Steps toward interstellar silicate mineralogy

VII. Spectral properties and crystallization behaviour of magnesium silicates produced by the sol-gel method

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Abstract. Amorphous silicate particles are generally assumed to be the main dust component in the envelopes of oxygen-rich evolved stars and may be considered the precursors of the pure crystalline enstatite and forsterite particles detected by ISO. We present optical constants in the broad wavelength range 0.2–500 $\mu$m for a unique series of pure amorphous Mg-silicates (Mg/Si in the range 0.7–2.4). They have been prepared by the sol-gel process, a chemical technique based on the condensation of Mg- and Si-hydroxides in a liquid phase. The salient feature of these Mg-silicates is the very small content of Si–OH bonds in the silicate network, which considerably reduces the activation energy of crystallization and, thus, decreases the temperature threshold for crystallization as well as crystallization time. The astrophysical relevance of our sol-gel silicates is shown by a comparison of optically thin model spectra based on dust emissivities with ISO-SWS spectra of AGB stars and with 10 $\mu$m emission profiles of such stars obtained by ground-based spectroscopy. As paradigmatic cases of AGB spectra with respect to the appearance of the silicate bands, TY Dra (slender bands and deep trough between them) and R Cas (broad bands and widely filled-up trough) were used, for which ISO-SWS spectra are available. The dust emissivity derived from TY Dra can be excellently reproduced by the models, suggesting that the dust grains consist indeed of pure amorphous Mg-silicates. Satisfactory agreement was also found with the mean 10 $\mu$m profiles of some groups of AGB stars and supergiants. Spectra with strong dust emission in the silicate trough like R Cas require additional contributions by other dust components, probably oxides. A rough orientation on the spectral properties of such potential trough opacity contributors has been obtained by subtracting a pure silicate spectrum (TY Dra) from a spectrum with a nearly filled trough and a less pronounced 20 $\mu$m band (R Cas). In agreement with other amorphous silicates, the spectral index of the new silicate analogues amounts to $-2$.

Key words. infrared: stars – methods: laboratory – infrared: ISM – stars: circumstellar matter – line: identification

1. Introduction

On the basis of ground-based observations and satellite observations (IRAS-LRS spectra), it seemed that cosmic dust silicates were predominantly amorphous. The detailed investigation of the profiles of the 10 and 18–19 $\mu$m silicate vibrational bands in comparison with laboratory analogs provided a similar result (Dorschner & Henning 1986, 1995; Dorschner 1999). Additional evidence for the formation of amorphous silicates was provided by non-equilibrium condensation experiments resulting in “chaotic silicates” (Nuth 1996). Consequentially, up to now, amorphous silicates with compositions reflecting the cosmic elemental abundance and the derivation of their optical constants were in the focus of our interest (Jäger et al. 1994; Dorschner et al. 1995; Mutschke et al. 1997). This led to a rather exhaustive characterization of amorphous Mg–Fe-, Mg–Al-, Ca–Al-, and Na–Al-silicates, but also to a relative neglect of pure Mg-silicates. The present paper is a contribution to fill this gap.

Spectra obtained by the Infrared Space Observatory (ISO) have surprisingly pointed to clear evidence of crystalline silicates. Observational evidence for the presence of crystalline silicates was found in the spectra of circumstellar dust around Herbig Ae/Be stars (Waelkens et al. 1996), low-mass evolved stars with high mass-loss including planetary nebulae (Waters et al. 1996; Justtanont et al. 1996) and Luminous Blue Variables (LBVs) (Waters et al. 1997). The circumstellar spectra of crystalline silicates exhibited great similarity with the spectrum of comet Hale-Bopp (Crovisier et al. 1997). From the comparison between laboratory spectra of pyroxene- and...
olivine-type silicates and astronomical spectra, it has been concluded that only completely iron-free magnesium silicates like forsterite and enstatite can account for the observed band positions (Jäger et al. 1998; Bowey et al. 2002; Molster et al. 2002b).

Recently, forsterite has been found among the first presolar silicates that were identified in interplanetary dust particles (Messenger et al. 2002) due to a large 17O excess and moderate 18O depletion (which is characteristic of H burning). This forsterite grain has been proposed to originate from an AGB star. Other silicate grains enriched in 17O and 18O point to an origin in high metallicity stars and type II supernovae. Due to their small sizes, chemically and isotopically similar grains could not be fully characterized, but it has been shown that they are rich in O, Si and Mg.

The main dust component in different astronomical environments, though, remains amorphous magnesium-iron silicates (Molster et al. 1999; Demyk et al. 1999; Bouwman et al. 2001; Molster et al. 2002a,b). The crystalline magnesite silicates have probably been formed by thermal annealing. The conversion of amorphous magnesium silicates to crystalline components can be explained by means of annealing processes occurring close to the condensation zones (Hallenbeck et al. 1998; Fabian et al. 2000). However, the annealing temperature necessary to convert the amorphous into the crystalline silicates at a timescale of hours to days is 1000 K. Unless the crystalline Mg-silicates can condense directly from the gas phase, nearly iron-free amorphous silicates should be the precursors of crystalline forsterite and enstatite. Additionally, Rietmeijer et al. (1999) demonstrated the formation of either pure magnesium or iron silicates in vapor-phase condensation experiments. In particular, no mixed Mg–Fe-silicate grains have been produced in the condensation experiment.

Therefore, we concentrated our experiments on amorphous, iron-free magnesium silicates. This does not mean that we consider Mg-silicates as the only silicate dust component. Mixed Mg–Fe-silicates can be formed after the condensation of Mg-silicates by solid-state reactions with iron or iron-containing species.

