean error 28 K.

As regards spectroscopic \( T_{\text{eff}} \) determinations, Santos et al. (2005 and references therein) give results for stars both with and without detected planetary companions, including 7 stars with measured angular diameters. The mean difference is \( (T_{\text{Santos}} - T_{\text{eff,dir}}) = 92 \) K, with a dispersion of 91 K and mean error 34 K. This is in agreement with Santos et al. (2005) themselves, who find their \( T_{\text{eff}} \) scale to be 139 K hotter than that by Alonso et al. (1996), based on the IRFM and calibrated to \( B - V \) and [Fe/H].

Another valuable comparison is with the recent paper by VF05. They give spectroscopic data for \( \sim 1000 \) stars on the Keck/Lick/AAT planet search program, based on fits of synthetic spectra to their high-resolution data and correcting their zero-points from observations of Vesta as a proxy for the Sun. For the 8 stars with measured diameters, the mean difference is \( (T_{\text{VF}} - T_{\text{eff,dir}}) = 64 \) K, with a dispersion of 124 K and mean error 44 K.

The reasons for the failure of spectroscopic \( T_{\text{eff}} \) determinations based on the excitation equilibrium in 1D static LTE models are given in e.g. Asplund (2005). Basically, because real stars are spherical, hydrodynamical systems with lines formed in NLTE, the three fundamental assumptions underlying traditional model atmospheres are inadequate and lead to biased results. The correction procedure used by VF05 seems to have eliminated at least part of this bias.

In the following, we review the GCS and other recent temperature scales and derive an improved calibration for the \( u_{\text{byb}} \) system.

3.1. \( T_{\text{eff}} \) in the GCS

The marked offset of the Santos et al. (2005) \( T_{\text{eff}} \) values is confirmed for the 160 stars common to Santos et al. and the GCS, which employed temperatures based on the Alonso et al. (1996) calibration of \( b - y, m_1 \) and \( c_1 \) to the IRFM scale. The mean difference is \( (T_{\text{Santos,IRFM}} - T_{\text{eff,dir}}) = 127 \) K (dispersion 84 K, mean error 7 K). For the spectral type range in question, this shows that the GCS \( T_{\text{eff}} \) scale is in excellent agreement in the \( \text{mean} \) with temperatures derived directly from the definition of \( T_{\text{eff}} \).

However, the Alonso et al. (1996) calibration of \( b - y, m_1 \) and \( c_1 \) may be valid only in the ranges in \( T_{\text{eff}} \) within which enough calibration stars exist. Figure 1a of Alonso et al. (1996) shows the fitted temperatures as a function of \( b - y \) and makes clear that there is a marked dearth of calibration stars blueward of \( b - y \approx 0.3 \) or \( T_{\text{eff}} \approx 6500 \) K, a similar lack is seen for the reddest stars. Alonso et al. (1996) give a dispersion for their relation of \( \sigma_{(b-y)} = 0.019 \) (110 K), while Ramírez & Meléndez (2005b) give 87 K for their new \( b - y \) relation, albeit at the price of not being valid over the whole parameter range of the GCS stars.

The potential problem in the Alonso et al. (1996) \( u_{\text{byb}} \) calibration for blue and red stars is clearly demonstrated by a comparison with other calibrations of Strömgren photometry. They all agree rather well between 0.3 \( < b - y < 0.6 \), but diverge outside these limits, see e.g. Fig. 24 in Clem et al. (2004).

The situation is unfortunately similar for stars with direct \( T_{\text{eff}} \) determinations, where Kervella et al. (2004) have only one star between 6000 and 8500 K (Procyon at 6500 K), compared to 5 stars between 8500 and 10000 K and 11 between 5000 and 6000 K.

### 3.2. Calibrations based on \( V-K \)

Alternatively, temperatures based on \( V - K \) can be used, because 2MASS photometry is available and well suited to our colour and magnitude ranges: of the 16682 GCS stars, 16139 have 2MASS \( K \)-magnitudes of the highest quality class “A”. We combine these with the \( V \)-magnitude from the GCS \( u_{\text{byb}} \) photometry.

In contrast to calibrations based on only visible colours, \( T_{\text{eff}} \) estimates based on \( V - K \) are remarkably robust; the small differences are probably mostly related to the different existing definitions of the \( K \)-band. As an example, the \( V - K \) calibrations of Alonso (1996), Ramírez & Meléndez (2005b), and di Benedetto (1998) agree pairwise to within \( \sim 20 \) K for the stars in the GCS. In contrast, the Alonso \( V - K \) and \( b - y \) calibrations differ by 180 K rms!

Today, the \( K \)-band system of choice is that defined by the 2MASS catalogue, which also gives \( K \) magnitudes of high quality for most of the stars in the GCS. We have used the calibration of di Benedetto (1998), which is in excellent agreement with the IRFM temperature scale of Ramírez & Meléndez (2005a) and is valid for the whole colour range of the GCS. In order to transform the Johnson \( V - K \) colours used by di Benedetto to the \( K \) system used by 2MASS, we use the relation:

\[
(V - K)_J = 1.007[(V - K)_s - 0.044] - 0.01.
\]

Figure 1 shows the difference between the \( T_{\text{eff}} \) values from the original GCS catalogue and those derived from the 2MASS photometry and the corresponding calibration by di Benedetto (1998). The systematic differences are quite marked, especially for the hotter stars.

The trend seen in Fig. 1 is qualitatively similar to that found by H06 (Fig. 7), also by comparison with values from di Benedetto (1998), but is better determined here, due to our much larger sample and because \( V - K \) is a much more reliable temperature indicator than \( B - V \).

### 3.3. A new \( b - y - T_{\text{eff}} \) calibration

Because of the larger number of suitable calibration stars available, the \( V - K \) calibration has less systematic error. However, the observational accuracy of the \( b - y \) index is substantially better than that of \( V - K \). We have therefore derived a new \( T_{\text{eff}} \) calibration for \( b - y \), based on the \( V - K \) temperature scale set

<table>
<thead>
<tr>
<th>( T_{\text{eff}} )</th>
<th>( b - y )</th>
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<tr>
<td>5000 K</td>
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<tr>
<td>6000 K</td>
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<td>7000 K</td>
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<tr>
<td>8000 K</td>
<td>0.55</td>
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<td>9000 K</td>
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Figure 2 shows the fit to the Alonso et al. (1996) calibration of \( b - y, m_1 \) and \( c_1 \) to the IRFM scale. The mean difference is \( (T_{\text{Santos,IRFM}} - T_{\text{eff,dir}}) = 127 \) K (dispersion 84 K, mean error 7 K).
by di Benedetto (1998). The best result is achieved when the sample is divided into three temperature ranges. In the blue range ($0.20 < b - y < 0.33$) the relation is:

$$
\theta_{\text{eff}} = 0.649 + 0.095(b - y) + 0.034[\text{Fe/H}] + 1.207(b - y)^2 - 0.005[\text{Fe/H}]^2 - 0.181(b - y)[\text{Fe/H}]
$$

where $\theta_{\text{eff}} = 5040$ K/$T_{\text{eff}}$. The dispersion of the fit is $\sigma(\theta_{\text{eff}}) = 0.007$ when 2.5-$\sigma$ outliers are removed, corresponding to 60 K or 0.004 in log $T_{\text{eff}}$ for the mean log $T_{\text{eff}}$.

