

Multifrequency interferometer and radio continuum monitoring observations of CTA 102[★]

F. T. Rantakyrö^{1,2,★★}, K. Wiik³, M. Tornikoski⁴, E. Valtaoja^{3,5}, and L. B. Bååth⁶

¹ European Southern Observatory, Casilla 19001, Santiago 19, Chile

² Observatorio Cerro Calan, Universidad de Chile, Santiago, Chile

³ Tuorla Observatory, Väisäläntie 20, 21500 Piikkiö, Finland

⁴ Metsähovi Radio Observatory, Metsähovintie 114, 02540 Kylmälä, Finland

⁵ Department of Physical Sciences, University of Turku, 20100 Turku, Finland

⁶ Center for Imaging Technologies, Halmstad University, 301 18 Halmstad, Sweden

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Abstract. This paper represents the work of several years of observation of CTA 102 with both single dish telescopes and interferometric arrays, covering wavelengths from 1.2 cm to 1.3 mm. The resolution of the maps covers an order of magnitude from 0.5 mas to 50 μ as. The images presented demonstrate the rapid structural changes in this source. These rapid structural changes correlates with the outbursts seen in the total flux, turnover frequency and in the spectral index. We have calculated the Brightness Temperatures of the components (T_B) directly from the determined component sizes and also using the logarithmic variability amplitudes and timescales to calculate the T_B s. Both the methods yielded measurements of source frame T_{BS} no higher than \sim a few $\times 10^{12}$ K. We find that the observed average proper motion is $\sim 0.4 \pm 0.07$ mas/yr, which corresponds to an apparent transverse velocity of 11 ± 2 c.

Key words. shock waves – quasars: individual CTA102 – galaxies: jets – radiation mechanisms: non-thermal

1. Introduction

CTA 102 (QSO 2230+114, $\alpha = 22\ 32\ 36.41$ and $\delta = +11\ 43\ 50.9$ (J2000), $z = 1.037$, and $m_v = 17.33$ (NED database)) has been studied at several wavelengths and during many epochs. It has been classified as an optical variable with a mean magnitude of 17.33 and as a High Polarized Quasar (HPQ). It was the first radio source for which variations in the flux density were reported (Scholomitski 1965; Dent 1965). The time-scale of the variations led Scholomitski to deduce a linear size of 0.1 pc for the radio emitting region. An angular size of 10 milliarcsec (mas) was deduced by Slish (1963) from the spectral turnover, but at the red shift distance of CTA 102 this implies that the region responsible for the synchrotron emission is larger than the variability time-scale suggests. With the inferred angular size the brightness temperature of the variable component would exceed the inverse Compton limit and a very large X-ray flux density should be observed. The dilemma of “Superluminal Flux Variations”

(Romney et al. 1984) can be solved by either an intrinsic model based on bulk relativistic motion of the radio emitting material (Blandford & Königl 1979; Scheuer & Readhead 1979) or an extrinsic model based on refractive interstellar scintillation (Rickett et al. 1984; Rickett 1986). Rantakyrö et al. (1996) showed that the major contribution to the variability at wavelengths shorter than $\lambda 32$ cm is due to intrinsic processes.

Observations of CTA 102 with the EGRET telescope at the high-energy γ -rays (>100 MeV) have shown that the source exhibits a high γ -ray luminosity, $L_\gamma = 5 \times 10^{47}$ erg s⁻¹ (Nolan et al. 1993), and the X-ray flux is correspondingly high, $F_X = 0.75 \mu$ Jy. L_γ dominates the emission seen at all other wavelengths, a common feature among gamma-bright blazars. The common explanation for the high apparent L_γ is that the emission is the result of a beamed jet with a high Lorentz factor.

The arc second scale structure of the source is dominated by a central core and two other components (Spencer et al. 1989). At $\lambda 18$ cm the stronger component has a flux density of 0.2 Jy and is located at ~ 1.6 arcsec at PA $\sim 140^\circ$, the fainter one is only 0.1 Jy at 1.0 arcsec at PA $\sim -40^\circ$. Both components have a steep spectrum. Observations at $\lambda 6$ cm (Wehrle & Cohen 1989), at $\lambda 18$ cm, and at $\lambda 1.3$ cm (Rantakyrö et al. 1996) show a central double knot feature (separated in NS direction by ~ 3 mas) with an extended diffuse tail bending sharply to the SW. Rantakyrö et al. (1996) showed that the source exhibits

Send offprint requests to: F. T. Rantakyrö,
e-mail: frantaky@eso.org

[★] Based on observations collected at the European Southern Observatory, Chile.

^{★★} Present address: European Southern Observatory, Casilla 19001, Santiago 19, Chile.

very fast structural changes. Due to this rapidity together with the long time between the epochs the proper motion was underestimated to be only $\mu = 0 \pm 0.5$ mas/year.

Typical for the major outbursts we observe in blazar and gamma-bright AGNs is that they first start with a rapid flux increase simultaneously at optical and IR frequencies and later at the high radio frequencies (86 GHz and higher) (Courvoisier et al. 1988). High frequency single dish monitoring shows that outbursts tend to emerge almost simultaneously over the range 86–300 GHz with the turnover frequency reaching 86 GHz within a month and then 22 GHz within 4–5 months (Lainela et al. 1993; Stevens et al. 1996). Similar time-scales are observed in 3C 279 (Litchfield et al. 1995). This has been explained (Marscher & Gear 1985; Marscher et al. 1992) by a thin shock which is formed close to the central engine and then moves down the jet. After some time the shock will expand adiabatically and the spectral turnover (due to synchrotron self-absorption) will move towards lower frequencies. The outburst will therefore be observed at lower frequencies after the expansion has started. Observations of the shocks at their early stages of development are fundamental to our understanding of how they are formed, how they emerge from the core, and how they develop on their way through the radio jet. It must be emphasized that such observations can only be done with very high angular resolution (to resolve the features) and at high frequencies (as the region close to the core is optically thick at low frequencies) thus mmVLBI is the only way to image the shocks as they emerge from the core.

The April 1990 session was the first epoch when we could produce hybrid maps using intercontinental baselines to obtain a resolution of $50 \mu\text{as}$ (Rantakyro et al. 1998). This was achieved because of the development of new receivers, improved phase stability of local oscillators, new data reduction techniques (Bååth et al. 1992), and the increase in the source flux density.

Our earlier observations (Bååth et al. 1992; Rantakyro et al. 1998) have shown that the radio cores of powerful AGNs (in the observer’s rest frame) are very small, on the order of 10^{16} – 10^{18} cm, which is only 5–5000 times larger than the Schwarzschild radius of a $10^9 M_{\odot}$ black hole.

A special and characteristic feature of the sub-milliarcsecond scale structures is that the curvature observed with cm-VLBI seems to continue, but is further enhanced, closer to the core (Rantakyro et al. 1998).

This paper presents four epochs of the Coordinated mm-VLBI Array (CMVA) $\lambda 3$ mm VLBI, $\lambda 7$ mm and $\lambda 13$ mm dual-frequency VLBA observations, three epochs of global 22 GHz VLBI observations, one adhoc EVN 22 GHz epoch, and continuum monitoring of this source at 22 [13 mm], 37 [8 mm], 90 [3 mm], and 230 GHz [1.3 mm]. We will also discuss and analyse these observations.

2. Observations and data reduction

2.1. 3 mm VLBI

The CMVA 1997 sessions were global 86 GHz $\lambda 3$ mm-VLBI sessions involving the following telescopes: Effelsberg

Table 1. CMVA Telescope information. D is the diameter in meters, μ is the sensitivity in K/Jy, T_{sys} the single-sideband system equivalent noise in Kelvin referred to outside the atmosphere, and the final column gives information about the sessions (April/Jun./Oct./Dec.) in which the telescope participated.

Name	D [m]	μ [Jy/K]	T_{sys} [K]	Sessions
Effelsberg	100	7.7	800	yes/no/yes/no
Hat Creek	3×6.1	90	420	yes/no/no/yes
Haystack	37	17	400	yes/yes/yes/yes
Kitt Peak	12	53	205	yes/yes/yes/yes
Metsähovi	14	58	300	no/no/yes/no
Onsala	20	35	480	yes/yes/yes/yes
Owens Valley	10.4	46	500	yes/yes/no/no
Pico Veleta	30	7.1	200	yes/no/yes/no
Pie Town				yes/yes/yes/yes
Quabbin	14	42	320	yes/no/no/yes

(Germany), Hat Creek (USA), Haystack (USA), Kitt Peak (USA), Metsähovi (Finland), Onsala (Sweden), Owens Valley (USA), Pico Veleta (Spain), Pie Town (USA) and Quabbin (USA). Information on the participating antennas can be found in Table 1. Especially the June 1997 epoch suffered from the small number of detected fringes and participating telescopes. The data were recorded using MarkIII (and compatible) recorders to thick tapes and using 14 IF-channels with a 4 MHz bandwidth in each, and later correlated at the Haystack correlator. The output from the correlator was read into the Haystack Observatory Post-processing System (HOPS) post-correlation package and the fringe search and amplitude calibration was done within this package.

