

Evidence for binarity in the bipolar planetary nebulae A 79, He 2-428 and M 1-91^{*}

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Abstract. We present low and high resolution long-slit spectra of three bipolar planetary nebulae (PNe) with bright central cores: A 79, He 2-428 and M 1-91. He 2-428 and M 1-91 have high density (from $10^{3.3}$ to $10^{6.5}$ cm^{-3}) unresolved nebular cores that indicate that strong mass loss/exchange phenomena are occurring close to their central stars. An F0 star is found at the centre of symmetry of A 79; its reddening and distance are consistent with the association of the star with the nebula. The spectrum of the core of He 2-428 shows indications of the presence of a hot star with red excess emission, probably arising in a late-type companion. A 79 is one of the richest PNe in N and He, the abundances of M 1-91 are at the lower end of the range spanned by bipolar PNe, and He 2-428 shows very low abundances, similar to those measured for halo PNe. The extended nebulae of A 79 and He 2-428 have inclined equatorial rings expanding at a velocity of ~ 15 km s^{-1} , with kinematical ages $\geq 10^4$ yrs. The association of these aged, extended nebulae with a dense nebular core (He 2-428) or a relatively late type star (A 79) is interpreted as evidence for the binarity of their nuclei.

Key words. ISM: abundances – ISM: kinematics and dynamics – planetary nebulae: individual: A 79 – planetary nebulae: individual: He 2-428 – planetary nebulae: individual: M1-91

1. Introduction

Most planetary nebulae (PNe) possess axisymmetrical shapes, and some 10–15% of the global sample display a marked bipolar morphology, in the form of an “equatorial” waist or ring from which symmetrical lobes depart (Corradi & Schwarz 1995).

It has been shown that pure hydrodynamical collimation provided by dense equatorial disks or torii (Icke et al. 1989), and/or magneto-hydrodynamical collimation requiring the presence of toroidal fields (Chevalier & Luo 1994) can explain the development of the extreme bipolar geometries observed. While the dynamical mechanisms leading to the formation of bipolar lobes have therefore been identified, the AGB or post-AGB phase at which the

asymmetries develop (e.g. Sahai 2000) and the ultimate cause of their occurrence are still not well understood. In particular, whether a binary companion is needed to cause or enhance the asymmetry in the wind of the PN progenitor is the subject of a long term debate (cf. the proceedings of the recent conference edited by Kastner et al. 2000). A recent view (Soker & Rappaport 2000) is that bipolar PNe, especially those with the most extreme morphologies, are formed in binary systems that avoid a common envelope evolution during the AGB phase of the star on the way of producing the PN, i.e. by binaries with (present) orbital separations from ~ 5 to ~ 200 AU. It is hard to find evidence of binary motions from radial velocity measurements, especially for the longest period systems. An additional, major reason that makes it difficult to find a direct evidence for binarity in bipolar PNe is that their central stars are generally faint. In some cases, this is because of dust obscuration in dense circumstellar discs surrounding the central stars, but in general it is due to the fact that bipolar PNe are produced by the most massive progenitors of PNe ($M \geq 2.3 M_{\odot}$, Phillips 2001), which rapidly evolve towards low-luminosities in their post-AGB evolution.

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* Based on observations made with the 2.5 m INT and the 2.6 m NOT telescopes operated on the island of La Palma by the ING and the NOTSA, respectively, in the Spanish Observatorio del Roque de Los Muchachos (ORM) of the Instituto de Astrofísica de Canarias.

For these reasons, the surprisingly high brightness of the central star of He 2-428 (PN G049.4+02.4), whose bipolar nebula appears rather old in the existing narrow-band images, attracted our attention and we decided to investigate its nature by means of low and high resolution spectroscopy. Abell 79 (PN G102.9–02.3) and M 1-91 (PN G061.3+03.6) were also observed because they share some similarities with He 2-428 and with a subclass of bipolar PNe having properties reminding those of known binary systems such as symbiotic stars (Corradi 1995). The results of our spectroscopic study are presented in this paper.

2. Observations and data analysis

2.1. Low-resolution spectroscopy

Long-slit spectra covering the effective ranges $\lambda\lambda 3650\text{--}9220$ (He 2-428 and M 1-91) and $\lambda\lambda 3690\text{--}7050$ (A 79) were obtained at the 2.5 m Isaac Newton Telescope on La Palma equipped with the IDS spectrograph, the 500 mm camera (He 2-428 and M 1-91) or the 235 mm camera (A 79) and a CCD detector. The spectral ranges were covered with spectral resolutions of $\sim 8 \text{ \AA}$ using either a grating of 150 lines mm^{-1} at two angles (He 2-428 and M 1-91), or a grating of 300 lines mm^{-1} at one angle (A 79) and slit widths of $1''.1$ (He 2-428 and M 1-91) and $1''.6$ (A 79). The long slit was placed through the central bright cores of the objects and across the rings and lobes. The positions and orientations (PA) of the slit, the spatial resolutions and the exposure times are listed in Table 1.

Bias frames, twilight or tungsten flat-field exposures, wavelength calibrations and exposures of the standard star BD+284211 (from the IRAF compilation) were taken each night. The spectra were reduced to absolute intensity units using the IRAF reduction package, following standard procedures for the long-slit case. After the bias subtraction, flat-field correction and two-dimensional wavelength calibration, the individual exposures were flux calibrated using the standard star fluxes and the mean extinction curve for La Palma. Cosmic rays were removed and, after subtracting the sky contribution, the equivalent nebular spectra were combined to improve the signal-to-noise ratio.

One dimensional spectra were then extracted over the main morphological regions of the nebulae: the core or central star, the lobes and/or rings. The two regions on each side of the central star are identified in the following as A (the region towards the north for A 79 and He 2-428, and the region towards the west for M 1-91) and B (the regions towards the south or east). Tables 2–6 give the positions and sizes of the selected regions. Line intensities were measured in each region by fitting Gaussian profiles.

2.2. High-resolution spectroscopy

High resolution, long-slit spectra of He 2-428 and A 79 were obtained at the 2.6 m Nordic Optical Telescope on

La Palma, using the echelle spectrograph IACUB and a Thompson THX31156 CCD. The projected slit width was $0''.5$, providing a spectral resolution $R = \lambda/\Delta\lambda = 40\,000$, with a reciprocal dispersion of 0.05 \AA per binned pixel. The spectral range, selected using a narrowband filter, includes $\text{H}\alpha$ and the $[\text{N II}] \lambda 6583$ line. The slit position angles and exposure times are given in Table 1. The data were reduced using standard procedures in IRAF. The uncertainties in the measured relative velocities are of $\sim 2 \text{ km s}^{-1}$.

2.3. Imaging

An $\text{H}\alpha + [\text{N II}]$ image of He 2-428 was obtained on April 25, 2001, at the prime focus Wide Field Camera of the INT, equipped with a mosaic of 4 EEV 2048×4100 CCDs. The scale was $0''.33$, the exposure time 10 min and the seeing $1''.1$. The central wavelength and width of the $\text{H}\alpha + [\text{N II}]$ filter are 6568 \AA and 95 \AA , respectively.