With some exceptions (Dorschner et al. 1995; Scott & Duley 1996; Hallenbeck et al. 2000), optical constants of amorphous Mg-silicates are rather rare in the literature. It is the aim of this paper to provide optical data of amorphous silicates with varying MgO/SiO2 ratios which cover the whole wavelength range important for the interpretation of ISO spectra. This investigation includes Mg9Si2O7, MgSiO3, Mg1.5SiO1.5, Mg2SiO4, and Mg2.5SiO4. Two of the produced nonstoichiometric materials correspond to the metastable eutectic Mg-silicate compositions Mg3Si2O7 and Mg2SiO22 reported to condense preferably in the magnesium silicate binary system by Rietmeijer et al. (1999). Furthermore, the influence of the Mg/Si ratio on band positions and strength ratios of the 10 and 20 µm bands has been studied. The spectroscopy is supplemented by a careful analytical characterization of the samples.

The sol-gel technique used for the synthesis of magnesium silicate samples is not only interesting for the production of high-melting silicates. It also provides materials bearing chemical properties expected for cosmic silicates. In fact, the formation of magnesium silicates with a small content of isolated Si–OH or Mg–OH bonds can be considered as highly probable, since H2O, the most abundant oxygen-bearing molecule, participates in the formation of olivine- and pyroxene-type silicates (Gail & Sedlmayr 1998). These silicate materials show dissenting material properties in comparison to the commonly produced silicates, particularly with regard to their crystallization behaviour. Therefore we completed our experiments with investigations of the annealing behaviour of the synthesized magnesium silicate samples.

2. Experimental

The sol-gel process is based on the chemical polymerization of silicates in a liquid phase at low temperatures. Metal organic compounds like tetraethoxysilane (TEOS) and magnesium methylenate Mg(OCH3)2 served as precursors. The metal organic materials have to be soluble in water and alcohol. The polymerization runs in two steps. The first step is the hydrolysis of the precursors and the formation of hydroxides, followed by the condensation of the hydroxides (Si(OH)4 and Mg(OH)2). It leads to the formation of a three-dimensional magnesium silicate network. Hydrolysis and condensation are chemical equilibrium reactions which run in competition. In order to avoid phase separations and the formation of inhomogeneous silicate material, it is important to choose silicon and magnesium components with nearly the same hydrolysis and condensation rates.

Compositions up to 0.7 mol MgO in the system have been synthesized with magnesium chloride or magnesium nitrate and tetraethoxysiloxane. Metal oxide (MeO) contents larger than 50 Mol% MgO (x ≥ 1) cannot be produced from anorganic magnesium compounds since they lead to the precipitation of the salt during the reaction (Burlitch et al. 1991).

In order to produce amorphous magnesium silicates Mg2SiO2+x (for x = 1...2.4), we used an advancement of the H2O2-assisted sol-gel reaction of magnesium methylenate (Mg(OCH3)2) and TEOS based on the synthesis described by Burlitch et al. (1991) (see also Agladze et al. 1996). The hydrogen peroxide serves as a proton provider and a catalyst. The synthesis has to be performed under a purified Ar-atmosphere to avoid the precipitation of insoluble Mg(OH)(OCH3) and phase separation of MgO. The removal of the solvents methanol and water from the produced gels has been run in a rotary evaporation at reduced pressure. The remaining magnesium silicate powder was heated in order to achieve a densification of the silicate framework and to remove the porosity of the grains. The amorphousness of the samples has been proven by means of X-ray diffraction. The stoichiometry, purity, and phase homogeneity as well as the densification process could be determined by using the Transmission Electron Microscope (TEM) and the Scanning Electron Microscope (SEM) combined with the Electron Dispersive X-ray (EDX) analysis. The samples’ compositions were exactly determined by EDX measurements. The compositional results from EDX were carefully compared with corresponding well-analyzed standard samples comprising crystalline and amorphous materials with compositions...
from Mg₈₀₅SiO₂₋₅...Mg₂SiO₄. In case of two samples, wet-chemical analyses were also performed in order to confirm our EDX results. The homogeneity and purity of the samples were additionally checked by TEM analysis combined with EDX. For an overview of the compositions, see Table 1.

The final powder products have been pressed into very dense pellets at pressures of about 200 t/cm² load. The pellets were embedded in an epoxide resin and their surfaces were ground and polished. Specular reflectance measurements, at nearly normal incidence, have been performed at the embedded and polished samples from the ultraviolet (0.2–200 µm). In the high frequency range a Perkin Elmer Lambda 19 UV/VIS/NIR spectrometer, covering the region between 0.2 and 2.5 µm, was applied. The spectral resolution depends on the wavelength and was 0.5 nm in the UV/VIS range. An aluminium mirror of calibrated reflectance was used as reference. The IR reflectance measurements in the range between 2 and 300 µm were performed by means of a Bruker FTIR spectrometer 113v. In this spectral region a gold mirror reference came into operation. The spectral resolution in the IR was 2 cm⁻¹ which is sufficient for room temperature measurements (Bowey et al. 2001). In the IR and FIR a DTGS/KBr and DTGS/PE detector in combination with KBr and mylar beamsplitter were used, respectively. The UV/VIS/NIR and IR spectra were merged together without an offset or scaling of the curves. A part of the powder samples has been used for transmission measurements of KBr and PE pellets in the IR range (2 to 300 µm). For this purpose, grains smaller than 1 µm were produced by additional grinding and sedimentation of the grains in water-free alcohol.

3. Results
3.1. Spectral properties

The results of the transmission measurements of the magnesium silicate sol-gel sample are shown in Fig. 1. In the binary system MgO-SiO₂, the effect of the MgO/SiO₂ ratios on the position and shape of the Si–O vibrational bands is demonstrated. Amorphous magnesium silicates typically show two broad bands at about 10 and 20 µm corresponding to Si–O stretching and bending vibrations. The large width of both bands results from a distribution of bond lengths and angles within the amorphous structure. The 20 µm band is additionally broadened due to the coupling of the Si–O bending to the Mg–O stretching vibration in this spectral region. The coupling has been reported e.g. by Gervais et al. (1987) leading to a combined band of a huge width. The incorporation of Mg into the silicate network can occur in two different ways, as network former (4-fold coordination) and/or as network modifier (6-fold coordination).