2.2. EVN, Global VLBI, and VLBA observations

The VLBI sessions (November 13th 1992; September 20th 1993; October 19th 1996) were global sessions including the VLBA, VLA, and other available telescopes. The VLBA session (June 24th 1998) was a dual-frequency 22/43 GHz observation. In March 1994 we did a short adhoc observation using the EVN antennas. Being an adhoc observation the quality of the image is much less than what is expected from a full experiment. Table 2 lists the antennas participating in these sessions. The participating antennas are Medicina (Italy), Noto (Italy), Metsähovi (Finland), Onsala (Sweden), NRAO 140 (Green Bank, USA), Effelsberg (Germany), Jodrell Bank Mk2 (England), VLBA_{BR} (Brewster), VLBA_{FD} (Fort Davis), VLBA_{KP} (Kitt Peak), VLBA_{LA} (Los Alamos), VLBA_{PT} (Pie Town), VLBA_{OV} (Owens Valley), VLBA_{NL} (North Liberty), VLBA_{SC} (Saint Croix), VLBA_{MK} (Mauna Kea) and VLBA_{HN} (Hancock) and one antenna from the Very Large Array (VLA).

The data were recorded using MarkIII and VLBA recorders to thick tapes, and using 14 IF-channels with a 4 MHz bandwidth in each, and later correlated at the VLBA correlator. The output from the correlator was read into the AIPS package and the fringe search and amplitude calibration was done within this package. The amplitude calibration was done by applying the measured system temperature at each station, correcting for

Table 2. EVN, Global and VLBA Telescope participation information. The participation of each telescope is listed by epoch (1992/1993/1994/1996/1998).

Name	1992	1993	1994	1996	1998
Medicina	yes	yes	yes	yes	no
Noto	yes	yes	yes	yes	no
Metsähovi	yes	yes	yes	yes	no
Onsala	yes	yes	yes	yes	no
NRAO 140	yes	yes	no	yes	no
Effelsberg	yes	yes	yes	yes	no
Jodrell Bank	no	yes	yes	yes	no
VLBA _{BR}	yes	yes	no	yes	yes
VLBA _{FD}	no	yes	no	yes	yes
VLBA _{LA}	yes	yes	no	yes	yes
VLBA _{PT}	yes	yes	no	yes	yes
VLBA _{OV}	yes	yes	no	yes	yes
VLBA _{NL}	yes	yes	no	yes	yes
VLBA _{SC}	no	yes	no	yes	yes
VLBA _{MK}	no	yes	no	yes	yes
VLBA _{KP}	yes	yes	no	yes	yes
VLBA _{HN}	yes	no	no	no	yes
VLA (USA)	no	yes	no	yes	no

gain and atmospheric effects. We believe that the amplitudes are correct to within 10%.

The later uv data model fitting was done in the DIFMAP package (Shepherd 1997). We first fitted Gaussian components directly to the uv-data and the final images were constructed by adding components using the differential mapping approach.

2.3. Continuum monitoring

CTA 102 was observed at $\lambda 3$ mm [90 GHz] and $\lambda 1.3$ mm [230 GHz] with the SEST at the European Southern Observatory site on Cerro La Silla in Chile (Fig. 2). Some of the data have been published in Tornikoski et al. (1996). At $\lambda 8$ mm [37 GHz] and $\lambda 13$ mm [22 GHz] it was monitored by the Metsähovi group as part of a larger sample of AGNs (Teräsranta et al. 1998) using the Metsähovi Radio Telescope (Fig. 1). The SEST observations at 90 GHz were made using a dual-polarization Schottky receiver until June 1995, and since then using a SIS receiver. As a backend, a wide band (1 GHz) AOS was used. For the 230 GHz observations a Schottky receiver and a wide band AOS were initially used, but since 1991 the data were mainly obtained with a single channel bolometer. Some of the recent data points were obtained with a SIS+AOS setup. At Metsähovi the 22 and 37 GHz observations were made using a HEMT frontend. At the SEST the flux density observations were made with dual-beamswitching mode with either 10 or 20 s spectra. The mean and RMS of the observation was calculated by doing a least-squares fit to the flux and RMS obtained from each individual spectra. There were typically 20 spectra in each observation run. The calibration of the flux densities used the standard SEST calibration based on measurement of planet fluxes. At Metsähovi the continuum receivers at 22 and 37 GHz were used with 20 s scans with a total integration time

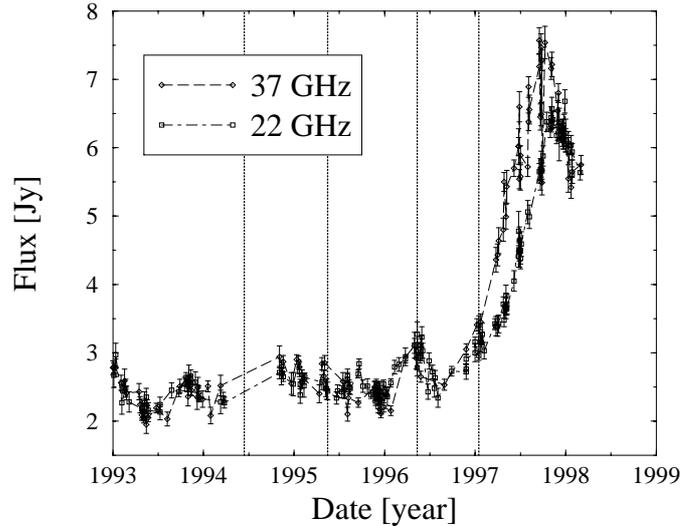


Fig. 1. 22 and 37 GHz continuum observations of CTA 102. Diamonds markers with the long dashed line are the 22 GHz observations and the squares with the short dash long dash line represents the 37 GHz observations. The vertical dotted lines indicate the estimated dates for the zero epochs from the proper motion estimates (see Sect. 4). The error bars indicate the total error of the measurement which consists of errors in calibration, pointing, and the the thermal noise of the measurement.

of 1200 s for each observation. See Teräsranta et al. (1998) for an extensive description of the calibration method used in these observations. The result of this monitoring is presented in Figs. 1–2. It is evident that the outbursts are first seen at 90 and 230 GHz (the poor time sampling of the 230 GHz precludes the determination of the time-delay between these two frequencies) and later appear simultaneously at 22 and 37 GHz. This agrees very well with what has been seen previously (Lainela et al. 1993; Stevens et al. 1996; Litchfield et al. 1995). Unfortunately the flux outburst seen at 22 and 37 GHz in early 1996 occurs at the time where we have no higher frequency measurements. The multifrequency variability behavior of CTA102 will be discussed in more detail in Tornikoski et al. (2002).

3. Observations

3.1. $\lambda 3$ mm-VLBI observations with the CMVA in 1997

The $\lambda 3$ mm-VLBI observations with the CMVA in 1997 are very strongly limited by the small number of detected fringes. Thus we present a more extensive discussion of the uv-data for these epochs. Shown in Fig. 3 are the amplitudes with baseline lengths for each epoch and similarly in Fig. 4 we show the uv-coverage of the observations in 1997. The most critical shortcoming of the observations is the low number of uv-data points. By using HOPS with incoherent averaging we obtained one data point for each baseline and 6.5 min scan. Thus each data point is highly significant and we have been very conservative in our editing (i.e. removal of data points).

Subsequent uv data model fitting was done using the DIFMAP package. We fitted elliptical Gaussian components

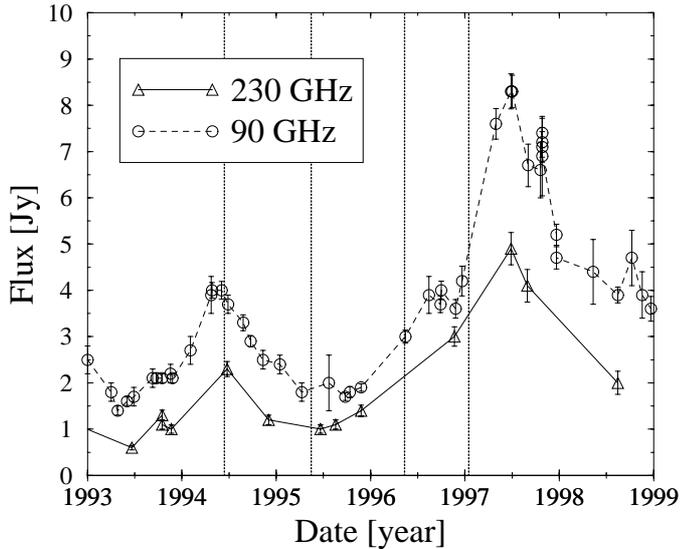


Fig. 2. 90 and 230 GHz continuum observations of CTA 102. Circles with the dashed line are the 3 mm observations and the triangles with the continuous line represents the 1.3 mm observations. The vertical dotted lines indicate the estimated dates for the zero epochs from the proper motion estimates (see Sect. 4). The error bars indicate the errors in the measurements and are the result of the measurement RMS errors and the calibration and pointing errors.

directly to the uv-data, until adding components to the fit did not significantly decrease the χ^2 value and a good fit to the closure phases was achieved. The final images were constructed using these model fits and hybrid mapping. The final uv-coverage varied so much between the epochs that no common restoring beam could be used (see the uv-coverages in Fig. 4). The final images of the four epochs are shown in Fig. 5 and the results from the χ^2 -fit are listed in Table 3. The errors in the parameters are typically in the order of $<15\%$. This error estimate is based on the spread of the fits yielding similar χ^2 values.

Note: in the following discussion it is important to remember that we are not discussing the images but components of the images. The specific size, structure, and location of each component may be open for discussion, but the existence, general position, and rough size, of the components are defined and do not vary significantly with the number of components used in the fit or the actual model fitting method used (using the uv-data model-fitting routine in DIFMAP or in AIPS).

3.2. 22 GHz global and EVN VLBI observations

These observations were part of the projects Global VLBI (GL010, GL013, GL014, and GW014 (Wiik et al. 2001)), and the adhoc EVN project GR005. The global VLBI projects consisted of snapshot observations of several QSOs, thus the restoring beam and signal to noise ratio are worse than expected for a full run. Thus although the 3 epochs have similar antenna configuration, the final restoring beam and SNR vary. We present the three images in Fig. 6.