2.4. Extinction correction and atomic data

In the low resolution spectra, line intensities have been corrected for extinction by interpolating Cardelli et al.'s (1989) R_V -dependent extinction law, with $R_V = A_V/E_{B-V} = 3.1$, the mean value for the diffuse interstellar medium. The logarithmic extinction c (see Osterbrock 1989) has been calculated for the outer nebular regions by fitting the ratio $I(\text{H}\alpha)/I(\text{H}\beta)$ to its recombination value for suitable physical conditions: $I(\text{H}\alpha)/I(\text{H}\beta) = 2.80\text{--}2.88$ for $N_e \simeq 1000 \text{ cm}^{-3}$ and $T_e = 10\,000\text{--}15\,000 \text{ K}$. The procedures followed to determine the values of the extinction parameter c in the cores are explained in Sects. 4.1, 4.2 and 4.3. All the values used for c are given in Tables 2–6, along with the measured and reddening-corrected line intensities for each area.

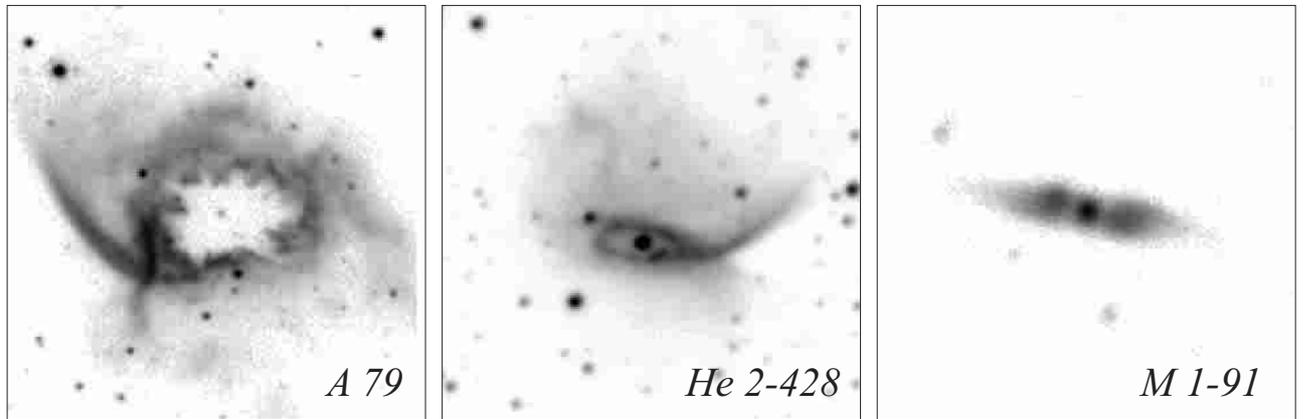
The line ratios of $[\text{S II}]$ lines $I(\lambda 6716)/I(\lambda 6731)$, $[\text{N II}]$ lines $I(\lambda 6548 + \lambda 6583)/I(\lambda 5754)$ and $[\text{O III}]$ lines $I(\lambda 4959 + \lambda 5007)/I(\lambda 4363)$ have been used to determine densities and temperatures. At high densities, like those found in the cores of He 2-428 and M 1-91 (see below), the $[\text{N II}]$ and $[\text{O III}]$ ratios are strongly dependent on density and can be used to determine this quantity if a value for the temperature is assumed. The physical conditions based on these lines as well as the ionic abundances implied by all the collisionally excited lines, excluding $[\text{Fe III}]$, have been determined with the *nebular* package in IRAF, with the atomic parameters referenced therein. The He I and He II emissivities have been taken from Benjamin et al. (1999), $[\text{Fe II}]$ emissivities are from Bautista & Pradhan (1996). Collision strengths and transition probabilities for $[\text{Fe III}]$ are those from Zhang (1996) and Quinet (1996), respectively.

3. Morphology of the nebulae

Figure 1 shows the images of the three nebulae. In addition to our INT image of He 2-428, a $[\text{N II}]$ image of A 79 was

Table 1. Journal of observations.

| Object | $\alpha(2000)$ (h m s) | $\delta(2000)$ ($^{\circ}$ ' ") | PA ($^{\circ}$) | Date | Exposure times (min.) | Scale ($''$ pixel $^{-1}$) |
|------------------------------|---------------------------|-------------------------------------|----------------------|----------------|--|---------------------------------|
| Low-resolution spectroscopy | | | | | | |
| He 2-428 | 19 13 05 | 15 46 42 | 0 | 1996 July 25 | 30, 3 ($\lambda\lambda 3690-6300$) 20, 3 ($\lambda\lambda 6020-9220$) | 0.41 |
| M 1-91 | 19 32 57 | 26 52 40 | +72 | 1996 July 25 | 30, 3 ($\lambda\lambda 3690-6300$) 20, 3 ($\lambda\lambda 6020-9220$) | 0.41 |
| A 79 | 22 26 17 | 54 49 38 | -20 | 1996 Aug 3 | $30 \times 2, 3 \times 2$ ($\lambda\lambda 3690-7050$) | 0.84 |
| High-resolution spectroscopy | | | | | | |
| He 2-428 | | | -10 +80 | 1999 August 31 | 30×2 30 | 0.14 |
| A 79 | | | +33 -57 | 1999 August 31 | 30 30 | 0.14 |

**Fig. 1.** Images of A 79 (in [N II], from Balick 1987), He 2-428 (in $H\alpha + [N II]$, see text) and M 1-91 (in $H\alpha$, Rauch 1999), in a logarithmic intensity scale. The size of each box is 60 arcsec.

kindly provided by B. Balick (from Balick 1987) and an $H\alpha$ one of M 1-91 by T. Rauch (Rauch 1999).

A 79 and He 2-428 (Fig. 1, left and centre) are similar, looking like rather evolved bipolar nebulae. They are composed of an irregular ring from which faint bipolar lobes depart, which appear to have almost vanished into the interstellar medium. Note the asymmetry in the surface brightness of the upper lobes, which have one edge much brighter than the other ones (the NE edge for A 79 and the NW one for He 2-428).

He 2-428 has a bright core inside the ring, while a fainter star-like object appears roughly at the centre of symmetry of the ring of A 79. M 1-91 (Fig. 1, right) also has a bright core, and possesses highly collimated lobes similar to those of its more studied sibling M 2-9 (cf. Doyle et al. 2000).

4. The nuclei of the nebulae

The central source in A 79 is found to have a stellar spectra, which is shown in Fig. 2 and discussed in Sect. 4.1, but the nuclei of He 2-428 and M 1-91 have emission line spectra. Figure 3 shows a close-up of the low-resolution

spectra of the bright cores of He 2-428 and M 1-91; Tables 2 and 3 show the line intensities relative to $H\beta$ before and after the extinction correction, the intensity measured for $H\beta$, the logarithmic extinction c and the size of the region over which the spectra have been extracted. Although both cores show indications of emission at high densities, as detailed below, their spectra are quite different. Both cores show the emission lines usually found in low-excitation nebulae ($H I$, He I, [O II], [O III], [N II], [S II], [Ar III]). M 1-91 shows also numerous lines of Fe II, [Fe II], [Fe III], [Fe IV], [Ni II] – most of them characteristic of high-density emission nebulae. However, He 2-428 does not have a single Fe line, but does show the Ca IR triplet in emission. He 2-428 also has a quite strong continuum emission.