The appearance of a third band at 12.5 µm, visible in the SiO₂ spectrum, is typical for SiO₂ and disappears at a MgO content of 0.5. The band can be assigned to the symmetric stretching vibration of Si–O–Si bonds or to ring structures (Fuxi 1979; Brinker & Scherer 1990). The small double band at about 7 µm is caused by traces of magnesium carbonate which can be formed during grinding. In order to separate large grains (≤1 µm) from the powder sample we used the sedimentation technique which lead to a slight enrichment of the carbonate in the sample because of the smaller specific weight of the carbonate grains. By comparison of the integral intensity of the 7 micron band with selected carbonate samples we could roughly estimate the carbonate content to 6 mol%. The carbonate impurity was only found in the ground and sedimented magnesium silicate sample which was used for the transmission measurement and is not an impurity in the reflection samples.

The position of the Si–O stretching vibration is shifted from 9 µm for the pure SiO₂ to 9.7 µm for MgSiO₃ and 10.25 µm for the Mg₂SiO₄. The influence of the MgO content on the position of the Si–O bending vibration groups is difficult to observe since the widths of the 20 µm bands are much stronger with increasing MgO content. The position of this feature seems to remain constant. This effect is related to morphological and matrix effects in the KBr. The KBr environment leads to a broadening and a long-wavelength shift of both peaks. However, the matrix influence is much stronger for the very broad 20 µm bands. We assume that different bonds within the silicate network such as Si–O and Mg–O will be differently influenced by KBr.

### Table 1. Composition of the magnesium silicate samples used for reflection measurements derived by EDX measurements in the SEM and TEM.

<table>
<thead>
<tr>
<th>Sample name</th>
<th>MgO wt%</th>
<th>SiO₂ wt%</th>
<th>Me–OH</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg₀.7SiO₂</td>
<td>31.12</td>
<td>67.74</td>
<td>0.87</td>
</tr>
<tr>
<td>Mg₁SiO₂</td>
<td>39.79</td>
<td>59.07</td>
<td>1.14</td>
</tr>
<tr>
<td>Mg₁₂SiO₆</td>
<td>50.31</td>
<td>48.71</td>
<td>0.98</td>
</tr>
<tr>
<td>Mg₂SiO₄</td>
<td>56.45</td>
<td>42.33</td>
<td>1.22</td>
</tr>
<tr>
<td>Mg₄SiO₄</td>
<td>61.34</td>
<td>37.89</td>
<td>0.77</td>
</tr>
</tbody>
</table>

Fig. 1. IR transmission spectra of magnesium silicates in the binary system MgO-SiO₂ for various MgO/SiO₂ ratios. The average particle size is less than 1 µm. For the sake of clarity, the curves have been successively shifted by 0.4.
3.2. Reflectance spectra

Two typical reflectance spectra of magnesium silicates are shown in Fig. 2. There are two pronounced silicate vibrational bands at 1000 and 500 cm\(^{-1}\) in all spectra discernible. In the FIR the spectra behave differently. Mg\(_{0.7}\)SiO\(_{2.7}\) shows a continuous decline of reflectivity with decreasing wavenumber starting at about 460 cm\(^{-1}\). In the spectra of the samples MgSiO\(_3\) up to Mg\(_{2.4}\)SiO\(_{4.4}\) a nearly constant reflectivity can be observed in the FIR, which can be seen in the reflectance spectrum of Mg\(_{2.4}\)SiO\(_{4.4}\) as a representative of this group. This FIR behavior will be discussed in the next section. The rising MgO content in the silicates also results in a shift of the 10 and 20 \(\mu\)m bands and an increase of band widths. Mg\(_{2}\)SiO\(_4\) displays a clear long-wavelength shift of the Si–O stretching band and the broadening of the Si–O bending vibration compared to Mg\(_{0.7}\)SiO\(_{2.7}\). The general reflectivity from the UV up to the FIR is as well growing with increasing MgO/SiO\(_2\) ratios in the samples. This is especially evident in the VIS and NIR ranges where the reflectivity is nearly constant. The UV reflectance is stamped by a strong rise of the reflectivity beyond 200 nm (50 000 cm\(^{-1}\)) due to electronic interband transitions. This behavior is typical for pure magnesium silicates since no absorbing elements (transition elements) with electronic transitions in the VIS and NIR region are contained. Very small structures in the reflectance spectra at about 3660 cm\(^{-1}\) are caused by O–H stretching vibrations of isolated Si–OH or Mg–OH groups.

3.3. Derivation and characteristics of the optical constants

Optical constants \((n, k)\) of the produced stoichiometric and nonstoichiometric magnesium silicates have been derived from the reflection measurements (see Fig. 3). For Mg\(_{0.7}\)SiO\(_{2.7}\) the Lorentz-oscillator fit method was exclusively used to determine the complex refractive index in the whole measurement range from the UV up to the FIR. For the other magnesium silicates \(n\) and \(k\) were evaluated by a combination of Kramers-Kronig analysis (KKR) and Lorentz-oscillator fit method. Concretely, we performed a KKR analysis in the IR range from 2 to 200 \(\mu\)m. The FIR tail starting from 200 \(\mu\)m and the NIR tail starting from 2 \(\mu\)m were extrapolated assuming that the reflectivities converge to constant values at zero and infinite wavelengths, respectively. The fulfillment of the causality criterion

\[
\int_{-\infty}^{\infty} \ln(R(\omega)/R(\infty))d\omega = 0
\]