In the middle range ($0.33 < b - y < 0.50$), the relation is:

$$
\theta_{\text{eff}} = 0.754 - 0.365(b - y) - 0.001[\text{Fe/H}] + 1.635(b - y)^2 - 0.011[\text{Fe/H}]^2 - 0.091(b - y)[\text{Fe/H}].
$$

The dispersion of the fit is $\sigma(\theta_{\text{eff}}) = 0.009$ when 2.5-$\sigma$ outliers are removed, corresponding to 57 K or again 0.004 in log $T_{\text{eff}}$ for the mean log $T_{\text{eff}}$.

In the red range ($0.50 < b - y < 0.60$), the relation is:

$$
\theta_{\text{eff}} = 0.255 + 1.656(b - y) + 0.018[\text{Fe/H}] - 0.397(b - y)^2 - 0.011[\text{Fe/H}]^2 - 0.101(b - y)[\text{Fe/H}].
$$

The dispersion of the fit is $\sigma(\theta_{\text{eff}}) = 0.012$ when 2.5-$\sigma$ outliers are removed, corresponding to 55 K or 0.005 in log $T_{\text{eff}}$ for the mean log $T_{\text{eff}}$.

We note that this calibration yields 5777 K for the Sun when using $(b - y)_0 = 0.403$ from Holmberg et al. (2006), although this was not forced on the fit. The two main calibrations are also very well connected: at their common colour, $(b - y) = 0.33$, the difference in temperature is 2, 6, and 7 K at [Fe/H] = 0, −0.50, and −1.00. Due to the small number of very red calibration stars, the difference in $T_{\text{eff}}$ grows to −19, 18, and 52 K at [Fe/H] = 0, −0.50, and −1.00 at $(b - y) = 0.50$ — still very small.

Figure 2 demonstrates the agreement of the resulting $T_{\text{eff}}$ values with those derived from $V - K$ and the di Benedetto (1998) calibration.

Finally, we compare our new photometric temperatures to the spectroscopic results by VF05. Figure 3 shows the temperature differences for the 697 single stars in common with the GCS. The mean difference is similar to that from the stars with angular diameters: $(T_{\text{eff}}^{\text{VF05}} - T_{\text{eff}}^{\text{phot}}) = 43$ K, with a dispersion of 91 K.

4. Metallicity calibration

[Fe/H] is important, both in itself as a diagnostic of the chemical evolution of the disk, and because it enters into the determination of stellar ages from theoretical isochrones. However, a comparison of the GCS photometric metallicities with the several high-quality spectroscopic studies available today (Fig. 4) shows significant differences, even when considering only spectroscopic studies using a photometric temperature scale.

For the four major spectroscopic studies (in the order Edvardsson et al. 1993; Chen et al. 2000; Reddy et al. 2003; and Allende Prieto et al. 2004), the mean differences ([Fe/H] − [Me/H]) are, for the F-calibration range: 0.064, 0.038, 0.114 and 0.013; and for the G-calibration range: 0.019, −0.038, 0.022 and −0.044. Only Allende Prieto et al. (2004) have stars in the range of the “K” calibration (as defined in GCS), with $([\text{Fe/H}] - [\text{Me/H}]) = -0.005$.

As regards Santos et al. (2005), who use a spectroscopic $T_{\text{eff}}$ scale, we find $([\text{Fe/H}] - [\text{Me/H}]) = 0.162$ for stars in F range, $([\text{Fe/H}] - [\text{Me/H}]) = 0.082$ for stars in the G range, and $([\text{Fe/H}] - [\text{Me/H}]) = 0.022$ for their stars in the K range.

We conclude that metallicities derived using the spectroscopic $T_{\text{eff}}$ scale must be reduced by about 0.10, 0.09 and 0.03 dex for the F, G and K temperature ranges. This is in fair agreement with the estimated effect on [Fe/H] of a temperature shift of about 100 K (see e.g. Feltzing & Gustafsson 1998).

We conclude that, when comparing metallicity scales from different sources, it is crucial to verify how these scales are established. It is especially important to check which $T_{\text{eff}}$ scale is used, because an erroneous $T_{\text{eff}}$ scale can introduce large
4.1. The original GCS calibration

The determination of accurate metallicities for F and G stars is one of the strengths of the Strömgren uvyβ system. Among the then available uvyβ calibrations, the GCS used that by Schuster & Nissen (1989) for the majority of the stars.

However, this calibration was found to give substantial systematic errors for the very reddest G and K dwarfs (b − y > 0.46), where very few spectroscopic calibrators were available at that time. In the GCS we therefore derived a new relation, based on a sample of 72 dwarf stars in the colour range 0.44 ≤ b − y ≤ 0.59, using the same relations in the calibration equation as the Schuster & Nissen (1989) G-star calibration. The resulting equation was:

\[
\frac{[\text{Fe/H}]}{\text{M}_\odot} = -2.06 + 24.56m_1 - 31.61m_2^2 - 53.64m_1(b - y) + 73.50m_2(b - y) + [26.34m_1 - 0.46c_1 - 17.76m_2^3]c_1.
\]

The metallicities from this calibration are compared to the new spectroscopic reference values in Fig. 5. The dispersion around the (zero) mean is 0.12 dex.

For the ~600 stars in the interval 0.44 < b − y < 0.46, the new calibration agreed with that by the Schuster & Nissen (1989) to within 0.00 dex in the mean (s.d. 0.12).

About 2400 GCS stars with high T eff and low log g were outside the range covered by the Schuster & Nissen (1989) calibration. For these stars, the calibration of β and m_1 by Edvardssson et al. (1993) was used when valid. For the stars in common, the two calibrations agree very well (mean difference of 0.00 dex, dispersion only 0.05).

For stars outside the limits of both calibrations, we derived a new relation, using the same terms in the equation as the Schuster & Nissen (1989) calibration for F stars. From 342 stars in the ranges: 0.18 ≤ b − y ≤ 0.38, 0.07 ≤ m_1 ≤ 0.26, 0.21 ≤ c_1 ≤ 0.86, and −1.5 ≤ [Fe/H] ≤ 0.8, we found the following calibration equation:

\[
[\text{Fe/H}] = 9.60 - 61.16m_1 + 81.25m_2(b - y) + 224.65m_2^2(b - y) - 153.18m_1(b - y)^2 + [12.23 - 90.23m_1 + 38.70(b - y)]\log(m_1 - c_3),
\]

where \(c_1 = 0.45 - 3.98(b - y) + 5.08(b - y)^2\). The dispersion of the fit is 0.10 dex.

Figure 5 compares the photometric [Fe/H] from this calibration with the spectroscopic values; for the stars in common, they again agree very well those from the Schuster & Nissen (1989) calibration (mean difference 0.02 dex, σ only 0.04).

4.2. An improved metallicity calibration

In order to define an improved photometric metallicity calibration that is valid for all GCS stars, we select only spectroscopic investigations using a photometric temperature scale (unlike the compilation of literature values by Cayrel de Strobel et al. 2001 used by H06). This yields a total sample of 573 stars from Edvardsson et al. (1993), Chen et al. (2000), Reddy et al. (2003), Allende Prieto et al. (2004), and Felting & Gustafsson (1998).

They all have a very consistent metallicity scale: Comparing stars in common yields differences of 0.02 dex or smaller in the mean, with a dispersion of ~0.07 dex. The 573 stars span the range 0.24 ≤ b − y ≤ 0.63, 0.10 ≤ m_1 ≤ 0.70, 0.17 ≤ c_1 ≤ 0.53, and −1.0 ≤ [Fe/H] ≤ 0.37.

A new fit of the uvy indices to the spectroscopic [Fe/H] values from this sample was performed, using a calibration equation containing all possible combinations of b − y, m_1, and c_1 to third order.