4.1. The central star of A 79

Figure 2 shows the low-resolution spectrum of the stellar-like object which is located roughly at the centre of symmetry of the nebular ring of A 79. At variance with He 2-428 and M 1-91, no nebular component is found in the core, and the spectrum is typical of a star of

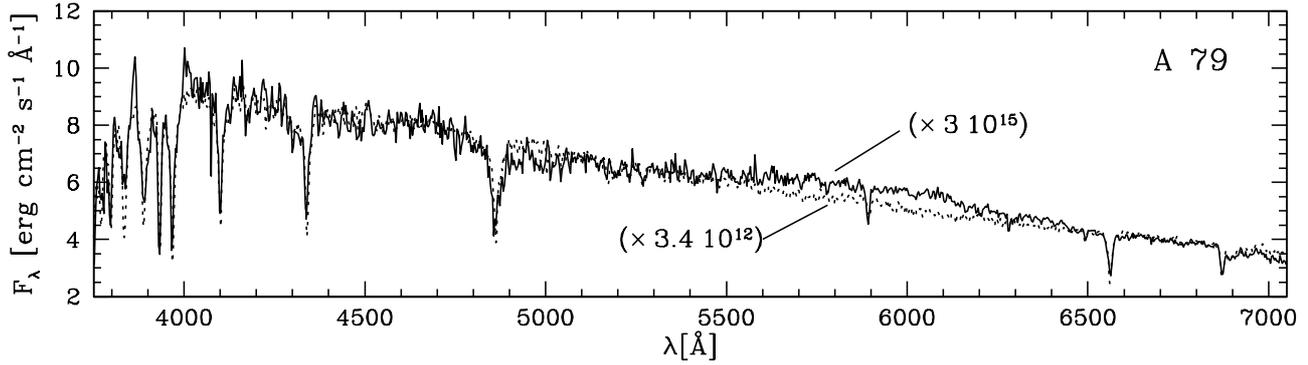


Fig. 2. The spectrum of the star at the symmetry centre of A 79 (continuous line) compared with an F0 V star spectrum (dotted line) from Jacoby et al. (1984). Both spectra have been normalized by the factors enclosed in parentheses.

intermediate spectral type. This stellar spectrum has been compared with those in the library of stellar spectra of Jacoby et al. (1984). The best visual fit is obtained with an F0 V star, whose spectrum is also shown in Fig. 2, but our spectrum does not allow us to exclude the adjacent spectral types or to define the luminosity class. The spectrum has been corrected for extinction using $A_V = 1.7$, the value leading to the best fit with the F0 V star spectrum. This value is equivalent to $c \simeq 0.7$, only somewhat higher than the optical depths found for the extended nebula of A 79 ($c = 0.39$ and 0.48), which supports the possibility that the star is in fact associated with the nebula. The agreement between the two spectra breaks in the range $\lambda\lambda 5500\text{--}6400$, where the central star of A 79 shows excess emission, a bump, over the comparison star. Similar excesses were found in two other field stars observed in the same exposure. The flux calibration was checked with another standard star and with data from different IRAF directories, but the bumps remained. They could be due to a deviation of the extinction curve from a linear trend around this wavelength region, known as the very broad structure in the extinction curve. The deviation seems to correlate with reddening and its origin is not well understood (see e.g. Jenniskens 1994). However, the deviation found for the central star of A 79, which amounts to ~ 0.1 mag, is higher than the value expected from its reddening, ~ 0.034 mag. Therefore, other explanations, including some uncontrolled instrumental effect, cannot be excluded.

4.2. The core of He 2-428

The spectrum of the nucleus of He 2-428 is shown in Figs. 3a and b; the measured and reddening-corrected intensities are listed in Table 2. The logarithmic extinction c has been calculated by fitting the ratios $I(\text{H}\alpha)/I(\text{H}\beta)$, $I(\text{H}\gamma)/I(\text{H}\beta)$, $I(\text{H}\delta)/I(\text{H}\beta)$, $I(\text{Pa}11)/I(\text{H}\beta)$ and $I(\text{Pa}12)/I(\text{H}\beta)$ to their recombination values for suitable physical conditions (see below). Optical depth effects might be affecting the H I intensities, as in M 1-91 (see Sect. 4.3), but since the

reddening-corrected ratios are within 10% of their recombination values for $\log(N_e) \sim 5.5$ and $T_e \sim 15\,000$ K, these effects, if present, must be small.

The extinction-corrected line ratios imply densities in the ranges: $\log(N_e[\text{S II}]) = 3.2\text{--}3.3$, $\log(N_e[\text{N II}]) = 5.1\text{--}5.5$, $\log(N_e[\text{O III}]) = 5.4\text{--}6.3$ for $T_e = 10\,000\text{--}20\,000$ K (with the highest values for $N_e[\text{N II}]$ and $N_e[\text{O III}]$ corresponding to the lower temperature).

The core shows a relatively strong continuum, with absorption lines from He II and some interstellar features. When corrected for reddening, the continuum and the absorption lines can be reproduced with an O5 star and an additional continuum component with an apparent onset at ~ 5000 Å. This additional component could be due to a late-type companion or arise in the line-emitting gas. The minimum contribution of this additional component to the observed continuum can be estimated by assuming that the continuum up to 5000 Å is mainly due to the hot star. We find that a minimum of 20–25% of the observed continuum should be due to this additional continuum component. The strongest source of nebular continuum that could produce an observable onset at 5000 Å, is the recombination continuum of H I. An estimate of its contribution to the observed continuum can be obtained from the intensity measured for H β and the emission coefficients for this line and the continuum (Osterbrock 1989). The result is that just a few percent of the observed continuum can be of nebular origin. Therefore, the additional continuum component is probably due to a late-type stellar companion of the hot star.

The spectrum in Fig. 3 shows also that the Ca II infrared triplet lines appear in emission, blended with three Paschen lines. The Ca II line intensities can be estimated by subtracting the expected contribution of the Paschen lines. This has been done by linearly interpolating the intensities of the surrounding Pa12, Pa14 and Pa17 lines. The three Ca II lines turn out to have very similar intensities, with $I(\lambda 8498)/I(\text{H}\beta) = 0.086$, $I(\lambda 8542)/I(\text{H}\beta) = 0.078$ and $I(\lambda 8662)/I(\text{H}\beta) = 0.062$, i.e. in the ratio 1.0:0.9:0.7, whereas the ratio for optically thin emission is 1:9:5. A near equality of the Ca II intensities is usually