was verified. Note that most of the resulting \(n(\omega)\) spectra (see Fig. 3) are characterized by a monotonous decrease between \(\omega = 0\) and the shortest resonance frequency, or, in other words, by a monotonous increase of \(n(\lambda)\) between the largest resonance wavelength and \(\lambda \to \infty\). It can be analytically shown that for strongly damped oscillators – i.e. for a damping constant \(\Gamma_\text{le}\) of the lowest energy oscillator which fulfills the condition \(\Gamma_\text{le} > \omega_\text{le}\) (where \(\omega_\text{le}\) is the lowest energy oscillator frequency) – \(n\) must indeed monotonously decrease between \(\omega = 20\) and \(\omega = \omega_\text{le}\). For one of our amorphous Mg silicates, namely Mg\(_{0.7}\)SiO\(_{2.7}\), it turned out that \(\Gamma_\text{le} < \omega_\text{le}\); therefore, its \(n\) curve resembles the “canonical” shape of a narrow Lorentz oscillator profile. By contrast, all the other samples represent the case of the very strongly damped oscillator system with \(\Gamma_\text{le} > \omega_\text{le}\). The observed strong broadening of the 20 micron bands of amorphous magnesium silicates is on one hand caused by the disorder in an amorphous solid leading to a distribution of bond angles and distances and therefore to a superposition of many slightly different vibrational frequencies but on the other hand by the coupling of the Si–O bending to the Mg–O stretching vibration in this spectral region. The coupling, reported by Gervais et al. (1987), give rise to the formation of a combined band with a huge width ranging from about 200 to 700 cm\(^{-1}\).

In the astronomical literature, the properties of these very broad oscillator profiles have been rarely addressed hitherto. However, the optical constants derived for different amorphous cosmic dust analogs are generally characterized by the condition \(\Gamma_\text{le} > \omega_\text{le}\) and the corresponding broad profile (see e.g. Eriksson et al. 1981; Draine & Lee 1984; Ossenkopf et al. 1992; Dorschner et al. 1995; Begemann et al. 1997).

KKR analysis could not be used in the UV/VIS/NIR region, since at the short wavelength side the spectra end in the region of electronic transitions, whereas the KKR method requires a negligible absorption at both spectral limits. Therefore, the Lorentz-oscillator fit method has been applied to calculate the \(n\) and \(k\) values below 14 \(\mu\)m. As for the applicability of this method, we refer to the monographs by Wooten (1972) and Bohren & Huffman (1983), who show that in the UV/VIS range, Lorentz oscillator fits can be used to model all direct interband transitions in insulators. In order to model the tail of the electronic transitions in our magnesium silicates we used 2 oscillators, a broad and very strong one at about 60 000 cm\(^{-1}\) representing the expected strong electronic transitions below 190 nm and being mainly responsible for the refractive index in the visible. A second oscillator at about 53 000 cm\(^{-1}\) was used to model the fine structure of the absorption edge in the.
range between 210 and 190 nm for each individual composition of magnesium silicates. The 10 \( \mu \text{m} \) IR band has been included in the modeling using 2–4 oscillators in order to achieve an overlap of the results obtained by KKR and Lorentz-oscillator fitting. It turned out that Lorentz-oscillator model was better suited to represent the tail of the infrared bands below 8 \( \mu \text{m} \). Therefore, we merged both results at this spectral position.

The validity of our calculations is demonstrated by the comparison between the original reflectance spectra of the silicates and the calculated reflection determined from the optical constants shown in Fig. 3. The measured and calculated reflection curves, displayed in Fig. 2, show a very good coincidence. Only small deviations in the band region of the \( \text{Mg}_0 \cdot 7 \text{SiO}_2 \cdot 7 \) spectrum can be seen, which result from the difficulty to reproduce the broad vibrational bands of amorphous samples with Lorentz-oscillators. Efimov (1999) has compared quantitative analysis methods of IR spectra of various inorganic glasses to determine optical constants and found that the Kramers-Kronig transformation and the Lorentz-oscillator fit method provide practically coinciding optical constants. KKR can have advantages compared to the oscillator-fit method since KKR involves no microphysical model for the response of solid material to the electromagnetic field. That means that KKR is not correlated to any particular band shape, which guarantees the practicality of this relation to spectra independent of the frequency range and the materials’ properties. Therefore, KKR is a generally accepted method for the determination of optical constants of solids including amorphous materials (Gaskell & Johnson 1976; Kamitsos et al. 1995; Hudgens & Martin 1996; Aasland et al. 1997).

The knowledge of the optical constants enables us to calculate the absorption cross section per unit volume of grains with different morphology (see Table 2 and Fig. 12). The calculated absorption cross sections have shown that MgO influences the position of the 10 and 20 \( \mu \text{m} \) band. With increasing MgO content, the 10 \( \mu \text{m} \) band is shifted to longer wavelengths, whereas the 20 \( \mu \text{m} \) band is shifted in the opposite direction. This result is in agreement with the findings of McMillan (1984), who demonstrated the influence of alkaline and alkaline earth oxides on the positions of the stretching and bending Si–O modes in silicate glasses and melts. The positions of the 10 and 20 \( \mu \text{m} \) bands are sensitive to the number of bridging oxygen atoms and therefore to the degree of polymerization of \( \text{SiO}_4 \) tetrahedra in the amorphous silicate network. The 10 \( \mu \text{m} \) bands are broadened due to the superposition of individual bands of Si–O bonds, whereas the huge increase of the 20 \( \mu \text{m} \) band widths’ are caused by superposition of Si–O and Mg–O bonds, varying in bond lengths and angles. Differences to measured transmission spectra of small grains in KBr, especially in the range of the 20 \( \mu \text{m} \) band, result from matrix and morphological effects in the KBr pellets.