The resulting calibration equation is:

\[
[\text{Fe/H}] = -2.19 - 1.02(b - y) + 7.34m_1 - 0.27c_1 + 5.86(b - y)^2 - 43.74m_2^2 - 0.14c_1^2 + 25.03(b - y)m_1 + 5.29(b - y)c_1 + 25.95m_1c_1 + 31.10(b - y)^3 + 46.19m_1^3 - 3.86c_1^3 + 4.54(b - y)b_1^3m_1 + 19.31(b - y)^2c_1 - 17.46m_2^3(b - y) + 18.36m_1^2c_1 - 9.99c_1^2(b - y) + 6.60m_1^2m_1 - 59.65(b - y)m_1c_1.
\]

This new calibration is used for all stars with 0.30 < b − y < 0.46. Together with the blue and red calibrations already derived in the GCS, this completes the final metallicity calibration of the present paper. All results discussed in the following are based on it.

Figure 6 shows the differences between the GCS [Fe/H] values and those derived with the new calibration; note that, in the left panel of Fig. 6, the heavy sequence at zero reference is 0.00 (dispersion 0.09) in the common range 0.3 < b − y < 0.32. Compared to the red relation, the mean difference is 0.00 (dispersion 0.09) in the common range 0.44 < b − y < 0.50.

Finally, Fig. 8 compares our new GCS metallicities with the spectroscopic [Fe/H] values from VF05. The mean difference VF05-GCS is 0.08 dex, with a standard deviation of 0.10 dex.
4.3. The Hyades and Coma clusters

One of the two open clusters included in the GCS, the Hyades, has been used by e.g. H06 to assess the zero-point of the GCS metallicity calibration. A comparison with the original $uwb$ photometry of the Hyades and Coma clusters by Crawford & Perry (1966) and Crawford & Barnes (1969) shows, however, that the photometry of the cluster stars that was listed in the GCS is not on the same system as the rest of the catalogue, perhaps because they were observed at high air mass from Chile. While unfortunate, this offset means that the Hyades data will give misleading results if applied to the metallicities (and thus ages) of the whole GCS catalogue.

The result of using the photometry from the original sources combined with the earlier GCS calibrations is shown in Fig. 9. For the Hyades, we then find $\text{[Fe/H]} = 0.10 \pm 0.10$; for Coma, $\text{[Fe/H]} = -0.02 \pm 0.08$ (mean and dispersion). The derived $\text{[Fe/H]}$ for the Hyades corresponds well to the standard value, as expected because it is mostly based on the Schuster & Nissen calibration, which used the Hyades as a main anchor point.

Using the new calibration instead yields $\text{[Fe/H]} = 0.06 \pm 0.07$ for the Hyades and $\text{[Fe/H]} = -0.09 \pm 0.06$ for Coma. The dispersion among the cluster stars is no larger than in the field star calibration, but there is an offset of about 0.07 dex.

A different photometric $\text{[Fe/H]}$ for the Hyades is to be expected, considering the non-standard $\text{He/Fe}$ ratio of this cluster (Vandenberg & Clem 2003), but Coma has a standard chemical mix, and the mean photometric metallicity is very near the accepted spectroscopic value.

In summary, we conclude that it is inadvisable to use the Hyades for general calibrations of photometric metallicities or comparing metallicity scales. The same is true for the ages, especially for the unevolved solar-type stars for which isochrone ages are bound to be very uncertain by any method.

Finally, we note that the revised data in Table 1 for Hyades and Coma stars are based on the standard photometry and can be used with confidence.

4.4. Solar analogs as a test of the calibrations

Solar analogs offer yet another test of the temperature and metallicity determinations. Such stars can be identified through either photometric or spectroscopic resemblance to the Sun – preferably both. 18 Sco (HD 146233) is one of the best known examples, with $b-y = 0.404$, $M_V = 4.77$, as compared to the value $b-y = 0.403$ for the Sun by Holmberg et al. (2006), determined
by comparison with a carefully selected sample of stars similar to the Sun. 

[Fe/H] for 18 Sco is close to zero with both the old (+0.03) and new (-0.02) metallicity calibrations, whereas \( T_{\text{eff}} = 5766 \) K as derived from \( b - y \) and the new calibration is much closer to that of the Sun than the GCS value of 5689 K, in good agreement with the general trend of Fig. 1.

5. Absolute magnitude/distance calibration

In order to determine an improved absolute magnitude/distance calibration for \( uvby \) photometry, we selected a sample of 2451 stars with absolute magnitudes better than 0.10 mag from Hipparcos and no indication of binarity in the GCS. A relation using all combinations of \( b - y \), \( m_1 \) and \( c_1 \) up to third order was then fitted to the absolute magnitudes of these stars.

The difference between the calibration data and the fitted relation is shown in Fig. 10. The dispersion of the fit is 0.24 mag, but there is a clear excess of stars with large differences, probably due to still-undetected binaries. Repeating the fit after removing stars more than 2.5\( \sigma \) from the mean relation reduces the dispersion to 0.16 mag. The stars span the range: \( 0.20 \leq b - y \leq 0.60 \), \( 0.09 \leq m_1 \leq 0.64 \), \( 0.16 \leq c_1 \leq 0.80 \), and \( -0.84 \leq M_V \leq 7.24 \).

The resulting calibration equation, valid within the above parameter ranges, is:

\[
M_V = 2.999 + 2.68(b - y) + 10.08m_1 + 3.14c_1 + 15.27(b - y)^2
- 17.73m_1^2 + 26.28c_1^2 - 12.73(b - y)m_1 - 20.79(b - y)c_1
- 38.86m_1c_1 - 17.47(b - y)^3 - 24.14m_1^3 + 8.16c_1^3
- 56.98(b - y)^3m_1 + 27.86(b - y)^3c_1 + 103.32m_1^3(b - y)
- 161.55m_1^2c_1 - 131.37c_1^2(b - y) + 29.51c_1^2m_1
+ 257.37(b - y)m_1c_1
\]

\( \sigma(M_V) \) corresponds to distance errors of only 11% and 7% (with and without 2.5-\( \sigma \) outliers). Note that this is the total dispersion, including also the error in the Hipparcos distances. A further check of the new calibration based on the wide physical binaries in the sample confirms this estimate (see Sect. 7.2).

This relation is a clear improvement over the photometric distance calibration used in the GCS, which had an uncertainty of 13% (0.28 mag). It can also be used to identify further binaries in the GCS catalogue, which only flagged stars with a difference between the Hipparcos and photometric \( M_V \) larger than 3\( \sigma \), i.e. larger than 0.84 mag from the photometry alone. We have not, however, recomputed the statistics on binaries in the GCS, as other sources of uncertainty remain important.

As already expected from Fig. 10 in the GCS, there is no systematic difference between the GCS distances and those computed with the above formula (see Fig. 10). However, the uncertainty of the individual distances – which dominates that of the space motions – is reduced enough that we have recomputed the distances and UVW velocity components for all the GCS stars, correcting a minor error in the GCS space velocities at the same time.

6. Interstellar reddening

In the GCS, interstellar reddening were derived from the intrinsic colour calibration by Olsen (1988), which yields reddening estimates with a stated precision of 0.009 mag. In the GCS there are 827 stars within 40 pc which have \( E(b - y) \) estimates. Figure 11 (left) shows the histogram of these \( E(b - y) \) values; a best-fit pure Gaussian shows only a slight zero-point shift of 0.0025 and a dispersion of 0.0105 mag.