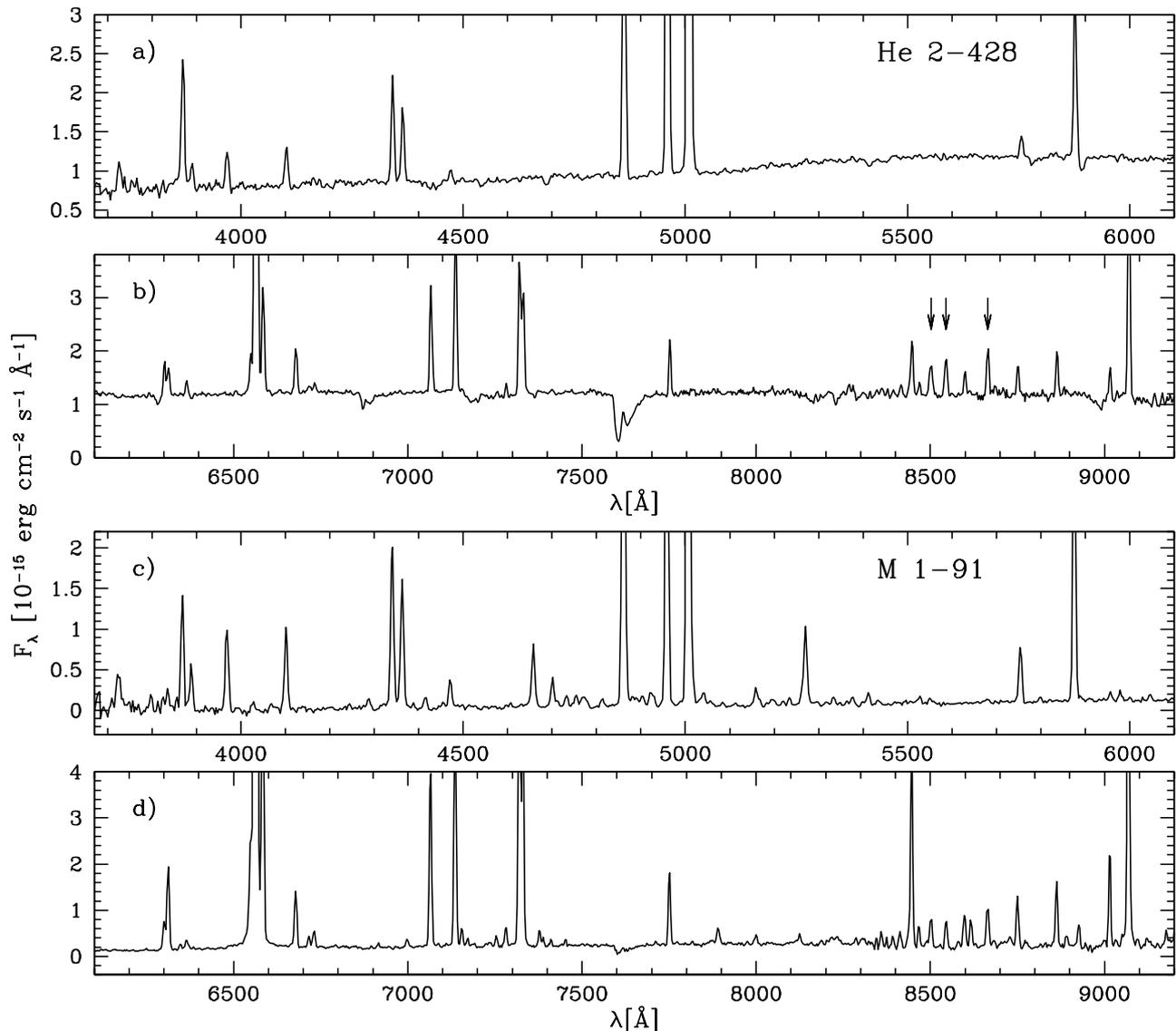


Fig. 3. Spectra of the cores of He 2-428 (a, b) and M 1-91 (c, d). The arrows in panel b) show the positions where the Ca II triplet lines appear in emission in He 2-428, blended with three Paschen lines.

found in all objects where the triplet is in emission and is explained as due to a high optical depth. The Ca II infrared triplet has been observed in emission in a variety of objects: some Be stars, high-luminosity young stellar objects (some with bipolar molecular outflows), certain active galactic nuclei, cataclysmic variable stars and T Tauri stars (Persson 1988a and references therein), symbiotic stars (Cieslinski et al. 1997) and the proto-planetary nebula He 3-401 (García-Lario et al. 1999). These objects support a dense neutral region in close proximity to a source of photons that is capable of ionizing Ca^+ – whose ionization potential is very low, 11.9 eV – unless it is well shielded. Therefore, for most of these Ca II triplet emitters, the emission is expected to arise in a disk. Some of the Ca II triplet emitters also show emission in $[\text{Ca II}] \lambda 7291$ and $\lambda 7324$, transitions which arise in the metastable lower levels of the triplet lines. These forbidden lines are suppressed at high densities, so that their absence in the core

of He 2-428 suggests $N_e > 10^{10} \text{ cm}^{-3}$ in the Ca II emitting region (Ferland & Persson 1989). Most of the Ca II emitters, unlike He 2-428, also show Fe II emission, which at least in active galactic nuclei seems to be correlated with Ca II emission (Persson 1988b), although the Ca II lines must arise in a more dense and optically thick material than Fe II emission.

4.3. The core of M 1-91

The spectrum of the core of M 1-91 is shown in Figs. 3c and d; the measured and reddening-corrected intensities are listed in Table 3. The relative intensities of the H I lines do not agree with case B expectations for any amount of reddening, implying that the core of M 1-91 must be optically thick in $\text{H}\alpha$ (Drake & Ulrich 1980). Since the amount of extinction has been estimated by averaging those derived for the outer regions of the nebulae

Table 2. Line intensities in the core of He 2-428.

| λ_{obs} | Identification | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | λ_{obs} | Identification | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} |
|------------------------|-----------------------------|-----------------------------|-------------------------|------------------------|----------------------------|-----------------------------|-------------------------|
| 3726.3 | [O II] 3726.0 + 3728.8 | 0.10 | 0.37 | 6678.8 | He I 6678.2 | 0.18 | 0.042 |
| 3869.4 | [Ne III] 3868.8 | 0.36 | 1.14 | 6718.1 | [S II] 6716.5 | 0.033 | 0.0077 |
| 3889.6 | He I 3888.7 + H8 3889.1 | 0.073 | 0.22 | 6732.5 | [S II] 6730.9 | 0.043 | 0.0098 |
| 3968.9 | [Ne III] 3967.5 + He 3970.1 | 0.11 | 0.30 | 7066.3 | He I 7065.3 | 0.42 | 0.081 |
| 4102.1 | H δ 4101.7 | 0.12 | 0.28 | 7136.9 | [Ar III] 7135.8 | 0.65 | 0.12 |
| 4341.4 | H γ 4340.5 | 0.27 | 0.49 | 7282.4 | He I 7281.4 | 0.049 | 0.0084 |
| 4364.1 | [O III] 4363.2 | 0.20 | 0.35 | 7321.0 | [O II] 7319.7 | 0.54 | 0.090 |
| 4471.9 | He I 4471.5 | 0.034 | 0.053 | 7331.5 | [O II] 7330.2 | 0.43 | 0.071 |
| 4862.3 | H β 4861.2 | 1.00 | 1.00 | 7752.6 | [Ar III] 7751.1 | 0.20 | 0.027 |
| 4923.6 | He I 4922.2 | 0.022 | 0.021 | 8416.0 | Pa19 8413.3 | 0.046 | 0.0044 |
| 4960.0 | [O III] 4958.9 | 2.05 | 1.83 | 8447.5 | O I 8446.5 | 0.26 | 0.025 |
| 5007.9 | [O III] 5006.8 | 6.42 | 5.48 | 8469.4 | Pa17 8467.3 | 0.061 | 0.0057 |
| 5756.4 | [N II] 5754.6 | 0.057 | 0.023 | 8501.5 | Ca II 8498.0 + Pa16 8502.5 | 0.16 | 0.015 |
| 5877.0 | He I 5875.7 | 0.41 | 0.17 | 8545.1 | Ca II 8542.1 + Pa15 8545.4 | 0.17 | 0.015 |
| 6302.3 | [O I] 6300.3 | 0.16 | 0.047 | 8599.6 | Pa14 8598.4 | 0.095 | 0.0083 |
| 6312.0 | [S III] 6312.1 | 0.14 | 0.040 | 8665.4 | Ca II 8662.1 + Pa13 8665.0 | 0.18 | 0.015 |
| 6364.8 | [O I] 6363.8 | 0.059 | 0.016 | 8751.8 | Pa12 8750.5 | 0.12 | 0.0094 |
| 6549.1 | [N II] 6548.0 | 0.12 | 0.031 | 8864.1 | Pa11 8862.8 | 0.18 | 0.014 |
| 6563.9 | H α 6562.8 | 11.6 | 2.89 | 9070.4 | [S III] 9068.9 | 1.17 | 0.101 |
| 6584.4 | [N II] 6583.4 | 0.42 | 0.10 | | | | |