### 3.4. Comparison with other amorphous magnesium silicates

Figure 4 shows the comparison of our \( n \) and \( k \) data with optical data of pyroxene and olivine glasses produced by melting and quenching techniques (Dorschner et al. 1995). The spectral behaviour in the UV/VIS range is influenced by the

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**Table 2.** Diagnostic spectral parameters of the 10 and 20 \( \mu \text{m} \) bands of amorphous magnesium silicates based on calculations of the absorption cross section per unit volume \( C(V) \) (in \( \text{cm}^{-1} \)) for small spheres (Sph.) and a continuous distribution of ellipsoids (CDE) for particles in the Rayleigh limit. \( \lambda \) and \( A \) represent the peak position in \( \mu \text{m} \) and the absorption cross section per unit volume \( C(V) \) in \( \text{cm}^{-1} \), respectively. \( W \) stands for the FWHM of the bands. The band ratio has been calculated by dividing the intensity of the 20 \( \mu \text{m} \) band by the intensity of the 10 \( \mu \text{m} \) band.

<table>
<thead>
<tr>
<th>Comp.</th>
<th>10 ( \mu \text{m} )</th>
<th>20 ( \mu \text{m} )</th>
<th>band ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( \lambda_{10} ) ( \mu \text{m} )</td>
<td>( \lambda_{20} ) ( \mu \text{m} )</td>
<td>( A_{10} ) ( \mu \text{m} )</td>
</tr>
<tr>
<td>----------------</td>
<td>------------------------</td>
<td>------------------------</td>
<td>------------</td>
</tr>
<tr>
<td>( \text{Mg}_0 \cdot 7 \text{SiO}_2 \cdot 7 )</td>
<td>9.15 9.20</td>
<td>20.21 20.86</td>
<td>1.41 1.56</td>
</tr>
<tr>
<td>( \text{Mg}_2 \text{SiO}_3 )</td>
<td>9.26 9.37 6165 6642 1.88 2.10</td>
<td>19.41 20.22 2520 3023 8.53 10.0</td>
<td>0.41 0.46</td>
</tr>
<tr>
<td>( \text{Mg}_3 \text{SiO}_4 )</td>
<td>9.62 9.74 6725 6992 1.99 2.41</td>
<td>18.11 18.70 3413 3825 5.61 5.68</td>
<td>0.52 0.57</td>
</tr>
<tr>
<td>( \text{Mg}_5 \text{Si}_3 \text{O}_5 )</td>
<td>9.80 9.91 6923 6398 2.05 2.43</td>
<td>17.42 17.90 3165 3698 10.0 13.0</td>
<td>0.47 0.50</td>
</tr>
<tr>
<td>( \text{Mg}_7 \text{Si}_5 \text{O}_7 )</td>
<td>10.07 10.2 4778 5198 2.66 2.80</td>
<td>17.25 17.76 4255 4395 9.83 13.1</td>
<td>0.82 0.84</td>
</tr>
</tbody>
</table>

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**Fig. 3.** Optical constants of amorphous magnesium silicates of varying composition derived from reflection measurements by KKR and Lorentz oscillator fit methods. The \( n \) and \( k \)-data files can be taken from the internet homepage of the Astrophysical Institute and University Observatory Jena (http://www.astro.uni-jena.de/Laboratory/Database/silicates.html).
presence of transition metal ions. The incorporation of iron in glasses leads to a series of electronic transitions from the UV up to the NIR range which is well discernible in the iron-containing glasses in Fig. 4. It is well known that in pure magnesium silicate glasses the UV absorption edge is determined by the interaction of UV radiation with electrons of bridging and non-bridging oxygen. The strong and rather broad absorptions at wavelengths smaller than 200 nm are caused by electronic transitions, concretely, by excitons and interband transitions between the 2p orbitals of oxygen and the 3d orbitals of silicon (Liepmann & Neuroth 1995; Fuxi 1979). Since the non-bridging oxygen are less tightly bound to silicon than the bridging oxygens their electronic transitions occur at longer wavelengths than those of bridging oxygen.

The UV absorption edge of the sol-gel product MgSiO$_3$ is shifted to shorter wavelengths (200 nm) compared to the iron-free MgSiO$_3$ glass. The short-wavelength shift of the UV absorption edge is probably related to the incorporation of Mg$^{2+}$ ions into the silicate as a network former avoiding the formation of non-bridging oxygen. This is also confirmed by the fact that the MgO content in the sol-gel silicates does not have any influence on the absorption edge. Small differences between the samples can be raised by varying Si–OH bonds. The $n$ and $k$ values of the sol-gel silicates are distinctly smaller than those of magnesium silicate glasses, resulting in differences of the absolute values of the absorption coefficients for spheres and CDE. The position of the 10 $\mu$m band is shifted to shorter wavelengths by 0.06 $\mu$m. The calculated bending mode position for MgSiO$_3$ spheres in the Rayleigh limit is shifted to longer wavelengths (19.4 $\mu$m) compared to the calculated position for MgSiO$_3$ glass spheres (17.7 $\mu$m; Dorschner et al. 1995).

However, the comparison with optical data of a Mg$_2$SiO$_4$ film (Scott & Duley 1996) produced by gas phase condensation shows a good agreement with the optical data of Mg$_2$SiO$_4$ produced by the sol-gel technique (see Fig. 5). There is a satisfactory agreement in the run of the $n$ and $k$ curves especially in the UV/VIS range. Slight differences, according to structural variety in the amorphous structure of the differently produced magnesium silicates, are discernible in the MIR range. For spherical particles the data by Scott & Duley (1996) yield maxima of the absorption cross section at 10.1 and 18.6 $\mu$m compared to our values of 9.8 and 17.4 $\mu$m (see Fig. 6). The comparison between the differently produced magnesium silicates demonstrates the existence of varying amorphous material with differences in the internal structures. Based upon these results, one has to conclude that the amorphous state of any magnesium silicate is not unique but there exist different possibilities for structural arrangements of subunits in the amorphous silicate structure, similar to the different structures of amorphous carbon with strongly varying optical properties.