The distribution is quite symmetric, showing that it is dominated by observational errors and that real reddening within 40 pc is negligible. This is no longer true for the distance range from 40 to 70 pc, where the distribution is markedly skewed, with a clear excess of true positive extinctions (see Fig. 11, right). Thus, contrary to the assertion by H06, this distance range contains a clear excess of stars with significant positive reddening; the mean reddening is 0.0048 mag for this sample.

We conclude that the intrinsic colour calibration by Olsen (1988) remains valid with sufficient accuracy for the GCS sample, so we do not recompute \( E(b - y) \) and \( (b - y)_0 \).

7. Stellar ages

7.1. Review of stellar models

The determination of ages for individual field stars in the range 1–10 Gyr is a field with rich opportunities for large systematic as well as random errors. Some of these arise from the calibrations of the observational data, as reviewed in the preceding chapters. Others are due to the various approximations used in stellar model calculations, especially as regards the treatment of convective core overshooting in this regime of small to vanishing convective cores, and of the stellar atmospheres that are used to compute the observable properties of a model, notably \( \log g \) and \( T_{\text{eff}} \).

The density and sampling of the grid of models and/or isochrones are also important in this range, where a major change in isochrone morphology near the turnoff occurs for ages of several Gyr. Other errors again may result from the
techniques used to interpolate in the published isochrones and compute masses, ages, and error estimates from the observed data.

In the GCS, great effort was devoted to the derivation of ages and masses and their uncertainties for the stars of the survey, using the sophisticated interpolation method and Bayesian computational techniques of Jørgensen & Lindegren (2005) and accounting for the average α-element enhancement of metal-poor stars. Exactly the same method was adopted in the very recent paper by Takeda et al. (2007). The theoretical isochrones used in the GCS computations were the latest set from the Padova group (Girardi et al. 2000; Salasnich et al. 2000), while Takeda et al. (2007) computed an extensive set of new tracks using the Yale-Yonsei stellar evolution code (Demarque et al. 2004).

In order to assess the effect of different model prescriptions, we have compared the Padova isochrones to both the Yale-Yonsei (Demarque et al. 2004) and Victoria-Regina models (VandenBerg et al. 2006) as well as to two different Geneva model series (the “basic” and “best low-mass” models, Lejeune & Schaerer 2001).

Figure 12 shows that the differences between the various models are in fact quite small. The difference in age for a star located on the three isochrones in the middle, if derived instead from the two outlying ones, is below 1 Gyr at the turnoff and about 2 Gyr at $M_V = 5$, respectively. For the 5 Gyr isochrones, the difference is about 1 Gyr at both points; the larger percentage age spread at the turnoff is related to the slightly different treatment of convective overshooting in the different models. The situation is similar at e.g. $[\text{Fe}/\text{H}] = -0.71$, the difference between the isochrones being even somewhat smaller.

Accordingly, in the following we use the same Padova isochrones and α-enhancement corrections as in the GCS itself and do not repeat the full age computations with all the different sets of models. This will highlight the effect of changing the calibrations as discussed above, while comparing with the ages computed by VF05 and Takeda et al. (2007) will illustrate the effects of photometric vs. spectroscopic input parameter determinations.

7.1.1. The model temperature scale

In the GCS, close attention was paid to verifying the consistency between the computed lower main sequences and the observed unevolved stars. An appreciable offset was found, and substantial, metallicity-dependent, negative temperature corrections were applied to the Padova models to avoid deriving spuriously large ages for the low-mass stars. No similar offset seems to have been found necessary by Takeda et al. (2007), perhaps because the Yale-Yonsei models (Demarque et al. 2004) themselves appear to be somewhat cooler than the Padova models (see Fig. 12). The offset is also masked by the hotter temperatures and higher metallicities they adopt for their stars.

With the new temperature and metallicity calibrations derived in this paper, the temperature corrections applied to the Padova isochrones in the GCS also need revision. We find corrections of $\delta \log T_{\text{eff}} = -0.005$ for $[\text{Fe}/\text{H}] \geq 0$, $-0.01$ at $[\text{Fe}/\text{H}] = -0.40$, $-0.02$ at $[\text{Fe}/\text{H}] = -0.70$, and $-0.025$ at $[\text{Fe}/\text{H}] \leq -1.30$ to be needed for the models to match the observed ZAMS; see Figs. 14 and 13.

As a further check, Fig. 14 compares the temperature-corrected solar-metallicity model main sequences with the distribution of stars in the observed catalogue as well as in a simulated sample (see Sect. 8.1) with errors in $\log T_{\text{eff}}$, $[\text{Fe}/\text{H}]$, and $M_V$ as observed, both in the range $[\text{Fe}/\text{H}] = 0.00 \pm 0.03$. Note that the main purpose of the figure is to illustrate the scatter of stars around the ZAMS due to measurement errors; the model has not been designed to account for the effect of the age-dependent sample volume of the GCS on the distribution of stars in the HR diagram (cf. Sect. 8.1).

Another way to check the temperature corrections is to consider active stars with low chromospheric ages. Figure 15 compares stars with $-0.1 < [\text{Fe}/\text{H}] < 0.1$ and chromospheric ages below 1 Gyr from the catalogue of Wright et al. (2004) to a solar-metallicity 1-Gyr isochrone, corrected as above. As seen, the agreement is again quite satisfactory.

Finally, a test can be made using single Hyades stars with photometry from Crawford & Perry (1966). Figure 16 compares these stars to a 0.7-Gyr corrected isochrone and shows the estimated ages and their uncertainties. The scale offset in the ages is due to the use of a standard Y/Z ratio in the models, which is incorrect for the Hyades (VandenBerg & Clem 2003).

7.2. Consistency checks with wide binaries

Wide physical binaries as confirmed by proper motions and radial velocities provide another check of the accuracy of our metallicity, distance, and age determinations. We have selected 18 such pairs from the GCS, with separate measurements of all parameters and no indication of further multiplicity. The pairs have a wide distribution in $[\text{Fe}/\text{H}]$, from $-0.4$ to +0.1, and ages in the range 0–10 Gyr. Figure 17 shows a typical example.

With the GCS calibrations, the rms difference in $[\text{Fe}/\text{H}]$ between the two components is 0.11 dex; using the new calibration reduces it to 0.06 dex, in excellent agreement with our other error estimates. Similarly, using the new photometric distance calibration (Sect. 5) instead of the older ones used in the GCS reduces the average difference in distance between the binary components from $16 \pm 3\%$ to $12 \pm 3\%$ (s.e. of mean).

The accuracy of the age determination can be estimated from the ratio of the age difference between the two binary components, $\Delta$Age, and the combined 1σ uncertainty of the two ages, $\sigma$Age. For the GCS ages we find $(\Delta$Age$/\sigma$Age) = 0.87. Recomputing the ages and age uncertainties for the binary
components, using the new calibrations and (lower) estimated errors for \([\text{Fe}/\text{H}], T_{\text{eff}}\) from \(b-y\), and photometric \(M_V\) as well as the newly corrected isochrones, we find \(\langle \Delta \text{Age}/\sigma \text{Age} \rangle = 0.76\). In other words, the age estimates become more consistent as well as more precise with the new calibrations.

7.3. New ages vs. the GCS ages

Figure 18 compares the GCS ages, computed with the old \([\text{Fe}/\text{H}], T_{\text{eff}}\) calibrations, with the ages computed using the new calibrations and model corrections from this paper. Overall, the differences are insignificant, much smaller than the estimated individual uncertainties. A linear fit gives the following mean relation between the new ages and those in the GCS: \(\text{Age}_{\text{New}} = 0.16 + 0.90 \times \text{Age}_{\text{GCS}}\) (all ages in Gyr). Thus, on average, the largest ages decrease by \(\sim 10\%\). This is similar to the differences seen when using different stellar models and has negligible impact on the interpretation.