$I(\text{H}\beta) = 4.0 \times 10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$
 $c = 1.63$
 $\text{Size} = 3''.7$

(see Sect. 4), and it is probably higher in the core, the reddening-corrected intensities are mainly given for illustrative purposes.

Line identifications rely on the comparison of the spectrum with those of He 2-25 and Th 2-B (Corradi 1995), M 8 (Esteban et al. 1999), η Car (Hamann et al. 1994), RR Tel (McKenna et al. 1997), IC 4997 (Hyung et al. 1994), the peculiar B[e] star HD 45677 (Swings 1973), and the tables by Moore (1945). The lines can have contributions of fainter transitions, mainly from [Fe II] and Fe II, and some weak lines of Mg II may also be present. The spectrum is very similar to those found in the cores of its sibling M 2-9 (as noted previously by Calvet & Cohen 1978 and Goodrich 1991) and other highly collimated planetary nebulae: He 2-25 and Th 2-B (Corradi 1995). The four objects have however different degrees of excitation and the intensities of the [Fe IV], [Fe III], [Fe II] and Fe II lines are also different, probably reflecting different conditions of density, and maybe, different evolutionary states.

The extinction-corrected line ratios, after allowing for a possibly somewhat higher extinction correction, imply densities in the ranges: $\log(N_e[\text{S II}]) = 3.55 \pm 0.10$, $\log(N_e[\text{N II}]) = 5.15 \pm 0.25$, $\log(N_e[\text{O III}]) = 6.4 \pm 0.4$, $\log(N_e[\text{Fe II}]) \sim 6$ and $\log(N_e[\text{Fe III}]) = 6.5 \pm 0.5$ for $T_e = 10\,000\text{--}20\,000$ K.

5. Chemical abundances in the lobes or rings

The measured line intensities for the extended areas (lobes or rings) of the three objects, along with the values derived for the logarithmic extinction c and the reddening-corrected relative intensities for all lines of interest are presented in Tables 4, 5 and 6.

The values for the temperatures $T_e[\text{N II}]$, densities $N_e[\text{S II}]$ and ionic abundances for the three nebulae, derived with the atomic data referenced in Sect. 2.4, are listed in Table 7. The [O III] $\lambda 4363$ line could be measured in both positions of M 1-91, but it has a poor signal-to-noise ratio, it could furthermore be contaminated by reflection from the core, and leads to temperatures up to 18 500 K, which are much higher than the temperatures derived from the [N II] lines (8600 and 8700 K) and have not been used in the abundance determination.

In A 79, where the intensity of He II $\lambda 4686$ is similar to that of H β , the H Balmer intensities in Table 4 include the contribution of the lines from the He Pickering series. This contribution was estimated using $I(\text{He II } \lambda 4861) = 0.05 I(\text{He II } \lambda 4686)$ and $I(\text{He II } \lambda 6563) = 0.134 I(\text{He II } \lambda 4686)$ (Storey & Hummer 1995). The line intensities used in the abundance determination for A 79 were consequently corrected by multiplying the line intensities in Table 4 by 1.06 (A 79 A) and 1.05 (A 79 B).

Table 3. Line intensities in the core of M 1-91.