The EVN observation was made with the antennas that were 22 GHz-capable at that time. With the limited

Table 3. Model parameters for the elliptical Gaussian components fitted to the CTA 102 $\lambda 3$ mm-VLBI maps made in the four CMVA epochs in 1997. Date is the epoch of observation, ID is the label identifying the component, $\Delta\alpha$ and $\Delta\delta$ give the position of the component relative to the core, Flux is the flux density of the component, b_{maj} and b_{min} are the major and minor axes of the elliptical Gaussians ($FWHM$), and PA is the position angle of the fitted Gaussians.

Date	ID	$\Delta\alpha$ [mas]	$\Delta\delta$ [mas]	Flux [Jy]	b_{maj} [mas]	b_{min} [mas]	PA [$^\circ$]
Apr.	I0	0	0	2.55	0.05	<0.001	60
Apr.	I1	0.06	-0.12	0.01	0.14	<0.001	-16
Apr.	I2	0.61	-0.16	0.13	0.2	<0.001	22
Apr.	I3	0.54	-0.59	0.06	0.2	<0.001	-17
Jun.	J0	0	0	1.48	0.4	0.025	-4
Jun.	J1	0.20	0.01	4.1	1.0	<0.001	-22
Jun.	J2	0.62	-1.20	1.96	0.8	<0.001	70
Oct.	K0	0	0	0.35	0.3	<0.001	77
Oct.	K1	0.11	-0.38	0.77	0.2	<0.001	60
Oct.	K2	0.33	-0.32	1.1	0.14	<0.001	50
Oct.	K3	0.49	-0.68	0.74	0.26	<0.001	70
Oct.	K4	1.84	-1.2	0.3	0.2	<0.001	50
Oct.	K5	1.84	-1.9	0.6	0.4	<0.001	60
Dec.	L0	0	0	1.0	0.1	<0.001	-35
Dec.	L1	0.09	-0.39	0.54	0.08	0.05	-30
Dec.	L2	0.37	-0.70	0.14	0.1	<0.001	0
Dec.	L3	0.66	-0.66	0.10	0.2	<0.001	-16
Dec.	L4	0.90	-0.76	0.12	0.3	<0.001	-22

uv-coverage and the short observing time, the final image has much poorer resolution and SNR than what is currently available with the EVN. The final hybrid mapping image is shown in Fig. 7. The error in the absolute calibration is much worse, estimated to be $\sim 40\%$. This map is presented here as it gives us crucial information about the structural changes in the source.

To obtain the position of the underlying components we have fitted Gaussian components to the uv-data. Due to the complexity of the image as many as 9 Gaussians have been needed to find a good fit to the data. The number of required components was estimated by adding components until the fit to the closure phases did not improve. An additional criterion was that the χ^2 should decrease significantly with an added component. The component positions, sizes, and fluxes for the three epochs are presented in Table 4. To test the convergence, we used several sets of starting values for the iterative solution, and the values shown in Table 4 were the best possible ones (minimum χ^2 was reached). The errors in these solutions are typically in the order of $<15\%$. This number is based on the spread of fits yielding similar χ^2 numbers. The components have been labeled so that they are uniquely identified. We will discuss the intra epoch identification of components and their apparent proper motion in Sect. 4.

3.3. 43 and 22 GHz VLBA observations June 24th 1998

In Fig. 8 we present the complete maps from the dual-frequency (22 and 43 GHz) VLBA observations made in June 24th 1998. There is no structure above the noise level

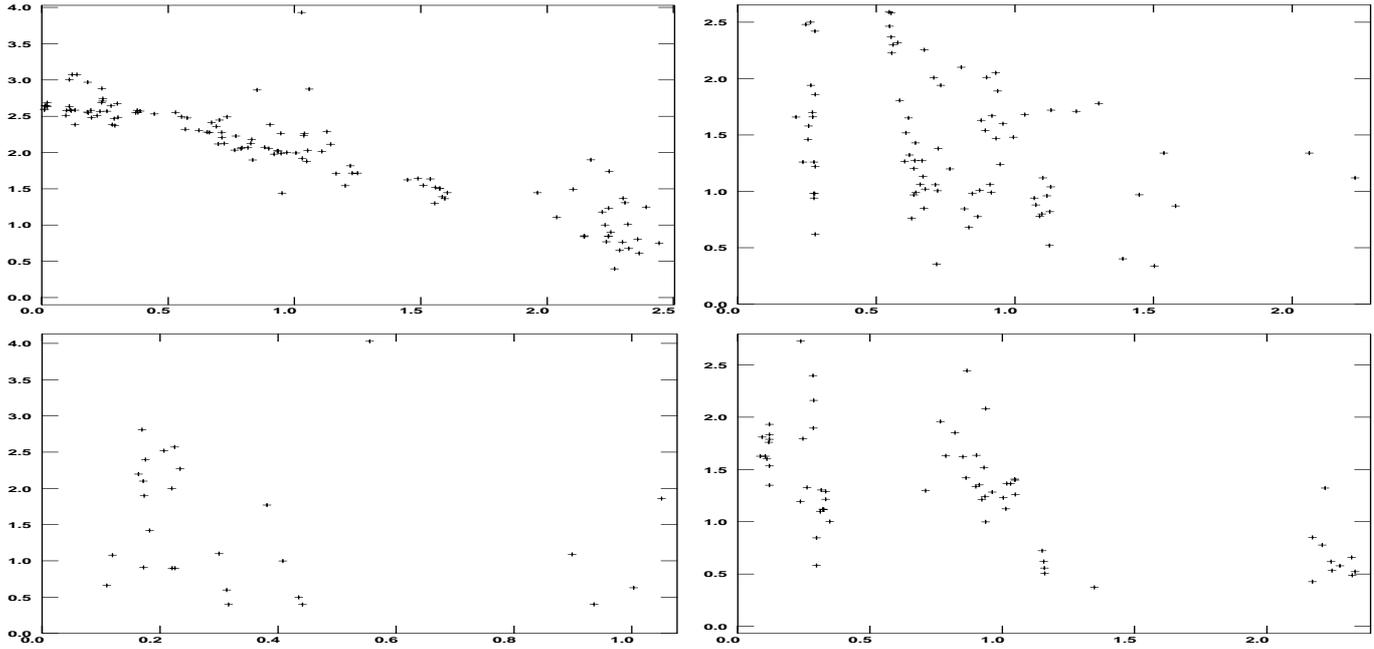


Fig. 3. Plots of uv amplitude vs. baseline length for the four epochs in 1997 with the CMVA. The values given on the x -axis are in $G\lambda$ and on the y -axis in Janskys in all four plots. **Top left:** April 14, **top right:** June 18, **bottom left:** October 24, and **bottom right:** December 13.

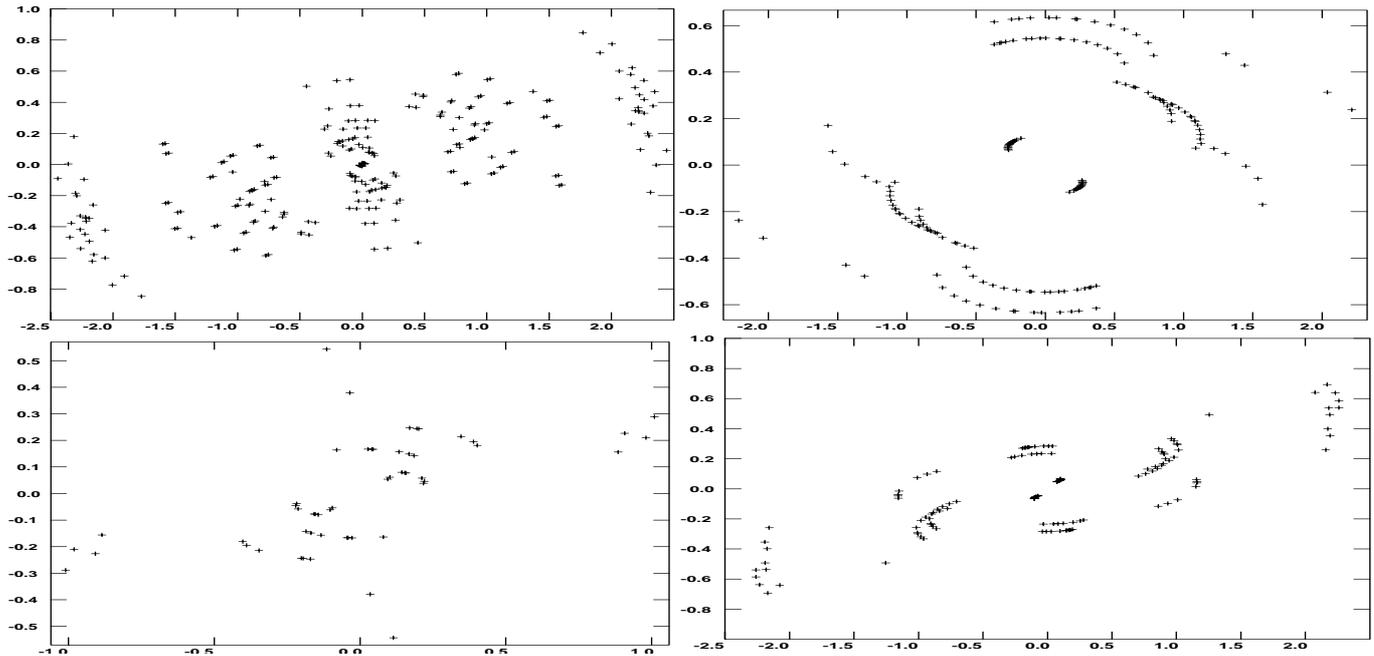


Fig. 4. CTA 102 Plots of uv-coverage for the four epochs with the CMVA in 1997. The values on both axes are in $G\lambda$ in all four plots. **Top left:** April 14, **top right:** June 18, **bottom left:** October 24, and **bottom right:** December 13.

outside the region shown in the two maps. The resulting model-fit of elliptical Gaussians to the calibrated uv-data is shown in Table 5. The discussion about the validity and fidelity of the χ^2 -fits made in Sect. 3.2 is also valid for these fits.