One can draw the conclusion that just as in the case of amorphous carbon, different structures with varying optical constants may exist and that the short-range as well as
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Table 3. Activation energies of crystallization \( E_a/k \) determined for differently produced magnesium silicates.

<table>
<thead>
<tr>
<th>Material</th>
<th>Material properties</th>
<th>( E_a/k ) (K)</th>
<th>Crystalline phase</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg2SiO4</td>
<td>Smoke, inhomogeneous</td>
<td>39 100</td>
<td>forsterite</td>
</tr>
<tr>
<td>MgSiO3</td>
<td>Smoke, inhomogeneous</td>
<td>42 040</td>
<td>forsterite, tridymite</td>
</tr>
<tr>
<td>MgSiO3</td>
<td>Glas, homogeneous, grain sizes ( \leq 1 \mu m )</td>
<td>40 100–43 300</td>
<td></td>
</tr>
<tr>
<td>( Mg_{0.09}Fe_{0.01}SiO_3 )</td>
<td>glass, homogeneous, grain sizes ( \leq 1 \mu m )</td>
<td>38 525</td>
<td>enstatite</td>
</tr>
<tr>
<td>Mg-silicate</td>
<td>Sol-gel, homogeneous, Me–OH bondings</td>
<td>26 600–31 700</td>
<td>enstatite</td>
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<tr>
<td>MgSiO3</td>
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<tr>
<td>( Mg_{1.5}SiO_3 )</td>
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<tr>
<td>( Mg_{1.8}SiO_3 )</td>
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<td>Mg2SiO4</td>
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<td>Mg2.4SiO4</td>
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<td>Mg2.6SiO4</td>
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The results of the annealing experiments are summarized in Table 3. For the sake of comparison, the table additionally contains activation energies of differently produced silicate materials like glasses and smokes (Fabian et al. 2000). The activation energies \( E_a/k \) of magnesium silicates produced by sol-gel synthesis amount to values between 26 600 and 31 700 K corresponding to about two thirds of the crystallization activation energy of Mg-silicate glasses and smokes. Corresponding annealing temperatures were between 723 and 873 K. Annealing experiments with sol-gel produced magnesium silicates demonstrate that \( E_a \) is independent of the composition of the materials. This unusual behaviour has its seeds in a content of non-associated Si–OH and Mg–OH bonds stemming from the sol-gel synthesis.

Non-associated Si–OH and Mg–OH bonds give rise to a narrow band at about 2.7 \( \mu m \) due to O–H stretching vibrations (see Fig. 7). These groups can remain from the condensation process. However, the band position of 3670 cm\(^{-1}\) rather points to an excess of Si–OH bonds (Iler 1979a; Morimoto et al. 1999) compared to Mg–OH since the latter have a band at 3700 cm\(^{-1}\) (Mitra 1962; Shinoda et al. 2002). In case of reduced temperature crystallization this narrow band at 2.7 \( \mu m \) has been found in addition to the first spectroscopic hints to crystallization due to a content of non-associated O–H bonds in these samples. The content of these O–H bonds has been spectroscopically determined by comparison of the 2.7 \( \mu m \) band with a sample of well known Si–OH content. The latter does not exceed 1.3 wt% that remained from the sol-gel synthesis. Isolated O–H bonds in a magnesium silicate framework reduce the formation of oxygen bridges between the SiO\(_4\) tetrahedra and form non-bridging oxygen. The increase of non-bridging oxygen leads to a decrease of the viscosity (Scholze 1988). The influence of OH groups is comparable to that of alkaline ions which act as network modifier introducing non-bridging
oxygen (Iler 1979b). This is easy to understand since the proton \( H^+ \) of the OH group can be considered like a alkaline ion. Thereby the viscosity of the magnesium silicates is decreased and the crystallization temperature can be lowered by 200 to 300 K (cf. Fig. 7). That means that the crystallization temperature is dependent on the Si–OH content. A further incorporation of Si–OH does not lead to a further decrease of the crystallization temperature. The temperature of crystallization can be decreased from 1000 K for Si–OH free material to 730 K for magnesium silicate containing 1.3 wt% Si–OH bonds.

A similar effect can be observed in the case of Fe incorporation. The incorporation of only 5 Mol% Fe reduces the activation energy \( E_a/k \) by about 2000–3000 K in comparison with the iron-free magnesium silicate. This is due to the decrease of viscosity beyond the transformation range of the amorphous material. The calculation of the activation energy enables us to compare the crystallization behaviour of different materials and to estimate time scales necessary for crystallization at different temperatures. For example, a magnesium silicate without Si–OH groups needs \( \tau = 3300 \text{ yrs} \) for crystallization at a temperature of 750 K, whereas Si–OH-containing magnesium silicates crystallize in minutes up to hours at this temperature. This time scale matches well to the expected residence times of condensed silicates close to the condensation zone. The formation of Si–OH bonds in cosmic magnesium silicate particles has to be taken into account since \( H_2O \) as the most abundant oxygen-bearing molecule plays a very important role in the condensation of circumstellar silicates (Gail & Sedlmayr 1998).

4. Comparison with observations

The prediction of the formation of pure magnesium or iron silicates during gas phase condensation in the MgO–FeO–SiO\(_2\) system and the formation of eutectic compositions (Rietmeijer et al. 1999a,b) raised a lot of questions concerning the production of amorphous mixed Mg–Fe silicates. The condensation of an amorphous pure magnesium silicate has been made likely by the detection of only very pure crystalline magnesium silicates which can be formed from the corresponding amorphous precursor by thermal annealing (Hallenbeck et al. 1998; Fabian et al. 2000). This scenario is also supported by gas phase condensation experiments which have shown that silicates are originally formed in the amorphous state. Though the activation energy of crystallization is smaller for iron-containing silicates due to the decrease of viscosity compared to magnesium silicates, there is no observational evidence for the formation of crystalline Fe-silicates in space. There have to be good reasons for the formation of only crystalline magnesium silicates.