| λ_{obs} | Identification | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | λ_{obs} | Identification | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} |
|------------------------|--|-----------------------------|-------------------------|------------------------|---|-----------------------------|-------------------------|
| 3724.5 | [O II] 3726.0 + 3728.8 | 0.099 | 0.23 | 5550.8 | N II 5552.0 ? | 0.0088 | 0.0055 |
| 3797.3 | H10 3796.9 | 0.024 | 0.053 | 5754.0 | [N II] 5754.6 | 0.10 | 0.057 |
| 3835.0 | H9 3835.4 | 0.030 | 0.063 | 5798.8 | [Fe IV] 5798.0 ($^4\text{G}^{-2}\text{D}$) | 0.0088 | 0.0049 |
| 3868.3 | [Ne III] 3868.8 | 0.19 | 0.39 | | [Fe IV] 5800.4 ($^4\text{G}^{-2}\text{D}$) | | |
| 3888.1 | He I 3888.7 + H8 3889.1 | 0.079 | 0.16 | 5875.4 | He I 5875.7 | 0.50 | 0.27 |
| 3968.3 | [Ne III] 3967.5 + He ϵ 3970.1 | 0.16 | 0.30 | 5956.8 | Si II 5957.6 | 0.012 | 0.0063 |
| 4027.3 | He I 4026.2 | 0.014 | 0.026 | 5978.4 | Si II 5978.9 | 0.018 | 0.0094 |
| 4101.4 | H δ 4101.7 | 0.15 | 0.26 | 6000.4 | [Ni III] 6000.2 (2F) | 0.012 | 0.0062 |
| 4243.9 | [Fe II] 4244.0 (21F) | 0.0083 | 0.013 | 6046.1 | O I 6046.4 | 0.012 | 0.0062 |
| 4287.2 | [Fe II] 4287.4 (7F) | 0.025 | 0.039 | 6300.3 | [O I] 6300.3 | 0.086 | 0.042 |
| 4388.0 | He I 4387.9 | 0.0064 | 0.0091 | 6312.0 | [S III] 6312.1 | 0.26 | 0.12 |
| 4340.3 | H γ 4340.5 | 0.31 | 0.45 | 6347.3 | Si II 6347.1 | 0.022 | 0.0096 |
| 4362.8 | [O III] 4363.2 | 0.25 | 0.36 | 6364.8 | [O I] 6363.8 | 0.041 | 0.018 |
| 4415.1 | [Fe II] 4416.3 (6F) | 0.023 | 0.032 | 6384.3 | Fe II 6383.8 (...) | 0.0044 | 0.0019 |
| 4455.0 | [Fe II] 4452.1 (7F) | 0.0059 | 0.0079 | 6547.3 | [N II] 6548.0 | 0.40 | 0.16 |
| | [Fe II] 4458.0 (6F) | | | 6564.8 | H α 6562.8 | 18.41 | 7.58 |
| 4471.0 | He I 4471.5 | 0.055 | 0.073 | 6583.1 | [N II] 6583.4 | 0.88 | 0.36 |
| 4606.6 | [Fe III] 4607.1 (3F) | 0.0054 | 0.0065 | 6678.1 | He I 6678.2 | 0.18 | 0.070 |
| 4657.9 | [Fe III] 4658.1 (3F) | 0.12 | 0.14 | 6716.0 | [S II] 6716.5 | 0.036 | 0.014 |
| 4701.2 | [Fe III] 4701.6 (3F) | 0.054 | 0.060 | 6730.7 | [S II] 6730.9 | 0.055 | 0.021 |
| 4712.2 | He I 4713.2 | 0.011 | 0.013 | 6915.4 | [Cr IV] 6914.8 (2F) | 0.014 | 0.0052 |
| 4732.7 | [Fe III] 4733.9 (3F) | 0.023 | 0.025 | 6998.3 | [Fe IV] 6997.1 ($^4\text{P}^{-2}\text{D}$) | 0.031 | 0.011 |
| 4754.0 | [Fe III] 4754.8 (3F) | 0.028 | 0.030 | 7065.2 | He I 7065.3 | 0.55 | 0.19 |
| 4771.6 | [Fe III] 4769.6 (3F) | 0.033 | 0.035 | 7088.0 | [Fe III] 7088.5 (15F) | 0.011 | 0.0037 |
| | [Fe III] 4777.7 (3F) | | | 7135.7 | [Ar III] 7135.8 | 0.75 | 0.25 |
| 4813.6 | [Fe II] 4814.6 (20F) | 0.020 | 0.021 | 7155.2 | [Fe II] 7155.1 (14F) | 0.061 | 0.021 |
| 4861.1 | H β 4861.2 | 1.00 | 1.00 | 7171.5 | [Fe II] 7172.0 (14F) | 0.026 | 0.0087 |
| 4881.9 | [Fe III] 4881.0 (2F) | 0.0080 | 0.0078 | 7225.0 | [Fe IV] 7222.9 ($^4\text{D}^{-4}\text{F}$) | 0.012 | 0.0040 |
| 4890.5 | [Fe II] 4889.6 (4F) | 0.0083 | 0.0081 | 7235.4 | C II 7236.2 | 0.021 | 0.0070 |
| 4905.2 | [Fe II] 4905.4 (20F) | 0.016 | 0.015 | 7254.2 | O I 7254.4 | 0.030 | 0.0099 |
| | [Fe IV] 4906.7 ($^4\text{G}^{-4}\text{F}$) | | | 7281.3 | He I 7281.4 | 0.057 | 0.019 |
| 4921.7 | He I 4921.9 | 0.031 | 0.030 | 7319.9 | [O II] 7319.7 | 0.96 | 0.31 |
| 4930.8 | [Fe III] 4930.5 (1F) | 0.013 | 0.012 | 7330.2 | [O II] 7330.2 | 0.75 | 0.24 |
| 4958.5 | [O III] 4958.9 | 0.80 | 0.74 | 7378.0 | [Ni II] 7377.9 (2F) | 0.0254 | 0.017 |
| 5006.5 | [O III] 5006.8 | 2.50 | 2.26 | 7387.8 | [Fe II] 7388.2 (14F) | 0.029 | 0.0092 |
| 5040.3 | Si II 5041.0 | 0.025 | 0.022 | 7411.5 | [Ni II] 7411.6 (2F) | 0.021 | 0.0066 |
| 5084.2 | [Fe III] 5084.8 (1F) | 0.0081 | 0.0069 | 7452.7 | [Fe II] 7452.5 (14F) | 0.019 | 0.0059 |
| 5112.4 | [Fe II] 5111.6 (19F) | 0.0054 | 0.0045 | 7712.3 | Fe II 7711.4 (73) | 0.012 | 0.0034 |
| 5159.5 | [Fe II] 5157.9 (19F) | 0.043 | 0.035 | 7750.9 | [Ar III] 7751.1 | 0.22 | 0.062 |
| | [Fe II] 5158.8 (18F) | | | 7816.2 | He I 7816.2 | 0.0095 | 0.0026 |
| 5194.9 | [Ar IV] 5191.8 | 0.022 | 0.018 | 7890.8 | [Ni III] 7889.9 (1F) | 0.068 | 0.019 |
| | [N II] 5197.9 + 5200.3 | | | 7999.2 | [Cr II] 7999.9 (1F) | 0.036 | 0.0091 |
| 5219.9 | [Fe II] 5220.1 (19F) | 0.0068 | 0.0053 | 8124.5 | [Cr II] 8125.2 (1F) | 0.042 | 0.010 |
| 5234.1 | [Fe IV] 5234.2 ($^4\text{G}^{-2}\text{F}$) | 0.0068 | 0.0053 | 8157.8 | Fe II 8157.5 ($\text{e}^6\text{D} - 5\text{p}^4\text{F}$) ? | 0.0076 | 0.0019 |
| | Fe II 5234.6 (49) | | | 8187.1 | N I 8188.0 | 0.021 | 0.0051 |
| 5270.3 | [Fe II] 5261.6 (19F) | 0.16 | 0.12 | 8345.1 | He I 8342.4 + Pa23 8345.6 | 0.028 | 0.0064 |
| | [Fe III] 5270.4 (1F) | | | 8359.5 | Pa22 8359.0 + He I 8361.7 | 0.058 | 0.013 |
| | [Fe II] 5273.4 (18F) | | | 8374.3 | Pa21 8374.5 | 0.022 | 0.0050 |
| 5317.9 | Fe II 5316.6 (49) | 0.0053 | 0.0039 | 8392.0 | Pa20 8392.4 | 0.031 | 0.0069 |
| 5333.6 | [Fe II] 5333.7 (19F) | 0.015 | 0.011 | 8412.9 | Pa19 8413.3 | 0.049 | 0.011 |
| 5348.0 | ? | 0.0027 | 0.0019 | 8446.3 | O I 8446.5 | 0.60 | 0.13 |
| 5363.9 | Fe II 5362.9 (48) | 0.0063 | 0.0045 | 8467.0 | Pa17 8467.3 | 0.069 | 0.015 |
| 5376.2 | [Fe II] 5376.5 (19F) | 0.014 | 0.0095 | 8501.6 | Pa16 8502.5 | 0.099 | 0.022 |
| 5411.8 | [Fe III] 5412.0 (1F) | 0.021 | 0.014 | 8545.5 | Pa15 8545.4 | 0.086 | 0.018 |
| 5433.9 | [Fe II] 5433.1 (18F) | 0.0074 | 0.0050 | 8580.5 | [Cl II] 8578.7 + He I 8582.5 | 0.028 | 0.0060 |
| 5526.5 | [Fe II] 5527.3 (17F) | 0.015 | 0.0096 | 8598.2 | Pa14 8598.4 | 0.11 | 0.024 |

Table 3. continued.