3.4. Spectral index

The spectral index is defined as $S \propto \nu^\alpha$, and thus we can calculate α from our flux monitoring measurements (Figs. 1–2) taken at the SEST and Metsähovi. The result is presented in

Figs. 9–10. Included in the figures are also the estimated dates for the zero epochs from the proper motion estimates (see Sect. 4).

The quiescent spectra, as defined by the minimum fluxes, from 1995.0/1995.5 (37–90 GHz/22–37 GHz) to 1996.4/1996.4 are typical falling spectra, but the flaring spectrum is highly inverted. At all times the turnover frequency is higher than 37 GHz except during late 1995 and early 1996, and for a substantial fraction of the time in conjunction with the flux outbursts higher than 90 GHz.

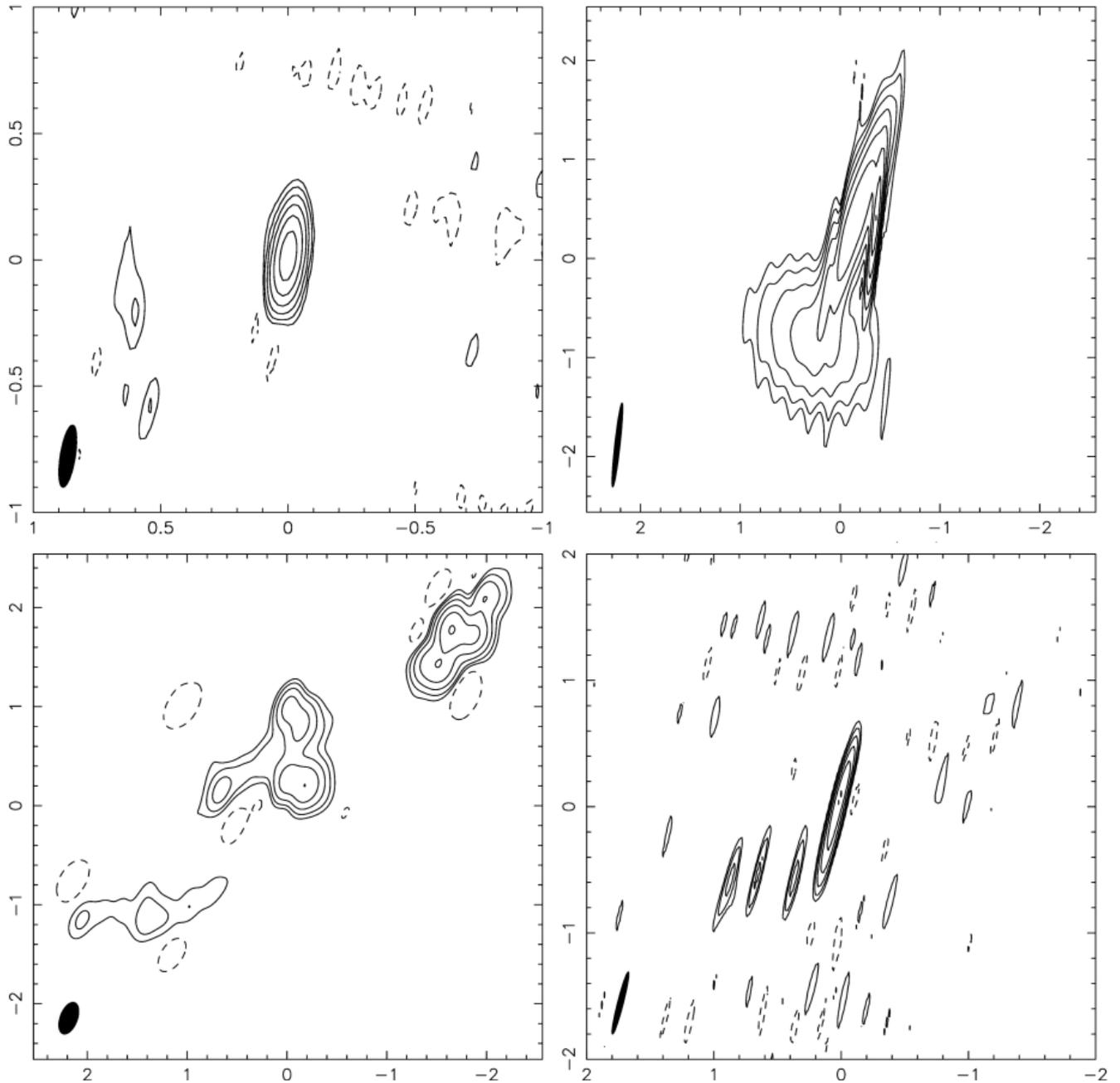


Fig. 5. CTA 102 86 GHz CMVA images from 1997. The map scales are all in mas. **Top left:** April 14, Peak flux 1.86 Jy/beam, and restoring beam 0.25×0.06 mas at -9° . Contour levels are $-2, 2, 4, 8, 16, 32, 64\% \times$ Peak flux. **Top right:** June 18, Peak flux 1.24 Jy/beam, and restoring beam 0.85×0.05 mas at -6° . Contour levels are $-1, 1, 2, 4, 8, 16, 32, 64\% \times$ Peak flux. **Bottom Left:** October 24, Peak flux 0.89 Jy/beam, and restoring beam 0.33×0.17 mas at -20° . Contour levels are $-3, 3, 6, 12, 24, 48, 96\% \times$ Peak flux. **Bottom right:** December 13, Peak flux 0.81 Jy/beam, and restoring beam 0.5×0.04 mas at -14° . Contour levels are the same as in October 24.

The spectral index turnover frequency is at all times lower than 230 GHz. Note that the sparse sampling at 90 and 230 precludes any detailed analysis of the short time-scale evolution of the spectral index as well as an accurate determination of the time delay between 90 and 230 GHz.

It is evident from the total flux monitoring (Figs. 1–2) and the estimates of the zero epochs (Table 6) that at the start (or with a delay of some weeks) of each large outburst there is an ejection of a component from the core. Thus the total flux monitoring is a valuable tool in helping us to understand the

structural changes in this source. This is also seen in the spectral index plots (Figs. 9–10) where each ejection causes a steepening in the spectrum. Better timesampling, especially at higher frequencies, is needed to study in detail the delay between the different wavelengths, the actual time between the ejection of a component and the change in the radio fluxes, and the spectral index in the single dish observations.

Unfortunately we do not have any simultaneous 3 and 7 mm VLBI observations of the source, but the simultaneous 13 mm and 7 mm VLBA observations allowed us to obtain a spectral