4.1. AGB stars

The testbed of silicate dust laboratory analogues is the comparison of theoretical spectra based on such data with the observed spectral energy distributions (SED). The broad and mostly structureless appearance of the emission profiles of the circumstellar silicate bands of evolved stars at 10 and 18 \( \mu \text{m} \) inhibits direct mineralogical conclusions. There are, however, characteristic points that have some diagnostic value: the exact peak positions and the widths of the bands, the asymmetry of the 10 \( \mu \text{m} \) band profile, the ratio of the band strengths, and the depth and shape of the “trough” between them. The exact appearance of the absorption coefficient derived from the observed SED is sensitively influenced by the assumptions of the derivation procedure (photospheric model of the star, assumed dust temperature, points where the dust emissivity of the envelope vanishes). An important point is that there could be a continuous dust absorption superposed to the silicate absorption bands. This effect could mask the widths of the bands and the absorption between the bands, in the so-called trough.

For the comparison with the observations we chose the two AGB stars TY Draconis and R Cassiopeiae, for which high-quality ISO-SWS spectra in the wavelength range from 2 to 45 \( \mu \text{m} \) are available. These spectra have been downloaded from the ISO archive and were reduced with the ISO Spectral Analysis Package (ISAP). TY Dra shows very slender bands and a deep trough, whereas the Mira star R Cas represents the case of very broad bands and a shallow trough. As effective dust temperature we adopted 400 K, that corresponds to the values derived in the literature for Miras and semi-regular variables (Hron et al. 1997).

The spectra of R Cas and TY Dra have been used for this purpose, not only because of the characteristic difference in the MIR spectra of both stars, but also because of the fact that for both of them, several ISO spectra exist, dating from different phases in their cycles of variability. The different spectra of R Cas strongly resemble each other in the region dominated by the dust emission (Kerschbaum et al. 2000), and the same is true for the spectra of TY Dra. This indicates that intrinsic differences between both stars are responsible for their largely different MIR dust emission.
Fig. 8. Comparison of our sol-gel-produced magnesium silicates with the observed ISO-SWS spectrum of TY Draconis. In the second line of the insert the full silicate formulae have been truncated in order to save space. The mixture of Mg$_5$SiO$_3$, Mg$_4$SiO$_4$, and Mg$_{24}$SiO$_{44}$ (for a CDE) gives the best reproduction of the dust emissivity reached so far.

The dust emissivity has been derived in the following way: At $\lambda = 7\, \mu m$, the observed flux was assumed to be wholly dominated by the stellar photosphere. Therefore, a Rayleigh function has been fitted to the spectral energy distribution at this wavelength and has been subtracted from the SED in order to derive the dust emissivity. Subtracting more sophisticated photospheric models which take into account the molecular absorption (primarily due to H$_2$O, CO and SiO) does not lead to significantly different results for the dust emissivity in this case, especially not for the region $\lambda > 9\, \mu m$ in which we are primarily interested. It is clear from radiative transfer calculations that for stars like TY Dra, the contribution of the dust emission to the total SED amounts to already 5–10% in the 7–9 $\mu m$ range. Therefore, the subtraction procedure explained above introduces a small uncertainty of the dust emissivity in the 7–9 $\mu m$ range. In Fig. 8, the normalized dust spectrum of TY Dra obtained by the described procedure is compared with emisissivities determined from the calculated absorption coefficients of the sol-gel silicates. While the observed spectrum cannot be satisfactorily reproduced by using a single magnesium silicate compound, a mixture of Mg$_{15}$SiO$_{35}$, Mg$_{24}$SiO$_{44}$ and Mg$_{24}$SiO$_{44}$ gives an almost perfect agreement with the observation. This shows that pure amorphous magnesium silicates are the best candidates for the dust spectra of such stars. The biggest deviation is visible at the “blue” wing of the 10 $\mu m$ band. The corresponding dust emissivity of R Cas (see Fig. 11) cannot be exclusively represented by sol-gel magnesium silicates or by the glassy Mg–Fe-silicates. This is mainly due to R Cas’ enhanced emission in the 11–15 $\mu m$ range, which is discussed below.

One problem with the magnesium silicates is their very low NIR opacity, which inhibits effective absorption of the stellar radiation and therefore strongly reduces heating. However, taking into account the probable formation of metallic iron in oxygen-rich circumstellar shells (see e.g. Kozasa & Hasegawa 1988; Gail & Sedlmayr 1999), this problem can be easily solved, because metallic iron inclusions will strongly enhance the NIR absorption of Mg silicates as recently demonstrated by Kemper et al. (2002). Near 1 $\mu m$, where the opacity of pure magnesium silicates reaches its minimum, the value of $Q_{\text{abs}}/a$ is increased by a factor of about 10 if only 0.1% of the grain volume is a metallic Fe inclusion. An enhancement by a factor of 100 is reached if 1% of the grain volume is metallic Fe (see Fig. 9).

It is a well-known fact that the silicate spectra of AGB-stars and other evolved stars exhibit great spectral diversity especially in the 10 $\mu m$ region. Speck et al. (2000) have used UKIRT CGS3 spectra in order to classify the 10 $\mu m$ profiles of AGB stars and supergiants into characteristic groups. We examined whether our magnesium silicates are able to match the mean spectra of selected star groups. Figure 10 illustrates that the derived mean profiles of group A to C and the additional supergiant group 1 can be well reproduced either by mixtures of or single magnesium silicates. The mean spectrum of supergiant silicate group 1 can be matched by Mg$_{15}$SiO$_{35}$ spheres in the Rayleigh limit. The spectrum of group A of the AGB stars can be fitted by either a single magnesium silicate (Mg$_{15}$SiO$_{35}$) or a mixture of the two components Mg$_{24}$SiO$_{44}$ and Mg$_{24}$SiO$_{44}$. In contrast groups C and D require a rather complex mixture with varying Mg/Si ratios.