The only noteworthy deviations occur on the two “branches” that can be seen in Fig. 18. This small group of stars is located in the “hook” region in the HR diagram, where an observed point is matched by two different isochrones, one placing the star on the main-sequence turnoff, the other on the early subgiant branch. As explained e.g. in Jørgensen & Lindegren (2005), this leads to a two-peaked G-function structure. Small changes in the assumed \([\text{Fe}/\text{H}]\) and \(T_{\text{eff}}\) may then change the relative height of the peaks, and thus the most probable age of the star. For such double-peaked G-functions, one could use a weighted mean of the two maximum values rather than a simple fit to the highest peak, but the improvement would be cosmetic rather than real.

Finally, we compare our results to two recent sets of ages, both computed from the spectroscopic results by VF05. One set is given in that paper itself, using a relatively crude method,
while the more recent one by Takeda et al. (2007) was computed with the same Bayesian technique as used in the GCS, based on a dense grid of stellar evolution tracks computed with the Yale-Yonsei code (Demarque et al. 2004). In order to avoid confusion by including stars with highly uncertain ages (see, e.g. Fig. 8 of Reid et al. 2007), we select only single stars with ages better than 25% as given by both sources.

Figure 19 shows the remarkable result of this comparison. While the VF05 ages are on average ~10% lower than ours, those by Takeda et al. (2007) are in essentially perfect agreement with ours. Considering that these results are based on totally different observational data and analysis techniques, calibrations, and stellar models, the agreement is extraordinarily close and inspires a solid confidence in age determinations from isochrones. Note that the differences between Takeda et al. (2007) and VF05 are due to different computational techniques applied to the same data, while the differences between the old and new GCS ages are due to improved calibrations, the computational method remaining the same. That the systematic differences seen in both cases are only of the order of ~10% gives further confidence in the robustness of the method.

For future reference we recall that, temperature and metallicity calibrations aside, the age estimates computed by H06 were based on an unrealistically small value for the uncertainty of \( T_{\text{eff}} \). Further, the computations ignored the uncertainty in \( M_V \) as well as the temperature offset of the models, the \( \alpha \)-enhancement of the metal-poor stars, and the presence of binaries in the sample. Moreover, the bright limit of \( M_V = 2 \) excluded many young stars for which good ages can be readily determined (see GCS Fig. 11a), while at the same time including low-mass giants for which meaningful ages cannot be derived. Finally, the uncertainty of the resulting ages was not discussed.

8. Results and sample characteristics

Based on the new calibrations and model corrections discussed above, we have computed new \( T_{\text{eff}}, [\text{Fe/H}], \) distances, ages and age uncertainties, and space motions for all the stars in the GCS. Table 1 gives the results; the full version is available in electronic form at the CDS. We have not recomputed Galactic orbital elements for the stars, as uncertainties in the assumed (smooth, axially symmetric) potential are more important than minor revisions of the space motions. In the following, we discuss the implications of the new data for our understanding of the evolution of the Milky Way disk.

In such discussions, it is crucial to not only employ the best possible calibrations from observed to astrophysical parameters, but also to understand to what extent the criteria used to select the stellar sample may influence the conclusions drawn. This is especially important when studying subsamples selected on the basis of having one or more of the derived parameters available, perhaps within a certain level of precision, rather than the entire GCS. Age is the most striking example: The samples of stars having ages better than 25%, or “well-defined” ages in the GCS sense, or any ages at all, are all very different from the full GCS sample in very non-random and non-intuitive ways.

Much effort was spent checking these issues in preparation for the GCS. Only overall results were mentioned in the paper.
8.1. Simulating the sample selection effects

To estimate the interplay between the sample selection criteria and any errors in the determination of the derived parameters in the GCS, we have performed an extensive set of numerical simulations based on a synthetic catalogue. The synthetic catalogue assumes a constant density of stars in a spherical volume of ∼250 pc radius, a mixture of 90% thin-disk and 10% thick-disk stars with an even distribution in stellar age and evolutionary stage. Several distributions in metallicity and kinematics were imposed on the thin disk in order to explore the possible systematic effects; for the thick disk we assumed an asymmetric drift in $V$ of 65 km s$^{-1}$ and ($\sigma_V, \sigma_V, \sigma_W$) = (72, 43, 36) km s$^{-1}$.

The star density was normalised such that, after applying the appropriate cutoffs, the resulting sample would contain about 15 000 stars total, with about 97% thin-disk and 3% thick-disk stars, as observed. Each component has a distribution in metallicity and kinematics similar to the observed values, and the distribution of stellar parameters and measurement errors is also like the real catalogue. In order to better test the age estimation process at faster evolutionary stages, the stars are more uniformly distributed along the isochrones than what would result from a standard IMF.

By applying the various calibrations, computations, and parameter cuts to the simulated catalogue in parallel with the observed sample, we can ascertain in quantitative terms which systematic effects may be introduced at each stage and whether they have any significant influence on the conclusions.

As a first example, we show how the volume of space sampled by the GCS varies with age. Because older stars are, on average, fainter (and cooler) than younger stars, and the GCS sample is limited by apparent magnitude, the volume sampled by the GCS decreases with stellar age. GCS Fig. 24 showed this effect as a function of colour; here we illustrate the dependence on age directly by imposing a simple apparent-magnitude cutoff at $V = 8$ and computing the average volume occupied by the stars in successive 1-Gyr age bins, normalised to that occupied by the youngest stars (=100%).

Figure 20 compares the result for the simulated sample (dotted curve) with the same computation for the real GCS (full line). Only single stars with “well-defined” ages are included. The GCS adopts fainter limiting magnitudes for the redder stars in order to achieve volume completeness to 40 pc, so the fraction of older stars is higher than for the simplified simulation.
However, the origin of the preponderance of young stars in, 

e.g., Figs. 23 and 29 is clear: They are included from a volume 

~5 times larger than the stars older than ~3 Gyr. Accounting 

properly for these sampling volume differences is, of course, 

relevant when deriving the star formation history of the solar neigh- 

bourhood from the data — a study we do not undertake here. 

More specific simulations have been carried out to test the 

most significant conclusions of the GCS; they are described in 

the following as appropriate in each context.

9. The metallicity distribution function

Models of star formation and chemical evolution in the galactic 

disk make predictions of the distribution of heavy-element abund- 

cances in stars that (could) have survived from all stages of the 

evolution. The classic failure of “closed-box” models – the so-


called “G-dwarf problem” – refers to the observed lack of those 

metal-poor dwarf stars that should have accompanied the high-

mass stars that produced the heavy elements we observe in the 

younger stars, assuming a constant IMF. One may ask whether 

the metallicity calibration or the way the data are compared with 

the models may cause a spurious difference. 

Figure 21 compares the distributions of the GCS stars in 

[Fe/H] and $T_{\text{eff}}$ as derived with the old and new calibrations. As 

seen, the new calibration leads to even fewer metal-poor stars in 

the sample than the old one, but the difference is marginal. 

Galactic evolution models typically predict average proper-


ties of the stellar population in a vertical column through the 

disk at the position of the Sun, while observations typically – as 

in the GCS – refer to a roughly spherical volume centred on the 

Sun. Knowing the motions of the stars enables us to allow for 

this difference.