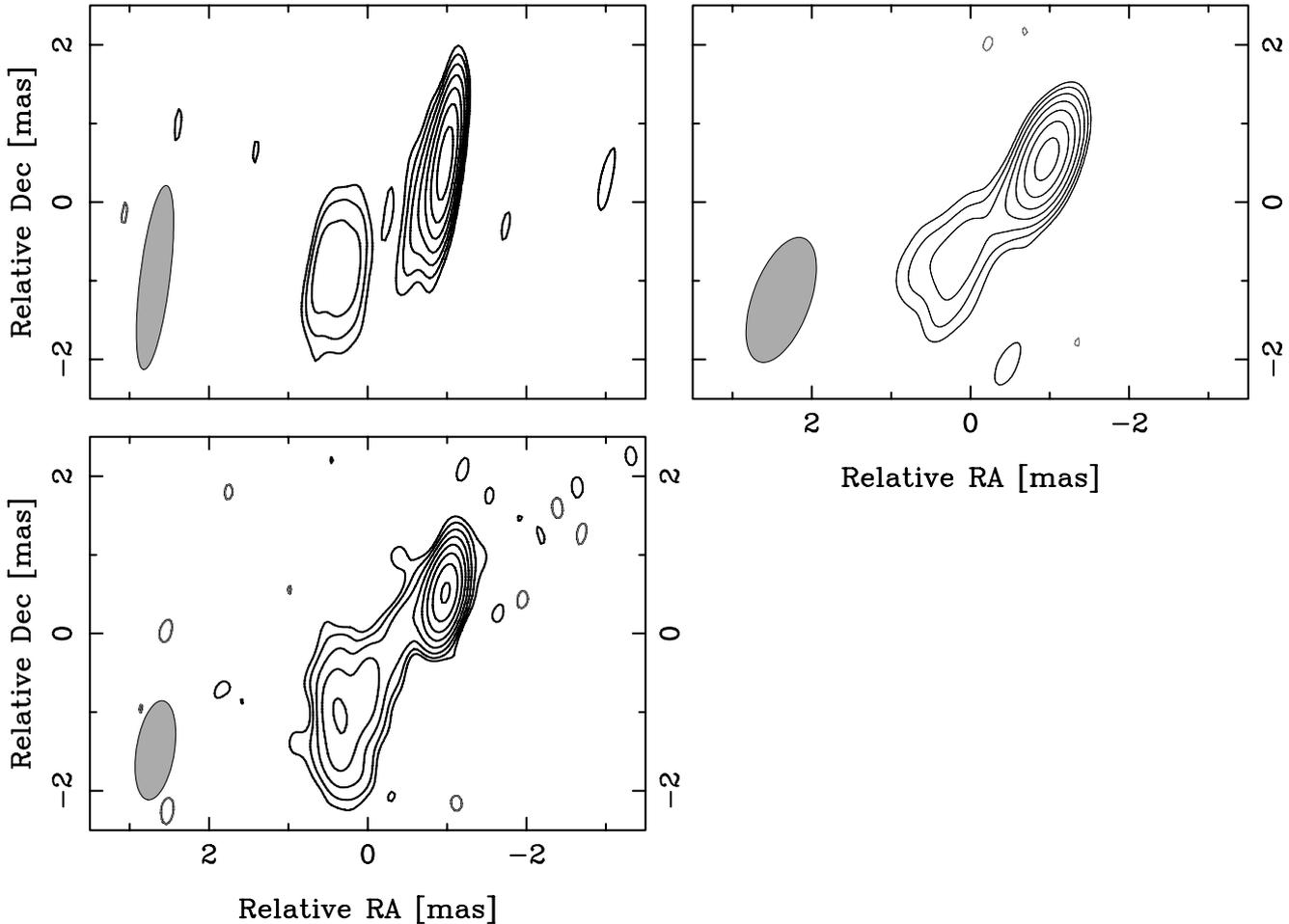


Fig. 6. CTA 102 22 GHz Global VLBI maps. The contour levels in all three maps are $(-3, 3, 6, 12, 24, \dots, 384) \times \text{RMS Noise}$. **Top Left:** November 13 1992. Peak Flux = 0.980 Jy/beam and RMS Noise = 3.3 mJy/beam. Convolution beam is an elliptical Gaussian (1.13×0.19 mas at PA = -7°). **Top Right:** September 20 1993. Peak Flux = 0.980 Jy/beam and RMS Noise = 4.1 mJy/beam. Convolution beam is an elliptical Gaussian (0.83×0.36 mas at PA = -19.8°). **Bottom Left:** October 19 1996. Peak Flux = 0.893 Jy/beam and RMS Noise = 2.1 mJy/beam. Convolution beam is an elliptical Gaussian (0.64×0.24 mas at PA = -8.8°).

index map of the source (Fig. 11). The spectral index is flat or positive for the core and in the extended component G2. As the dynamic range is insufficient to follow the underlying jet at 43 GHz we cannot determine if the change in the spectral index at G2 is intrinsic to the source or if it is an artifact caused by the lower dynamic range.

4. Proper motion of components

In the following discussion, it is assumed that the observed redshift, $z = 1.037$, is cosmological in origin with $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$, and $q_0 = 0.5$. Using these parameters, 1 mas then corresponds to a distance of $4.2 h^{-1} \text{ pc}$. At the measured redshift, an angular velocity of 1 mas yr^{-1} then corresponds to an apparent transverse velocity of $v = 28 h^{-1} c$.

4.1. Distance from the core

We have calculated the separation from the core individually for each epoch and frequency to avoid problems with the absolute position of the “core”, which may differ at different

frequencies. We have added the measured distances from the core from Rantakyro et al. (1996), Wehrle & Cohen (1989), and Jorstad et al. (2001) to expand the database and to improve the quality of the fits. The errors in the core separation estimates represent the 3σ error for the determination of the position of the component. In the case of the observations not determined in this paper, these errors are three times the standard error from the fit to the components (Rantakyro et al. 1996; Wehrle & Cohen 1989; Jorstad et al. 2001), while the position measurements presented in this paper are estimated from the spread in solutions in DIFMAPS model fit software and typically have values of $<15\%$ of the measured values.

The positions of the components in Jorstad et al. (2001) and in this article agree quite well if error-bars are taken into account. They do all follow a general trend that agrees with the general direction of the jet in this source.

In Fig. 12 the components are plotted as a function of their position in RA and DEC with respect to the core, D . The direction of the jet twists almost 90° at $r \sim 2$ mas, at $r \sim 6$ mas, and, finally at $r \sim 7-8$ mas. The same twisting of the jet is seen directly in Fig. 8.

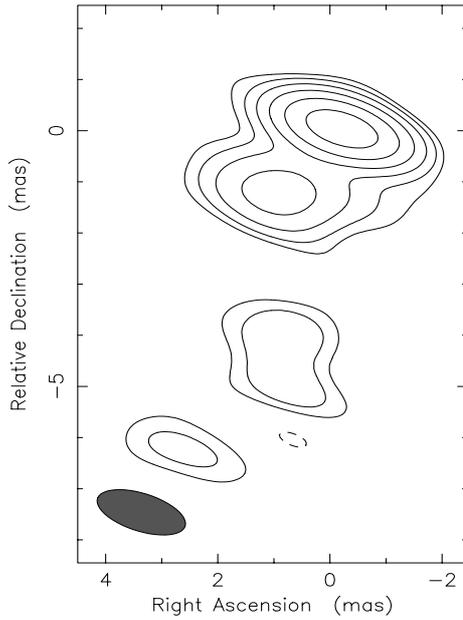


Fig. 7. CTA 102 22 GHz map from 1994 March 7. Contour intervals are chosen as $-2, 2, 4, 8, 16, 32, 64$ percent of the peak flux density in the map. The peak flux is 0.39 Jy/beam. The restoring beam is an elliptical Gaussian (1.65×0.73 mas in $PA = 70^\circ$).

4.2. Proper motion

In Fig. 13 we have plotted the component separations from the core. Squares indicate distances measured in this paper, those from Rantakyrö et al (1996) and Wehrle & Cohen (1989) are marked with circles. The diamonds are measurements taken from Jorstad et al. (2001). The vertical fine dotted lines indicate the epochs of observation. The thicker dotted sloped lines show the weighted least squares fit for the proper motion of the components. The fit was done by first fitting the observed $\lambda 3$ mm-VLBI observations and then sequentially fitting the components further from the core. We assume that all components are visible within the distance limit of ≤ 10 mas from the core and they do not disappear and reappear randomly (i.e. the Christmas tree effect causing misidentification). The effect of components disappearing due to sensitivity being too low to detect the weaker components and reappearing again when increasing in apparent flux will not affect our measurements since the components even if undetected are still moving down the jet increasing their distance from the core. **Note:** Jorstad et al. (2001) had included the 1997.58 B3 component in their fit for motion of B3 and we find a better fit if this is grouped with the $\lambda 3$ mm-VLBI observations of the innermost component motion (J). This confusion is understandable due to the limited resolution available with $\lambda 7$ mm VLBA observations. We include a blow-up of the inner 4 mas showing the measured positions of the components and the weighted LSQ fits determining the proper motion in Fig. 14. The symbols used are the same as in Fig. 13.

Table 6 presents the proper motions, μ , in both mas/yr and in v/c , in the cosmological model that is used (see beginning of Sect. 4), and the zero-epochs calculated from the fitted proper motions. We have labelled the moving components from A to J,

Table 4. Model parameters for the spherical Gaussian components fitted to the CTA 102 maps for the global and EVN sessions 1992, 1993, 1994, and 1996. Flux is the flux density of the component, $\Delta\alpha$ and $\Delta\delta$ gives the position of the component relative to the core, Size is the size of the fitted Gaussian (diameter).

Epoch	ID	$\Delta\alpha$ [mas]	$\Delta\delta$ [mas]	Flux [Jy]	Size [mas]
1992	C0	0	0	0.98	0.06
1992	C1	0.19	-0.28	0.17	0.18
1992	C2	0.8	-0.7	0.039	0.17
1992	C3	1.3	-1.4	0.21	0.48
1992	C4	2.8	-6.64	0.40	2.8
1993	D0	0	0	0.53	<0.01
1993	D1	0.03	-0.08	0.54	<0.01
1993	D2	0.45	-0.56	0.091	0.084
1993	D3	1.2	-1.25	0.17	0.50
1993	D4	1.3	-2.0	0.03	<0.01
1993	D5	1.4	-4.6	0.10	2.5
1993	D6	2.8	-7.0	0.20	1.6
1993	D7	4.1	-9.7	0.06	2.1
1994	E0	0	0	0.416	0.2196
1994	E1	1.0	-1.2	0.14	1.2
1994	E2	1.0	-4.3	0.06	1.2
1996	F0	0	0	0.24	<0.01
1996	F1	0.07	-0.16	0.68	0.074
1996	F2	0.2	-0.4	0.19	0.30
1996	F3	0.6	-0.7	0.04	<0.01
1996	F4	1.2	-1.4	0.34	0.64
1996	F5	1.3	-2.1	0.17	0.41
1996	F6	1.0	-4.6	0.045	0.95
1996	F7	2.9	-7.0	0.34	2.86
1996	F8	5.2	-8.9	0.09	1.4

and this labelling should not be confused with the individual labelling of the components in the maps presented in this paper.

We have determined the proper motion in this source by using all the measured transverse speeds by doing a LSQ fit to the data in Table 6. The average proper motion is $\sim 0.4 \pm 0.07$ mas/yr, which corresponds to an apparent transverse velocity of $11 \pm 2 c$.

The apparent proper motion is a function of the viewing angle, θ , and the component motion in the rest frame of the source, β :

$$\beta_{\text{app}} = \frac{\beta \sin \theta}{1 - \beta \cos \theta}. \quad (1)$$

The smallest possible β can be calculated assuming an optimum θ ($\theta_{\text{opt}} = \arccos \frac{\beta_{\text{app}}}{\sqrt{\beta_{\text{app}}^2 + 1}}$) for the observed proper motion.

In the following we will use γ when discussing the velocity of the plasma flow. γ_{min} can easily be calculated from β_{min} using:

$$\gamma_{\text{min}} = \frac{1}{\sqrt{1 - \beta_{\text{min}}^2}}. \quad (2)$$

Thus for the observed $\beta \sim 11$, we obtain a viewing angle, $\theta \sim 5.2^\circ$ and the corresponding $\gamma_{\text{min}} \sim 11.1$.