4.2. The trough opacity problem

When comparing the dust emission of the circumstellar envelope of TY Dra with that of a typical Mira variable like R Cas or R Aql, it becomes clear that the flux minimum between the two silicate bands is much less conspicuous than should be expected from the absorption efficiency of almost any amorphous silicate produced in the laboratory. This discrepancy is known for several years already; it has been called the “trough opacity problem” (Dorschner 1999).
It turned out that “filling of the trough” in order to obtain spectra like that of R Cas cannot be reached by silicate absorption. Silicates containing alkaline earth or transition metal oxides cannot provide spectra with 10 µm profiles shifted to wavelengths longer than 11 µm since the position of this Si–O stretching band depends on the polymerization degree of SiO$_4$ tetrahedra and therefore on the number of bridging oxygen atoms in the silicate network (McMillan 1984). Even though in Mg$_2$SiO$_4$ only non-bridging oxygen atoms are present, the formation of a three-dimensional amorphous network requires the existence of at least a small portion of bridging oxygen atoms. This can only be compensated by the incorporation of structural inhomogeneity on an atomic scale. A considerably higher content of metal oxide in the silicate gives rise to the formation of rather inhomogeneous material due to the stoichiometry problems. In this study we were able to incorporate a metal oxide content up to 2.4 wt% without producing a non-homogeneous material.

There are, however, oxides that could contribute to the trough opacity. First observational evidence pointing in this direction was given by the 13 µm band that has been discussed as being due to Al–O vibrations in α-Al$_2$O$_3$ or in MgAl$_2$O$_4$ (Begemann et al. 1997; Posch et al. 1999; Fabian et al. 2001). Further experiments with other oxides that could effectively contribute to the trough opacity are in progress in the Jena laboratory.

In order to roughly illustrate the amount and the cumulative SED of potential trough opacity contributors from the observations, we simply subtracted the normalized dust emission of a star like TY Dra from the normalized dust emission of a star that does not show a deep trough between the two silicate bands such as R Cas. The result of such a subtraction is shown in Fig. 11. As already mentioned, this difference spectrum can hardly be understood in terms of different silicate dust populations. Different grain sizes could play a role, since for large grains (i.e. when their radius is no longer small compared to the wavelength), both the 10 and the 20 µm bands can develop huge shoulders partly filling the trough between them. However, the dominance of grains with diameters of several µm is not very probable in an average circumstellar shell. An exception are very evolved AGB or massive stars, which can have grain sizes up to 6 µm (Molster et al. 1999; Hoogzaad et al. 2002). Optical depth effects are negligible, because the circumstellar shells of both stars are optically thin over the whole wavelength range considered here. Therefore, it seems rather likely that a distinct dust grain population is responsible for the broad emission peaking around 13 µm. As potential carriers of this emission oxides like Al$_2$O$_3$ (Begemann et al. 1997), MgAl$_2$O$_4$ (Posch et al. 1999; Fabian et al. 2001) and Ca–Al–oxides (Mutschke et al. 2002) have been discussed. It is an interesting coincidence that the only band that has been definitely observed is located exactly at the 13 µm peak of the difference spectrum.
reduce amorphous magnesium silicates with different Mg/Si ratios in a homogeneous form and to derive optical constants by Kramers-Kronig analysis and Lorentz-oscillator fit method. The diagnostic spectral parameters in the MIR region have been derived by calculating the absorption efficiency in vacuum both for spheres and for a distribution of ellipsoids in the Rayleigh limit. The 10 and the 20 \( \mu m \) bands have been shown to approach each other with increasing magnesium content (which shifts the 10 \( \mu m \) band towards the “red” and the 20 \( \mu m \) band towards the “blue”). This effect is due to the influence of the MgO content on the degree of polymerization of the SiO\(_4\) tetrahedra. As expected, large differences between pure magnesium- and composite magnesium-iron-silicates were found in the NIR region.

The crystallization of amorphous Mg-silicates by thermal annealing has also been investigated. The sol-gel produced magnesium silicates show an interesting annealing behaviour. The activation energy was found to be independent of the Mg/Si ratio, but largely dependent on the Si–OH content. The activation energy of crystallization can be reduced by one third by the presence of up to 1.5 wt% Si–OH bonds compared to magnesium silicates which do not contain Si–OH. This leads to a significant reduction of the necessary crystallization temperature and crystallization time.

First results of a comparison with observed dust emission spectra underline the relevance of amorphous Mg-silicates for our understanding of circumstellar shells. Comparisons with the normalized dust spectrum of TY Dra have demonstrated that a mixture of Mg\(_1\)SiO\(_3\), Mg\(_2\)SiO\(_4\), and Mg\(_2\)SiO\(_3\) gives a nearly perfect match with the observations. Pure amorphous magnesium silicates are the best candidates for modeling the dust spectra of such stars.

The corresponding dust emissivity of R Cas (see Fig. 11) cannot be exclusively represented by sol-gel magnesium silicates or by the glassy Mg–Fe-silicates. Other dust components like aluminium oxides or spinels can contribute to the trough opacity. The trough opacity beyond 16 \( \mu m \) could be influenced by iron oxide or mixed magnesium iron oxides. Furthermore, different grain sizes could play a role, since for large grains (i.e. when their radius is no longer small compared to the wavelength), both the 10 and the 20 \( \mu m \) bands can develop huge shoulders partly filling the trough between them. However, the dominance of grains with diameters of several \( \mu m \) is not very probable in an average circumstellar shell.

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