We have performed the correction from a volume-complete 

to a column-complete sample in a rigorous manner, using the 

self-consistent mass models of the disk derived by Holmberg & 

Flynn (2000, 2004; latest version in Flynn et al. 2006). With this 

model, we derive the relation between volume and column den-

sity for each velocity dispersion. Figure 22 shows the vertical 

velocity dispersion of the GCS stars as a function of metallicity, 

together with a smooth polynomial fit. This fit is then used to 

transform the volume densities to corresponding column densi-

ties as functions of [Fe/H]. 

Figure 22 compares the volume and column metallicity dis-

tribution functions with each other and with a closed-box model 

without instantaneous recycling approximation (Casuso & Beckman 2004), convolved with a Gaussian of $\sigma = 0.08$ to 

account for the observational error in [Fe/H]. Clearly, neither 

the calibration nor the volume/column correction can account 

for the observed dramatic deficiency of metal-poor stars relative 

to the model.

We cannot comment on the reasons why H06 reached a dif-

ferent conclusion from the same data (albeit with a different metallicity calibration), since the closed-box model discussed by H06 was not described there.

10. The age-metallicity diagram

The relationship between average age and metallicity for stars in 

the solar neighbourhood – the so-called age-metallicity relation (AMR) – is probably the most popular diagnostic diagram for 

comparing galactic evolution models with the real Milky May. 

There is, however, no consensus on its shape or interpretation.

The discussion centres essentially on (i) the presence or ab-

sence of a general slope of the AMR (a gradual increase in mean 

[Fe/H] with time), and (ii) how much of the scatter in [Fe/H] at 

any given age is accounted for by observational errors and how 

much reflects the complexity in the evolution of a real galaxy as 

compared to most current models. It is thus crucial to ascertain 

whether the distribution of stars in the age-metallicity diagram 

(AMD) reflects primarily the intrinsic properties of the sample 

or primarily artefacts of the measurement and parameter calcu-

lation procedures.

This can be investigated by means of our simulated sample. First, we check whether the new calibrations have by them-

selves caused any significant change in the AMD, using the stars 

with the very best ages ($\sigma(\text{Age}) < 25\%$). In order to elimi-

nate the bright, distant early F stars in the GCS whose high 

[Fe/H] we suspected to be due to overestimated reddening cor-

rections, we have limited the sample to single stars within 40 pc 

or with $E(b-y) < 0.02$ mag. As seen, the revised calibrations 

cause hardly any difference in the AMD, neither for the full sam-

ple (Fig. 23) nor for the strictly volume-limited one (Fig. 24). 

Perhaps the most obvious structure in the observed AMD 

is the marked increase in mean metallicity and the absence 

of metal-poor stars for ages below 2 Gyr (see Fig. 23 and GCS 

Figs. 27, 28). It is important to understand if this is due, at least in 

part, to the selection criteria used to define the catalogue sample, 

or whether it is a genuine property of the solar neighbourhood. In 

the latter case, it could be interpreted as a cut-off in the resupply 

of fresh low-metallicity gas, followed by closed-box evolution.
Table 1. Sample listing of the recomputed parameters for the first five stars in the GCS catalogue. $Age_{\text{low}}$ and $Age_{\text{up}}$ are the lower and upper 1-$\sigma$ confidence limits on the computed age, respectively. The full table is available in electronic form from the CDS (see reference on title page).

| HIP Name | Comp RA ICRF Dec ICRF $\log T_e$ [Fe/H] $d$ ($d$) Age $Age_{\text{low}}$ $Age_{\text{up}}$ $U$ $V$ $W$ |
|----------|---------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|          |               |       |       |       |       |       |       |       |       |       |       |       |
| 437 HD 15 | 00 05 17.8 | +48 28 37 | | | | | | | | | | |
| 431 HD 16 | 00 05 12.4 | +36 18 13 | | | | | | | | | | |
| 420 HD 23 | 00 05 07.4 | −52 09 06 | 3.776 | −0.17 | 42 | 4.44 | 6.3 | 15 | 22 | 16 | | |
| 425 HD 24 | 00 05 09.7 | −62 50 42 | 3.768 | −0.33 | 70 | 3.91 | 8.5 | 7 | 14 | | | |
| HD 25     | 00 05 22.3 | +49 46 11 | 3.824 | −0.30 | 79 | 3.09 | 2.0 | 22 | 16 | | | |

Figure 21. Left: metallicity distribution function for all stars using the new calibration (solid) as well as the original GCS values (dotted). Right: the distribution of $T_{\text{eff}}$ with the new and old calibrations (same symbols).

Figure 22. Left: the $W$ velocity dispersion as a function of [Fe/H] for the volume-complete sample (equal-size bins). Right: metallicity distribution function for stars in the volume-complete sample (solid); in the column, using the fit in the left-hand panel (dashed); and in the closed-box model of Casuso & Beckman (2004, thin line).

Figure 23. Top: AMR from the original GCS, for single stars with ages better than 25% and with $E(b-y) < 0.02$ or $d < 40$ pc. Large dots are mean values in bins with equal numbers of stars. Bottom: same, using the improved stellar parameters.
Focusing on the stars older than 4 Gyr in Fig. 24, we find a mean \([\text{Fe/H}] = -0.24\) dex and standard deviation \(\sigma = 0.22\) dex for the original GCS data (top panel, 70 stars), and a mean \([\text{Fe/H}] = -0.21\) dex and \(\sigma = 0.21\) dex using the new calibrations (bottom panel, 75 stars). Subtracting the estimated observational error in each case (0.10 and 0.07 dex) yields an intrinsic (“cosmic”) scatter in \([\text{Fe/H}]\) at a given age of 0.20 dex – identical to the result by Edvardsson et al. (1993) from high-resolution spectroscopy.

We conclude the discussion by reiterating the importance of the sample selection on the resulting AMR. If certain types of stars are excluded a priori, the gross shape of the AMR may be predetermined whatever new metallicities or ages may be observed. Figure 27 illustrates this, using two popular sources, VF05 and Edvardsson et al. (1993). Both were selected for specific purposes, and both are prone to selection effects affecting the AMR.

Edvardsson et al. selected evolved F-type dwarfs in order to be able to determine isochrone ages, excluding a priori any old, metal-rich and therefore redder (i.e. G) stars that might have populated the upper right-hand part of the AMR. VF05 studied stars used in planet searches and thus avoided stars with weak lines, i.e. hot metal-poor stars in the opposite corner of the AMR. These facts are clearly discussed in the papers, but make these and other inherently biased samples unsuitable for discussions of the general AMR of the solar neighbourhood.

10.1. AMR slope vs. a radial metallicity gradient

Recently, Rocha-Pinto et al. (2006) interpreted an observed variation of mean metallicity with the difference between the mean orbital radius of the star \((R_m)\) and that of the Sun \((R_\odot)\) as evidence for a tight age-metallicity relation in the thin disk. However, because their values of \(R_m\) range from 6 to 9 kpc, many of their stars must have large velocities and orbital eccentricities, usually associated with thick-disk stars. This was already noted by Edvardsson et al. (1993), although they did not use the explicit term “thick disk”.

A much more natural explanation of the apparent radial variation in metallicity is that the observed stellar sample is a mix of thin-disk stars dominating close to the solar circle, and thick-disk stars dominating at both high and especially low \(R_m\). To verify this, we have compared the observed radial metallicity distribution for single stars in the GCS (using the new calibrations)
AMR for two pre-selected samples using different metallicity and age determination methods. All ages have errors below 25%. Top left: the VF05 sample, using our data. Top right: the Edvardsson et al. sample, using our data. Bottom left: the VF05 sample, using their data. Bottom right: same, using Takeda et al. ages. with that of our simulated catalogue, which has the flat age-metallicity distribution of Fig. 25, i.e. no correlation between age and metallicity in either the thin or the thick disk. However, we have added a radial metallicity gradient of ~0.09 dex/kpc for the thin-disk stars, close to the observed values (see, e.g., discussion in Sect. 6.2 of the GCS). Figure 28 shows that this reproduces the observed radial metallicity variation without any variation of metallicity with age.