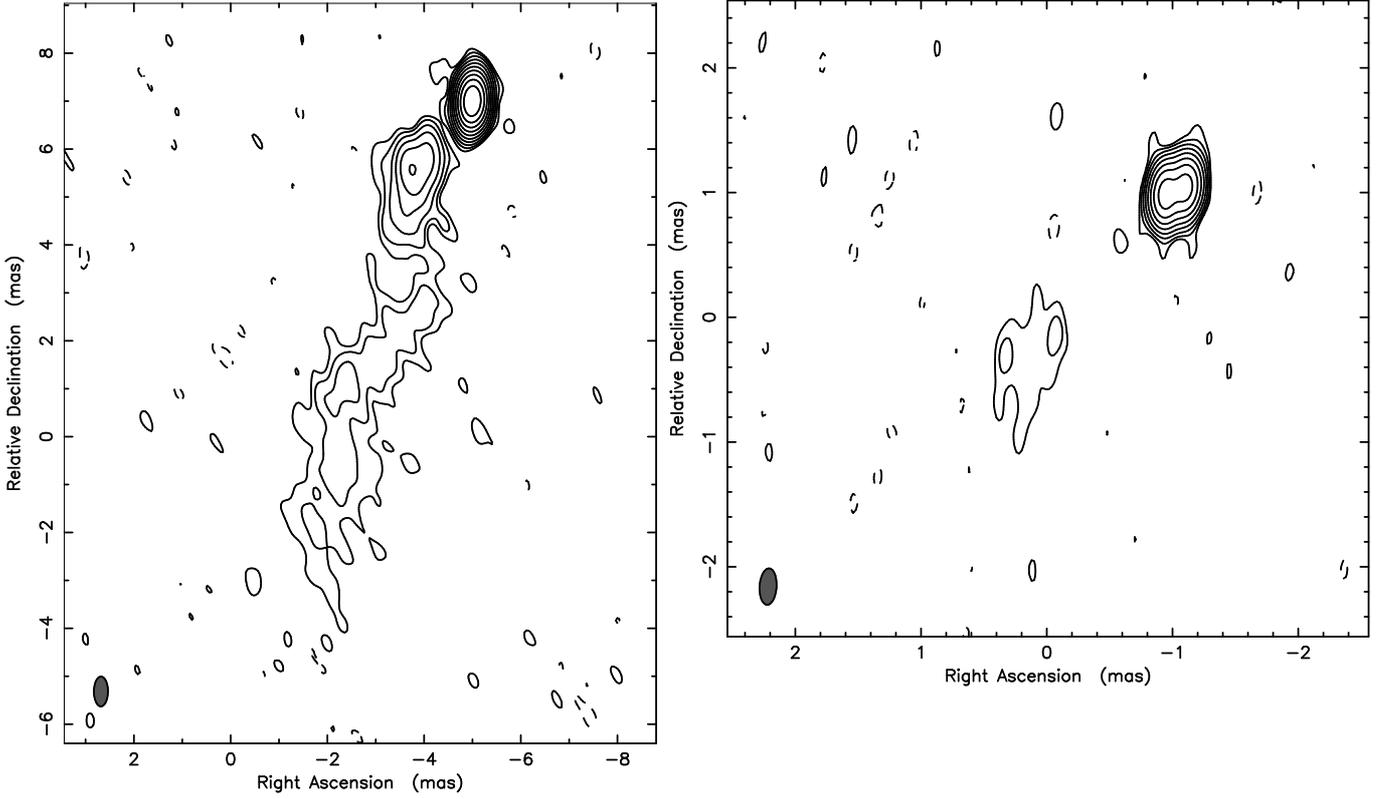


Fig. 8. **Left:** 22 GHz map from 1998 June 24. Peak flux density = 3.59 Jy/Beam. Contour intervals are chosen as $(-0.1, 0.1, 0.2, 0.4, 0.8, 1.6, 3.2, 6.4, 12.6, 25.8, 51.2) \times 36$ mJy/beam. The restoring beam was a elliptical Gaussian (0.62×0.29 mas in $PA = -0.3^\circ$). **Right:** 43 GHz map from 1998 June 24. Peak flux density = 2.06 Jy/Beam. Contour intervals are chosen as $(-0.5, 0.5, 1, 2, 4, 8, 16, 32, 64) \times 21$ mJy/beam. The restoring beam was a elliptical Gaussian (0.29×0.14 mas in $PA = -3.4^\circ$).

Table 5. Model parameters for the elliptical Gaussian components fitted to the CTA 102 VLBA maps made in June 24th 1998. λ is the observing wavelength in millimeter, ID is the label identifying the component, $\Delta\alpha$ and $\Delta\delta$ give the position of the component relative to the core, Flux is the flux density of the component, b_{maj} and b_{min} are the major and minor axes of the elliptical Gaussians ($FWHM$), and PA is the position angle of the fitted Gaussians.

λ	ID	$\Delta\alpha$ [mas]	$\Delta\delta$ [mas]	Flux [Jy]	b_{maj} [mas]	b_{min} [mas]	PA [$^\circ$]
7	G0	0	0	2.1	0.08	0.04	-70
7	G1	0.16	-0.06	2.1	0.05	0.02	-87
7	G2	1.25	-1.36	0.2	0.80	0.46	-26
13	H0	0	0	1.4	0.18	<0.01	-19
13	H1	0.14	-0.03	3.0	0.16	0.07	-38
13	H2	1.05	-1.18	0.16	0.60	0.34	-4
13	H3	1.39	-1.44	0.17	0.52	0.23	20
13	H4	1.38	-2.14	0.13	0.94	0.66	-33
13	H5	2.5	-6.3	0.13	5.0	1.44	-22

5. Component peak brightness temperatures

With Gaussian components the observed brightness temperature, $T_{\text{B,obs}}$, is given by:

$$T_{\text{B,obs}} = 1.224 \times 10^{12} \frac{S_\nu(1+z)}{\nu^2 \times b_{\text{min}} \times b_{\text{maj}}} [\text{K}] \quad (3)$$

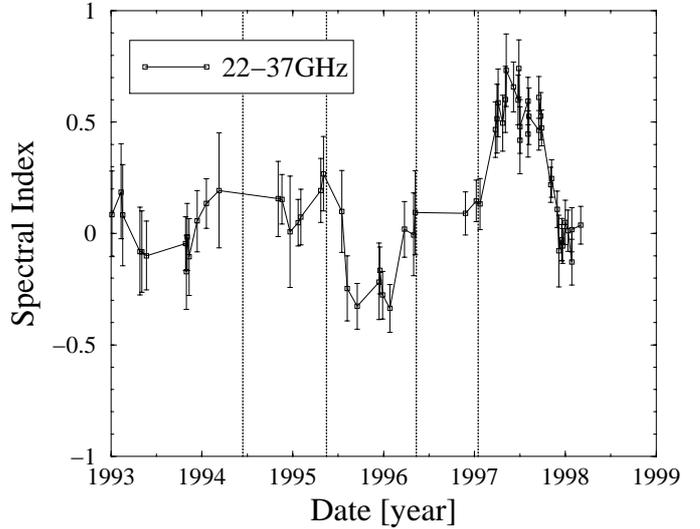


Fig. 9. Spectral index obtained from the 22 and 37 GHz observations made at Metsähovi. The spectral index is defined as $S \propto \nu^\alpha$. The errors bars indicate the 3σ limit of the observations. The vertical dotted lines indicate the estimated dates of the zero epochs from the proper motion estimates (see Sect. 4).

where S_ν [Jy] is the observed peak flux density at the frequency ν [GHz]. z is the redshift, b_{min} and b_{maj} are the minor and major axes of the Gaussian component [mas]. Using the

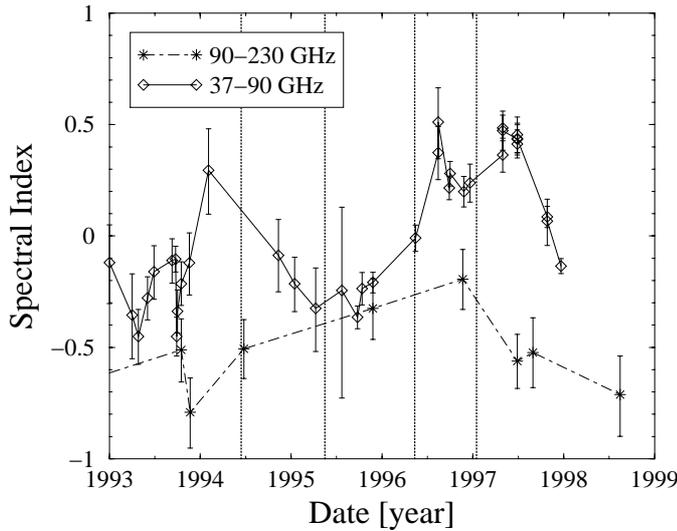


Fig. 10. Spectral index obtained from the 37, 90, and 230 GHz observations made at Metsähovi and SEST. The spectral index is defined as $S \propto \nu^\alpha$. The errors bars indicate the 3σ limit of the observations. The vertical dotted lines indicate the estimated dates of the zero epochs from the proper motion estimates (see Sect. 4).

values in Tables 3–5 and Eq. (3), we obtain the $T_{B,obs}$ values presented in Table 7. **Note:** $T_{B,obs,max}$ is the brightness temperature obtained by using the Gaussian model fit parameters and $T_{B,obs,min}$ is obtained by using the 1/10th of dirty beam size if the Gaussian model component size is smaller than this size. Since the $T_{B,obs}$ are the result of the T_B s in the source frame multiplied by the Doppler beaming factor, we include the estimated Doppler factor in Table 7. For each component we have calculated the Doppler factor, D , using Eq. (4).

$$D = \frac{1}{\gamma(1 - \sqrt{1 - 1/\gamma^2} \cos \theta)}. \quad (4)$$

Using the above determined $\theta \sim 5.2^\circ$ and the corresponding $\gamma_{min} \sim 11.1$, the Doppler factor, D , is ~ 11 .