| λ_{obs} | Identification | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | λ_{obs} | Identification | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} |
|------------------------|----------------------|-----------------------------|-------------------------|------------------------|---|-----------------------------|-------------------------|
| 8616.6 | [Fe II] 8617.0 (13F) | 0.086 | 0.018 | 8862.7 | Pa11 8862.8 | 0.21 | 0.041 |
| 8664.7 | Pa13 8665.0 | 0.13 | 0.027 | 8891.5 | [Fe II] 8891.9 (13F) | 0.039 | 0.0076 |
| 8682.4 | N I 8680.2 + 8683.4 | 0.022 | 0.0046 | 8926.0 | Fe II 8926.7 ($e^4\text{D}-5p^4\text{D}$) | 0.069 | 0.013 |
| 8728.6 | [Fe III] 8728.9 (8F) | 0.034 | 0.0070 | 9014.8 | Pa10 9014.9 | 0.27 | 0.051 |
| 8750.3 | Pa12 8750.5 | 0.16 | 0.032 | 9068.7 | [S III] 9068.9 | 1.53 | 0.29 |
| 8840.0 | [Fe III] 8838.2 (8F) | 0.034 | 0.0070 | | | | |

$I(\text{H}\beta) = 5.7 \times 10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$
 $c = 1.04$
 $\text{Size} = 4''.1$

Table 4. Line intensities in the ring of A 79.

| A 79 A | | | A 79 B | | | Identification |
|------------------------|-----------------------------|-------------------------|------------------------|-----------------------------|-------------------------|----------------------|
| λ_{obs} | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | λ_{obs} | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | |
| 3727.6 | 2.27 | 3.32 | 3727.1 | 3.02 | 4.12 | [O II] 3726.0+3728.8 |
| 3868.2 | 1.38 | 1.94 | 3867.8 | 1.27 | 1.67 | [Ne III] 3868.8 |
| 4339.8 | 0.41 | 0.49 | 4340.6 | 0.48 | 0.55 | H γ 4340.5 |
| 4685.0 | 1.06 | 1.12 | 4685.1 | 0.84 | 0.88 | He II 4685.7 |
| 4860.8 | 1.00 | 1.00 | 4860.7 | 1.00 | 1.00 | H β 4861.2 |
| 4958.4 | 3.54 | 3.42 | 4958.5 | 2.56 | 2.50 | [O III] 4958.9 |
| 5006.2 | 10.75 | 10.24 | 5006.5 | 8.14 | 7.83 | [O III] 5006.8 |
| 5198.0 | 0.23 | 0.20 | 5199.0 | 0.26 | 0.24 | [N I] 5197.9+5200.3 |
| 5753.2 | 0.46 | 0.35 | 5754.6 | 0.45 | 0.36 | [N II] 5754.6 |
| 5875.8 | 0.15 | 0.11 | 5876.3 | 0.23 | 0.18 | He I 5875.7 |
| 6300.1 | 0.42 | 0.29 | 6300.6 | 0.58 | 0.43 | [O I] 6300.3 |
| 6311.5 | 0.17 | 0.12 | 6312.2 | 0.08 | 0.06 | [S III] 6312.1 |
| 6547.3 | 6.43 | 4.27 | 6547.9 | 7.69 | 5.52 | [N II] 6548.0 |
| 6562.1 | 4.24 | 2.81 | 6562.7 | 3.91 | 2.80 | H α 6562.8 |
| 6582.6 | 19.38 | 12.78 | 6583.1 | 22.36 | 15.98 | [N II] 6583.4 |
| 6715.7 | 1.43 | 0.92 | 6716.3 | 1.73 | 1.22 | [S II] 6716.5 |
| 6730.1 | 1.09 | 0.70 | 6730.6 | 1.37 | 0.97 | [S II] 6730.9 |

$I(\text{H}\beta) = 1.9 \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$ $2.2 \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$
 $c = 0.48$ 0.39
 $\text{Size} = 11''.8$ $8''.4$
 $d^a = 18''.5$ $24''.4$

^a Distance from the center of the extracted region to the central star.

The total abundances were derived by estimating the contribution of the unobserved ions using the relations of Kingsburgh & Barlow (1994); the results are presented in Table 8. An estimate of the Fe abundance for M 1-91 can be obtained from $\text{Fe}/\text{O} \simeq \text{Fe}^{++}/\text{O}^+ \simeq 0.01$, or about one fourth of the solar value.

The derived abundances can be compared with those found for 15 bipolar PNe by Perinotto & Corradi (1998) and Pottasch et al. (2000), and with the abundances measured in H II regions in the solar neighbourhood (Osterbrock 1992; Rodríguez 1999), also shown in Table 8. A 79 is among the richest PNe in N and He, and shows a

Table 5. Line intensities in the ring of He 2-428.

| He 2-428 A | | | He 2-428 B | | | Identification |
|------------------------|--|-------------------------|--|-----------------------------|-------------------------|----------------------|
| λ_{obs} | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | λ_{obs} | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | |
| 3727.1 | 0.70 | 1.97 | 3727.6 | 0.63 | 1.95 | [O II] 3726.0+3728.8 |
| 4101.9 | 0.18 | 0.36 | 4102.3 | 0.11 | 0.24 | H δ 4101.7 |
| 4340.4 | 0.32 | 0.51 | 4341.2 | 0.36 | 0.60 | H γ 4340.5 |
| 4861.9 | 1.00 | 1.00 | 4862.2 | 1.00 | 1.00 | H β 4861.2 |
| 4959.7 | 1.34 | 1.23 | 4959.8 | 1.29 | 1.17 | [O III] 4958.9 |
| 5007.7 | 4.15 | 3.66 | 5007.9 | 3.92 | 3.42 | [O III] 5006.8 |
| 5757.2 | 0.05 | 0.02 | 5753.2 | 0.06 | 0.03 | [N II] 5754.6 |
| 5876.7 | 0.34 | 0.16 | 5876.8 | 0.34 | 0.15 | He I 5875.7 |
| 6300.7 | 0.09 | 0.03 | 6302.0 | 0.15 | 0.05 | [O I] 6300.3 |
| 6549.0 | 0.75 | 0.25 | 6549.2 | 1.11 | 0.34 | [N II] 6548.0 |
| 6563.8 | 8.38 | 2.77 | 6564.0 | 9.32 | 2.80 | H α 6562.8 |
| 6584.3 | 2.22 | 0.73 | 6584.6 | 3.34 | 0.99 | [N II] 6583.4 |
| 6678.9 | 0.15 | 0.05 | 6679.5 | 0.14 | 0.04 | He I 6678.2 |
| 6716.8 | 0.25 | 0.08 | 6717.8 | 0.36 | 0.10 | [S II] 6716.5 |
| 6731.2 | 0.28 | 0.09 | 6732.2 | 0.42 | 0.12 | [S II] 6730.9 |
| 7066.6 | 0.17 | 0.05 | 7066.4 | 0.14 | 0.03 | He I 7065.3 |
| 7137.2 | 0.36 | 0.09 | 7137.1 | 0.41 | 0.10 | [Ar III] 7135.8 |
| 7320.8 | 0.20 | 0.05 | 7321.6 | 0.30 | 0.06 | [O II] 7319.7 |
| 7331.3 | 0.16 | 0.04 | 7332.1 | 0.18 | 0.04 | [O II] 7330.2 |
| 9070.4 | 1.44 | 0.18 | 9070.8 | 1.58 | 0.16 | [S III] 9068.9 |
| $I(\text{H}\beta)$ | $6.3 \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$ | | $6.8 \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$ | | | |
| c | 1.30 | | 1.41 | | | |
| $Size$ | 3''3 | | 3''3 | | | |
| d^a | 3''7 | | 3''7 | | | |

^a Distance from the center of the extracted region to the core.