We have deliberately made no attempt to fit the detailed structure in the \( R_a - [\text{Fe/H}] \) distribution. This depends on the complex structure of the distribution of the \( U \) and \( V \) velocities (see Figs. 29, 30 and GCS Fig. 20), which exhibits a multitude of kinematic groups not accounted for in a simple diffusion picture. As an example, the peak in [Fe/H] at \( R_a \approx 6.8 \) kpc is associated with the \( \zeta \) Herculis stream discussed in the GCS and again by Famaey et al. (2005) and Bensby et al. (2007).

11. Age-velocity relation and disk heating

As demonstrated earlier in this paper, our new calibrations cause no significant systematic changes in the velocities and ages of the GCS stars (apart from the overall ~10% age scale reduction). Thus, no major revision of the GCS results on the evolution of the kinematics of the disk with age is to be expected. However, the size of our sample allows us to examine that evolution in greater detail than was done in the GCS.

For this task, we select the cleanest sample of GCS stars, i.e. the single stars with \( \sigma(Age) < 25\% \) and with complete space velocity data. Note that, due to our improved age determination, there are now 4065 stars in this class as compared to 2852 in the original GCS – an increase by almost 50%.

Figure 29 shows the observed space velocity components as functions of age, while Figs. 30 and 31 show them in the \( U - V \) and \( V - W \) planes, separated into four groups by age. Like Figs. 20 and 30 of the GCS, they illustrate the significant substructure in the \( U \) and \( V \) velocity distributions that persists over a wide range of ages (see also Famaey et al. 2005 and the study of the Hercules stream by Bensby et al. 2007). In contrast, the \( W \) velocities show no deviation from a random distribution in any age group (Fig. 32), suggesting that different heating mechanisms are at work in the plane of the disk and perpendicular to it. However, it must also be noted that phase mixing is stronger for vertical motions due to the Galactic potential, and the orbital periods shorter, resulting in a more efficient smoothing of structure.

A detailed discussion of the mechanisms affecting disk star orbits in and perpendicular to the plane is beyond the scope of the present paper, but we can consider two basic questions, i.e. (i) whether the velocity dispersion of disk stars continues to increase during the lifetime of the disk or whether it shows signs of a plateau or saturation in some age interval, and (ii) what functional form appears appropriate for the rising parts of the age-velocity relation (AVR). For this discussion, we divide the
sample by age into 30 bins with equal numbers of stars (i.e. 135 in each bin), against the only 10 bins used in the GCS; this allows us to follow the evolution in greater detail.

Figure 33 shows the resulting AVR, which shows a smooth, general increase of the velocity dispersion with time in both $U$, $V$, and $W$. Fitting power laws while excluding the three youngest and three oldest bins, we find exponents of 0.38, 0.38, 0.54 and 0.40 for the $U$, $V$, $W$ and total velocity dispersions – slightly larger than the values derived in the GCS, as expected from the change in age scale.

This, however, is clearly not the full story of the phenomenon known as “disk heating”. If that term is taken to refer to an increase in the random motions of disk stars, it is clear from Fig. 30 that the present distribution of the $U$, $V$ velocities is not the result of pure “heating”; non-random processes are at work as well. Several possible mechanisms have been described in modern literature, based on detailed simulations, but all result in velocity dispersion increases with time that can be approximated by a power law. This is true, e.g. for the simulations that use transient spirals as the heating agent (De Simone et al. 2004) or produce velocity structure and heating of the disk by interaction between two spiral systems (Minchev & Quillen 2006) or between a spiral and the bar (Chakrabarty 2007).

To identify any underlying “pure” heating mechanism within the disk, one would have to remove the major non-random substructures, such as the Hercules stream or the Sirius-UMa, Coma, and Hyades-Pleiades branches (GCS; Famaey et al. 2005; Bensby et al. 2007). This, however, introduces a certain arbitrariness as to the choice of stars to be removed; and it appears more interesting to us to identify the cause(s) of the substructures that dominate the $U$, $V$ plane than to quantify any remaining minor effects.

On the other hand, the observed heating of the vertical ($W$) velocities, which show no signature of non-random mechanisms, is more efficient than found in simulations. E.g. Hänninen & Flynn (2002) find an exponent of only 0.26 using molecular clouds and need massive black holes to reproduce the observed heating rate, in agreement with several earlier studies. The black hole hypothesis is inconsistent with other observational data, but the extra vertical heating might be due e.g. to infalling satellites with dark matter substructure (Benson et al. 2004). In any case, further theoretical work on the heating mechanisms affecting the vertical velocities in the disk will have to satisfy the observational constraint illustrated in Fig. 33.

This conclusion contrasts with that by Quillen & Garnett (2001), who claimed that the heating of thin-disk stars saturates at a maximum velocity dispersion ~3 Gyr after the birth of a star; the oldest stars were assumed to belong to the thick disk and heated by a different mechanism. This led Freeman & Bland-Hawthorn (2002) to suggest that remnants of early mergers might still be traced as dynamical groups in the disk today (see Helmi et al. 2006, for an actual application).

Figure 33 shows no such saturation in our data, but the levelling-off of the velocity dispersion in the two oldest bins might be taken as weak evidence for a constant velocity
Fig. 33. Velocity dispersions vs. age for the GCS subsample of Fig. 29 (4065 single stars with \( r(Age) < 25\% \); new calibrations). The 30 bins have equal numbers of stars; the lines show fitted power laws. The 3 youngest and oldest bins have been excluded from the fit.

The thick disk of the synthetic sample is well visible in

\[
\begin{align*}
\sigma_{\text{tot}} & = \sigma_U + \sigma_V + \sigma_W \\
\sigma_U & = \sqrt{\sigma^2_U + \epsilon^2} \\
\sigma_V & = \sqrt{\sigma^2_V + \epsilon^2} \\
\sigma_W & = \sqrt{\sigma^2_W + \epsilon^2}
\end{align*}
\]

dispersion in the thick disk. When judging the merits of the two
results, it should be remembered that the sample discussed here is some 20 times larger than that discussed by Quillen & Garnett (2001) and the sampling errors correspondingly smaller.

Finally, we want to verify whether our age computation tech-
niques might bias the slopes seen in the age-velocity relation
(AVR). To do so, we have imposed a fixed AVR on our synthetic
catalogue, assuming purely Gaussian velocity distributions and
adopting the slopes of \( \sigma(U, V, W) \) vs. time as derived above. The thick disk contribution in the simulation is at the same level as in the observed sample, about 3% after applying the apparent-magnitude cutoff. We then recomputed the ages and age errors for all stars in the synthetic sample, using our new calibrations and retaining only stars with (new) ages better than 25%, sorted the stars into 30 equal-size bins, and recomputed the velocity dispersion in each bin.

The input and reconstructed AVRs are compared in Fig. 34. Symbols with error bars show the “observed” points with recomputed ages and age bins. As can be seen, all the reconstructed velocity dispersions are quite consistent with the input AVRs over the range 1.5–8 Gyr. There is thus no evidence for any error or bias being imprinted on the AVR from the age estimation process.