Assuming for an unresolved component close to the core the flux can be expressed as $S \propto S_0 \nu^\alpha$, and the resolution is inversely proportional to the baseline lengths (NS and EW) and observing frequency, then Eq. (3) can be simplified to:

$$T_{B,obs} \propto \nu^\alpha \times baseline_{NS} \times baseline_{EW}. \quad (5)$$

Thus the low values of $T_{B,obs}$ from the EVN observation are expected because of the short baseline lengths. The $\lambda 3$ mm-VLBI observations suffer from smaller baseline lengths compared to Global VLBI, but this is compensated by the positive spectral index of the source in 1997. The most accurate determination of $T_{B,obs}$ is from the 22 GHz Global VLBI observations, while the 43 GHz observations are hampered by the spectral index, $\alpha \leq 0$, during the observations. In many cases in the $\lambda 3$ mm-VLBI observations the χ^2 solutions yielded very thin and narrow elliptical Gaussians. The narrow, thin elliptical Gaussians are the result of the model fitting procedure and are not believed to be a physical representation of the actual shape of the Gaussians. Unfortunately this means that the determined $T_{B,obs,max}$ may be highly incorrect, and in these cases

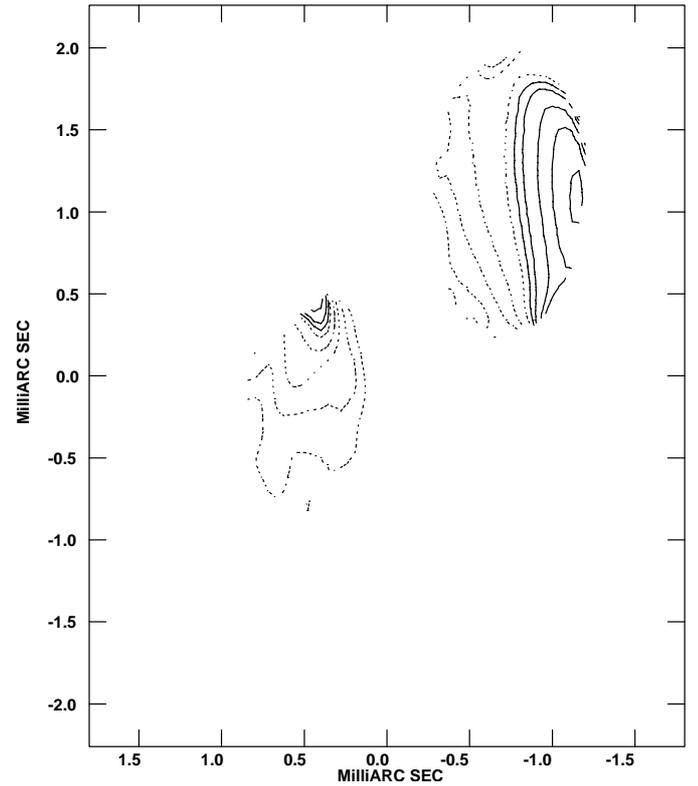


Fig. 11. CTA 102 spectral index map from 1998 June 24, determined using the simultaneous 22 and 43 GHz VLBA maps. Spectral index is defined here as $S \propto \nu^\alpha$. Contour levels are defined as $(-1.5, -1, -0.75, -0.5, -0.3, -0.1, 0, 0.1, 0.3, 0.5, 0.75, 1) \times 1.0$. The first negative contour is shown as a dashed line in the figure.

the $T_{B,obs,min}$ may yield a more realistic value. The long thin Gaussians often occur by using the modelling software as it tries to use 1 component when instead 2 or more components makes a better fit. Thus even if these components are extended the software basically fits a thin line connecting these two components underestimating the area of the Gaussians.

Using the logarithmic variability amplitudes and timescales to calculate T_B (Teräsanta & Valtaoja 1994), we obtain an independent estimate for the brightness temperature. **Note:** this is the T_B as seen in a reference frame comoving with the emitting component. We later will refer to this reference frame as the “source rest frame”. The T_B can be expressed as:

$$T_B = 5.87 \times 10^{21} \frac{\lambda^2 \Delta S}{\tau_{obs}^2} \left[1 - \frac{1}{\sqrt{1+z}} \right]^2 \times h^2 \text{ [K]} \quad (6)$$

where z is the redshift, λ is the observing wavelength, ΔS is the amplitude of the outburst in Jy, τ_{obs} is the variability timescale in days, and h is the scaling factor for H_0 (see Sect. 4). τ_{obs} is defined as (Burbidge et al. 1974):

$$\tau_{obs} = \frac{\Delta t}{\Delta [\ln(S)]}. \quad (7)$$

This method requires a good time-sampling and the 230 GHz data are too sparsely sampled to be suitable for calculations of T_B . Applying this to the 1997.0 outburst at 22, 37, and, 90 GHz we obtain: $T_B \sim 5 \pm 2$ [22 GHz], 4 ± 1 [37 GHz], and

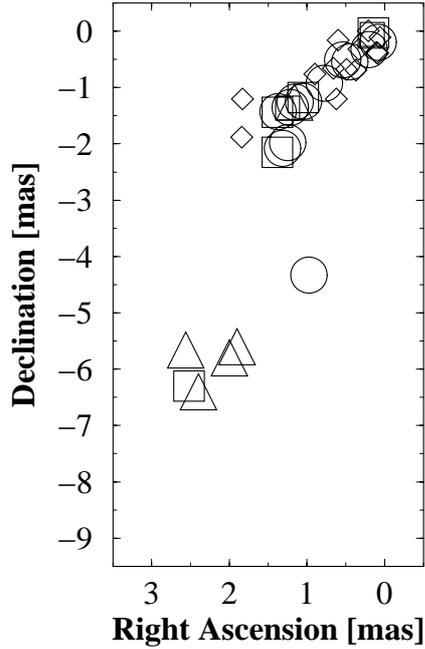


Fig. 12. The position of the fitted Gaussian components are plotted relative to the core, *D*. The observed positions are labelled as, \diamond , λ 3 mm-VLBI, \circ , 22 GHz observations, \triangle , 0.9 to 1.6 GHz, and, \square , VLBA observations at 22 and 43 GHz.

$1 \pm 0.5 [90 \text{ GHz}] \times 10^{12} \text{ K}$. Even in the best case the available sampling causes us to underestimate the full amplitude of the outburst, and miss the most rapid variations. The critical points in the determination of T_B are the determination of the underlying quiescent flux so that an accurate value of the flux increase due to the outburst can be found, and the confusion caused by superposed flare components. The latter can be avoided to some degree by selecting a suitable outburst that does not exhibit this feature. In determining the quiescent flux we have used the same method as Teräsraanta & Valtaoja (1994), i.e. taking half the flux before the outburst as the quiescent flux. All these factors will underestimate rather than overestimate the T_B s by as much as a factor of 5. The sampling and the flux variations are unsuitable to make this calculation for the actual epochs of the 22 GHz observations. Assuming that all outbursts reach similar maximum T_B s ($\sim 1 \times 10^{12}$) and the γ s (~ 11) determined in Sect. 4.2 describes the relativistic plasma jet, then:

1. The highest measured T_B s (Sep. 1993, Oct. 1996, and Apr. 1997) all conform with a maximum source frame (i.e. after correcting the observed T_B with the inferred Doppler factor) T_B s of \sim a few $\times 10^{12} \text{ K}$.
2. The highest values for T_B are all measured in the core or in a component just ejected. This is most clearly seen in 3 mm-VLBI observations in 1997 where the highest T_B is obtained in April 1997, just during the rapid increase in the total flux density. The later measurements in 1997 all show significantly lower values for T_B .
3. The measured variability of the T_B s at 22 and 37 GHz in 1997.0 agree well with the $6 \times 10^{12} \text{ K}$ obtained by Teräsraanta & Valtaoja (1994). These values are significantly lower

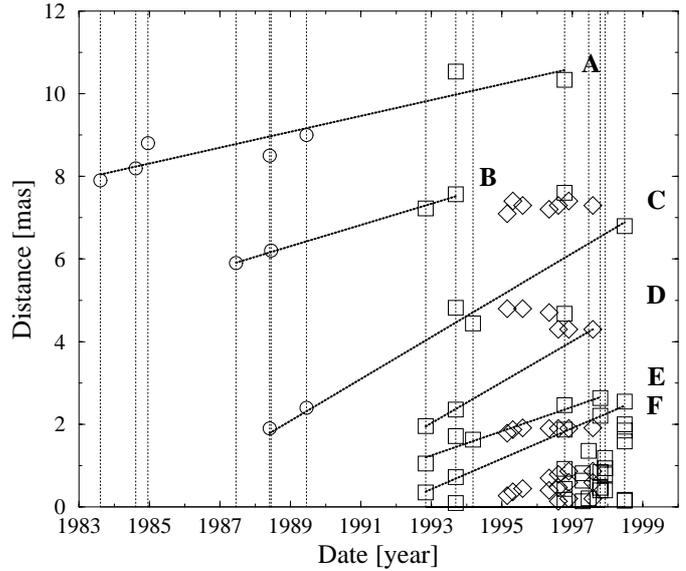


Fig. 13. The position of the fitted Gaussian components are plotted relative to the core, *D*. The lines represent the fitted proper motion to the measured position of the observed components. The moving “components” are labelled from A to I and the proper motion is listed in Table 6. The separations from the core measured in this paper are marked with squares, those from Rantakyro et al. (1996) and Wehrle & Cohen (1989) are marked with circles. The diamonds represent the data from Jorstad et al. (2001). The vertical dotted lines indicate the epoches of observations.