12. Thick disk vs. thin disk

In the literature, different criteria are used to distinguish thick-
disk stars from the more numerous thin-disk stars in the Solar
neighbourhood, based on kinematics, detailed chemical com-
position, or age. There is, however, no real consensus on what lim-
iting values to adopt in any of these parameters, and the allo-
cation of any individual star to either disk component is often
ambiguous. Questions of current interest include the fraction of
thick-disk stars in the GCS, we calculated the fraction of thick-
disk stars in the simulated catalogue with \( V \)-velocities below
\(-100\) km s\(^{-1}\) and \([\text{Fe/H}] > -1\). This sample contained 27% of the total number of thick-disk stars in the catalogue, and no thin-
disk stars were found in this velocity-metallicity domain. In the real, observed GCS we find 67 stars in this region. Thus, if we assume the same thick-disk velocity distribution as in the simu-
lation, we find a total of 248 thick-stars; as the total number of single stars with complete space velocities in the GCS is 8479, the thick-disk fraction is thus 2.9%.

As regards a possible AMR in the thick disk we note that,
interestingly, the “observed” AMR for the simulated thick-
disk stars in Fig. 25 shows a pronounced AMR of slope
\(-0.022\) dex/Gyr, although the input “true” AMR had a constant
metallicity between the assumed thick-disk age limits of 11 and
12 Gyr. This effect would have been even more pronounced if
our strict quality criteria on accepted ages had not been applied
(as in H06), or if the thick-disk sample had contained a small
fraction of stars with younger ages and/or higher metallicity.

Samples of field thick-disk stars can be constructed by com-
bining different membership criteria. For nearby field stars, a
kinematic criterion is most commonly used, based on a decom-
position of the local velocity distribution into Gaussians cor-
responding to the thin and thick disk and assuming values for
the asymmetric drift and \( U, V, W \) velocity dispersions for each.
Membership probabilities for either disk are then assigned for
each star, based on the observed space motion.

First, as shown in Fig. 30 and GCS Fig. 20, the actual lo-
cal velocity distribution is nothing like a two-Gaussian model;
in particular, the \( \zeta \) Herculis stream occupies a position near the
overlap between the thin and thick disks. Second, Fig. 34 shows
that the practice of assuming a single set of velocity dispersions
for the thin disk, regardless of age, ignores the effects of the
continuing dynamical heating of the disk. As general thin-disk
samples are typically dominated by relatively young stars (see
Figs. 23 and 29), the mean values of \( \sigma(U, V, W) \) will tend to be
underestimated, enhancing the probability that thin-disk outliers
will be classified as thick-disk stars.
If the thick disk is indeed very old, as is most commonly assumed, the kinematic parameters characterising the thin disk should be chosen to correspond to the oldest thin-disk stars (see Fig. 34). It is interesting to note that Bensby et al. (2004), who identify thick-disk stars with intermediate ages and chemical properties, assume significantly lower values of $\sigma(U, V)$ for the thin disk than Reddy et al. (2006), who find a smaller fraction of such stars and consider them to be outliers from the thin disk.

Given the inherent ambiguity of kinematic population indicators, the enhanced $[\alpha/Fe]$ ratio observed in thick-disk stars may be the best membership criterion for individual field stars. In order to study the AMD of the thick disk from the cleanest possible sample of stars, we therefore selected all stars in common between the GCS and those kinematically classified thick-disk stars from Reddy et al. (2006) that also have $[\text{Ti/Fe}] > 0.25$.

Figure 35 shows the AMD for this “clean” thick-disk sample, using our new ages. We see a tight grouping of stars with ages around 11 Gyr and $[\text{Fe/H}] \sim -0.55$, and no trace of a slope. Taken together, Figs. 25 and 35 put into question the claims of a significant age-metallicity relation in the thick disk by, e.g. H06 or Bensby et al. (2004).

Note that a strong, spurious correlation of age with metallicity would result if the Padova isochrones had not been corrected for the increasing discrepancy between the original isochrones and the observed unevolved stars at decreasing metallicity (see Sect. 2). This is also the case if the $\alpha$-enhancement of metal-poor stars is ignored when choosing the $Z$ parameter of the models.

13. Conclusions

We have redetermined the basic calibrations used to infer astrophysical parameters for the GCS stars from $ubvy$ photometry. The result is a substantial improvement in the determination of effective temperatures, especially for the hotter stars, and of absolute magnitudes (i.e. distances), as well as minor corrections to $[\text{Fe/H}]$. The GCS reddening calibration appears to be essentially correct. These new results are obtained by drawing on the large body of 2MASS K photometry, high-resolution spectroscopic abundance analyses, and accurate Hipparcos parallaxes that are now available.

Using the improved astrophysical parameters, we have recomputed the ages and age error estimates for the GCS sample (Table 1). In the process, we have compared results from a variety of stellar models, finding no large differences between models for typical GCS stars. We have also recomputed the temperature corrections needed for the models to agree with the observed unevolved main sequence at metallicities below solar.

The resulting ages correlate well with those published in the GCS, but are on average ~10% lower. The recent ages by VF05 for ~400 stars in common are some 10% lower still, while those by Takeda et al. (2007) are essentially in perfect agreement with ours, although they were also based on the spectroscopic temperatures and metallicities by VF05. This independent verification places the determination of isochrone ages on a very firm basis, provided adequate precautions are taken.

We note that, because of a small offset in the GCS $ubvy$ photometry for the Hyades stars and the non-standard He abundance of this cluster, the Hyades cannot be used to check metallicity or age scales for field stars such as those in the GCS, as assumed by H06. The revised results given here for Hyades and Coma stars are based on standard photometry whenever available.

The revised $[\text{Fe/H}]$ values change the observed metallicity distribution only marginally; it is still in strong disagreement with the prediction of closed-box galactic evolution models.

In preparation for the discussion of Galactic relations involving stellar ages, notably the age-metallicity and age-velocity diagrams, we have performed extensive simulations of the effects of our selection and computation procedures by applying them to synthetic catalogues with properties closely resembling those of the GCS, but with a variety of specified intrinsic properties, such as the AMR and AVR. We find that our methods faithfully recover the input relations within the observational errors, without introducing spurious trends or other systematic effects.

The observed AMR retains the general features of that of the GCS, i.e. little or no variation in mean metallicity with age in the thin disk, plus an admixture of perhaps 5% thick-disk stars, and with a large and real scatter in $[\text{Fe/H}]$ at all ages. We find no evidence for a significant AMR in the thick disk. Note that these conclusions are only robust when backed by careful end-to-end simulations of the properties of the sample and associated selection criteria (notably the limits by apparent magnitude...
and the blue colour cutoff), and by meticulous attention to the
details of the computation of the stellar ages and their uncertain-
ties. Investigations using simpler approaches (e.g. H06 or Reid
et al. 2007) may well reach different conclusions.

A significant result of the GCS was the demonstration that
the dynamical heating of the thin disk continues throughout its
life. We confirm this from our revised data set, and with sub-
stantially higher time resolution than in the original GCS. Our
simulations also confirm that no bias has been introduced in the
slope of the AVR for the individual U, V, W velocity components
by our age computation technique.

We conclude that kinematic parameters taken to represent
the thin disk in thick-disk/thin-disk separations based on ob-
served velocities should be chosen to correspond to the oldest
thin-disk stars. Using average values for thin-disk samples domi-
nated by stars much younger than the thick disk may lead to con-
tamination of the thick-disk samples by kinematic outliers from
the thin disk, especially when such non-Gaussian kinematic fea-
tures as the Hercules stream are present.

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