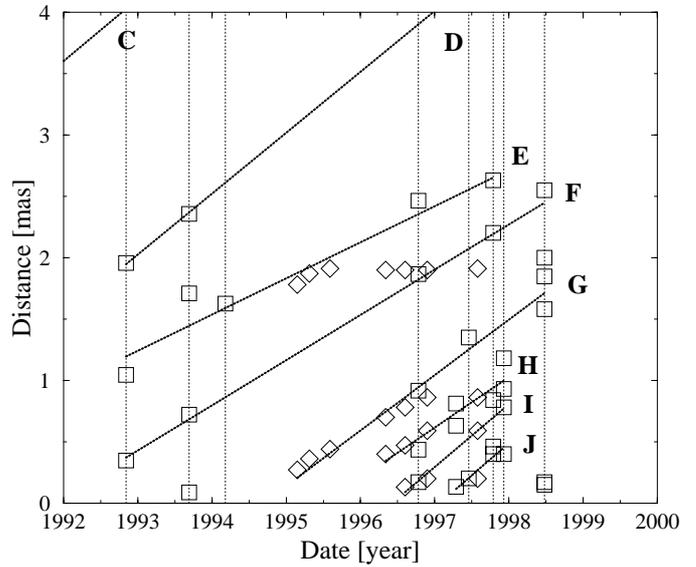


Fig. 14. A blow-up of the inner 4 mas in Fig. 13. Distances from the core measured in this paper are marked with squares. The diamonds represents the data from Jorstad et al. (2001). The vertical dotted lines indicate the epoches of observations.

- than the direct measurements but as discussed previously these measurements are underestimates of the T_B .
4. The 1994 measurement yielded very much lower values. This agrees with the flux monitoring which shows the source being in a relative quiescent state after the large outburst in 1992 and before the outburst in 1996.

Table 6. The proper motions in this Table are obtained from weighted least squares fit to the positions of the components in Fig. 13. The errors are the 3σ errors obtained from the fit. The columns are from left to right: ID is the name of the moving component (this label is unique for the proper motion and should not be confused with the labelling used for the individual components in the maps), μ is proper motion in mas/yr, proper motion in v/c , and the zero-epoch when the component was ejected.

ID	μ [mas/yr]	v/c	Zero [year]
A	0.15 ± 0.04	4.2 ± 1.1	1930.3
B	0.25 ± 0.16	7.2 ± 3.3	1964.4
C	0.47 ± 0.05	13.2 ± 1.3	1984.4
D	0.49 ± 0.15	13.8 ± 4.1	1988.9
E	0.31 ± 0.06	8.8 ± 1.7	1989.2
F	0.37 ± 0.03	10.4 ± 0.9	1991.9
G	0.39 ± 0.03	11.0 ± 0.9	1994.4
H	0.37 ± 0.06	10.3 ± 1.6	1995.4
I	0.43 ± 0.06	12.0 ± 1.7	1996.4
J	0.45 ± 0.07	12.7 ± 1.9	1997.04

None of the methods yielded measurements of source frame T_B s significantly greater than $\sim a \text{ few} \times 10^{12}$ K. This may be due to the limiting factor described in Eq. (5) and/or intrinsic to the source. We want to state that 3 mm-VLBI is a very useful technique to determine T_B if the observations are done during outbursts when $\alpha > 0$.

6. Conclusions

This paper represents the several year's work and observations with both single dish telescopes and interferometric arrays, covering wavelengths from 13 mm to 1.3 mm. Similarly the resolution of the maps covers an order of magnitude from 0.5 mas to $50 \mu\text{as}$. The highest resolution maps are vital to our observations of the rapid structural changes in this source, and thanks to the proper motions determined close to the core (from CMVA observations), we have been able to apply these proper motion measurements to the observations with poorer resolution and a much worse time sampling. Thus we draw the following conclusions:

- The images we have presented clearly demonstrate the rapid structural changes in this source. Using mmVLBI, VLBA at 22 and 43 GHz, and Global VLBI we are able to determine the proper motion using component speeds from close to the core out to component speeds determined at a few tenths of mas from the core.
- We find that the observed average proper motion is $\sim 0.4 \pm 0.07$ mas/yr, which corresponds to an apparent transverse velocity of $11 \pm 2 c$.
- The multi-band radio flux monitoring shows a source with rapid flux changes and quick changes in the spectral index and the turnover frequency. These changes are connected to the structural changes seen in this source.
- For the stronger outbursts the higher frequencies are leading the lower frequencies. On the other hand at 22 and

Table 7. Brightness temperatures obtained from the Gaussian components fitted to the data. See the running text for a description of the parameters and how they are calculated.

Date	Freq [GHz]	ID	$T_{B,\text{obs,max}}$ [10^{10} K]	$T_{B,\text{obs,min}}$ [10^{10} K]	D
Nov. 13, 1992	22	C0	170	80	11
Nov. 13, 1992	22	C1	3	3	11
Nov. 13, 1992	22	C2	4	4	11
Nov. 13, 1992	22	C3	0.08	0.08	11
Nov. 13, 1992	22	C4	0.02	0.02	11
Sep. 20, 1993	22	D0	2700	90	11
Sep. 20, 1993	22	D1	2800	90	11
Sep. 20, 1993	22	D2	7	7	11
Sep. 20, 1993	22	D3	0.4	0.4	11
Sep. 20, 1993	22	D4	15	5	11
Sep. 20, 1993	22	D5	0.01	0.01	11
Sep. 20, 1993	22	D6	0.04	0.04	11
Sep. 20, 1993	22	D7	0.01	0.01	11
Mar. 7, 1994	22	E0	4	4	11
Mar. 7, 1994	22	E1	0.05	0.05	11
Mar. 7, 1994	22	E2	0.02	0.02	11
Oct. 19, 1996	22	F0	1200	80	11
Oct. 19, 1996	22	F1	60	60	11
Oct. 19, 1996	22	F2	1	1	11
Oct. 19, 1996	22	F3	200	13	11
Oct. 19, 1996	22	F4	0.4	0.4	11
Oct. 19, 1996	22	F5	0.5	0.5	11
Oct. 19, 1996	22	F6	0.03	0.03	11
Oct. 19, 1996	22	F7	0.02	0.02	11
Oct. 19, 1996	22	F8	0.02	0.02	11
Jun. 24, 1998	43	G0	90	90	11
Jun. 24, 1998	43	G1	280	280	11
Jun. 24, 1998	43	G2	0.1	0.1	11
Jun. 24, 1998	22	H0	400	140	11
Jun. 24, 1998	22	H1	140	140	11
Jun. 24, 1998	22	H2	0.4	0.4	11
Jun. 24, 1998	22	H3	0.7	0.7	11
Jun. 24, 1998	22	H4	0.1	0.1	11
Jun. 24, 1998	22	H5	0.004	0.004	11
Apr. 14, 1997	86	I0	1700	300	11
Apr. 14, 1997	86	I1	2.4	0.4	11
Apr. 14, 1997	86	I2	20	4	11
Apr. 14, 1997	86	I3	10	2	11
Jun. 18, 1997	86	J0	5	5	11
Jun. 18, 1997	86	J1	140	30	11
Jun. 18, 1997	86	J2	80	16	11
Oct. 24, 1997	86	K0	40	2	11
Oct. 24, 1997	86	K1	130	8	11
Oct. 24, 1997	86	K2	260	15	11
Oct. 24, 1997	86	K3	100	6	11
Oct. 24, 1997	86	K4	50	3	11
Oct. 24, 1997	86	K5	50	3	11
Dec. 13, 1997	86	L0	340	84	11
Dec. 13, 1997	86	L1	4	4	11
Dec. 13, 1997	86	L2	50	10	11
Dec. 13, 1997	86	L3	20	4	11
Dec. 13, 1997	86	L4	10	3	11

37 GHz the outbursts are almost simultaneous in time as is expected by the shock in jet model.

- The determination of the proper motions show a highly relativistic jet, and allows us to extrapolate backwards to find the zero epochs of the outbursts. We see that at the start of each large outburst there is an ejection of a component from the core. Thus the total flux monitoring is a valuable tool in helping us understand the structural changes in this source. The ejection of a component from the core is also seen in the spectral index plots, where each ejection causes a steepening in the spectrum. Better timesampling, especially at higher frequencies, is needed to study the delay between the bands in detail, as well as the actual time between an ejection of a component and the change in the radio fluxes and spectral indexes in the single dish observations.
- The determination of the source frame T_B of the individual components agree both with the current models for the ejection of components in relativistic plasma jets and estimates of source frame T_B s using the logarithmic variability amplitudes and timescales. These observations also show a connection between the outbursts in the total flux monitoring and the high source frame T_B s determined from the interferometer images.

We conclude that further studies of this source are needed, including high resolution images and observations at longer wavelengths in order to determine the spectral indexes as a function of time and of distance from the core. The single dish monitoring has been of great value and should be a fundamental part of future observations of this source. Most important is that the observations should be done with short times between the sessions to obtain the smallest possible error in the determination of the proper motion of each component. With an observed proper motion of $\sim 0.4 \pm 0.07$ mas/yr we would ideally need a maximum of 3 months between observations.

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