Ne overabundance that could be real (Perinotto & Corradi 1998). M 1-91 and He 2-428 have a N/O abundance ratio one order of magnitude lower, unusual but not unique among bipolar PNe (cf. Fig. 8 in Perinotto & Corradi 1998). The O, S and Ar abundances in A 79 and M 1-91, and the Ne abundance in M 1-91, are essentially identical to those measured in nearby Galactic H II regions. This is not unexpected since the Galactocentric distances of the three PNe considered here are most probably between 6 and 10 kpc (this can be deduced from their distances: see Sect. 7), the same distance range covered by the H II regions whose abundances are given in Table 8. However, He 2-428 shows quite low abundances for most elements relative to H, when compared both with the H II regions and with the sample of bipolar PNe. In fact, the abundances are similar to those found for PNe belonging to the halo (Howard et al. 1997) and close to the abundances of some PNe classified as Peimbert's (1978) type III, i.e. belonging to an intermediate type between disc and halo nebulae (Maciel et al. 1990). This low metallicity suggests

that the central star of He 2-428 had a low-mass progenitor. The low upper limit derived for H₂ emission in this nebula by Guerrero et al. (2000) strengthens this conclusion, since H₂ emission in PNe seems to show some correlation with the mass of the progenitor star (Zuckerman & Gatley 1988).

6. Kinematics of A 79 and He 2-428

The expansion velocities of the rings of A 79 and He 2-428 have been derived by assuming that the rings are intrinsically circular so that their inclination i , or angle between the polar axis of the ring and the line of sight, can be estimated from the relative lengths of the major and minor semi-axis in the [N II] images. This inclination angle can then be used to deproject the velocities measured in the high-resolution spectra.

The ring of A 79, which is fragmented and broadened, is estimated to have its major semi-axis, equivalent to the ring radius, at a position angle $\text{PA} = 105^\circ \pm 5^\circ$ with size

Table 6. Line intensities in the lobes of M 1-91.

| M 1-91 A | | | M 1-91 B | | | Identification |
|------------------------|---|-------------------------|---|-----------------------------|-------------------------|-------------------------------|
| λ_{obs} | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | λ_{obs} | $(I_{\lambda}/I_{\beta})_0$ | I_{λ}/I_{β} | |
| 3726.7 | 0.90 | 1.95 | 3726.4 | 0.86 | 2.05 | [O II] 3726.0 + 3728.8 |
| 3868.5 | 0.039 | 0.076 | 3867.8 | 0.029 | 0.062 | [Ne III] 3868.8 |
| 4101.3 | 0.15 | 0.25 | 4101.3 | 0.16 | 0.29 | H δ 4101.7 |
| 4340.2 | 0.33 | 0.47 | 4340.0 | 0.33 | 0.49 | H γ 4340.5 |
| 4362.8 | 0.032 | 0.045 | 4362.2 | 0.012 | 0.018 | [O III] 4363.2 |
| 4471.0 | 0.043 | 0.056 | 4470.6 | 0.031 | 0.042 | He I 4471.5 |
| 4657.1 | 0.023 | 0.027 | 4657.5 | 0.020 | 0.023 | [Fe III] 4658.1 (3F) |
| 4861.0 | 1.00 | 1.00 | 4860.8 | 1.00 | 1.00 | H β 4861.2 |
| 4881.8 | 0.0095 | 0.0094 | 4882.3 | 0.0073 | 0.0072 | [Fe III] 4881.0 (2F) |
| 4922.0 | 0.017 | 0.017 | 4921.9 | 0.018 | 0.017 | He I 4921.9 |
| 4958.6 | 0.54 | 0.51 | 4958.4 | 0.56 | 0.52 | [O III] 4958.9 |
| 4985.6 | 0.0061 | 0.0057 | 4984.1 | 0.016 | 0.015 | [Fe III] 4985.9 + 4987.2 (2F) |
| 5006.6 | 1.69 | 1.53 | 5006.3 | 1.73 | 1.55 | [O III] 5006.8 |
| 5198.8 | 0.030 | 0.024 | 5198.0 | 0.030 | 0.023 | [N I] 5197.9 + 5200.3 |
| 5269.4 | 0.030 | 0.023 | 5270.0 | 0.025 | 0.018 | [Fe III] 5270.4 (1F) |
| 5753.9 | 0.037 | 0.022 | 5753.9 | 0.039 | 0.022 | [N II] 5754.6 |
| 5875.6 | 0.27 | 0.15 | 5875.2 | 0.27 | 0.14 | He I 5875.7 |
| 6300.0 | 0.074 | 0.035 | 6299.7 | 0.070 | 0.030 | [O I] 6300.3 |
| 6312.0 | 0.022 | 0.011 | 6311.7 | 0.023 | 0.010 | [S III] 6312.1 |
| 6364.0 | 0.023 | 0.011 | 6363.9 | 0.031 | 0.013 | [O I] 6363.8 |
| 6547.7 | 1.57 | 0.69 | 6547.6 | 1.84 | 0.73 | [N II] 6548.0 |
| 6562.7 | 6.54 | 2.87 | 6562.6 | 7.30 | 2.87 | H α 6562.8 |
| 6583.1 | 4.90 | 2.13 | 6582.6 | 5.73 | 2.23 | [N II] 6583.4 |
| 6677.6 | 0.086 | 0.037 | 6677.3 | 0.098 | 0.037 | He I 6678.2 |
| 6716.2 | 0.32 | 0.13 | 6715.8 | 0.35 | 0.13 | [S II] 6716.5 |
| 6730.6 | 0.45 | 0.19 | 6730.2 | 0.51 | 0.19 | [S II] 6730.9 |
| 7064.9 | 0.092 | 0.035 | 7064.4 | 0.11 | 0.036 | He I 7065.3 |
| 7135.7 | 0.30 | 0.11 | 7135.1 | 0.35 | 0.11 | [Ar III] 7135.8 |
| 7281.7 | 0.019 | 0.0067 | 7280.3 | 0.025 | 0.0078 | He I 7281.4 |
| 7320.0 | 0.096 | 0.033 | 7318.7 | 0.11 | 0.032 | [O II] 7319.7 |
| 7330.0 | 0.074 | 0.026 | 7329.2 | 0.097 | 0.029 | [O II] 7330.2 |
| 7750.6 | 0.088 | 0.027 | 7750.3 | 0.10 | 0.027 | [Ar III] 7751.1 |
| 8446.6 | 0.094 | 0.023 | 8446.3 | 0.068 | 0.014 | O I 8446.5 |
| 8545.4 | 0.021 | 0.0051 | 8543.3 | 0.045 | 0.0090 | Pa15 8545.4 |
| 8597.8 | 0.035 | 0.0083 | 8597.7 | 0.041 | 0.0079 | Pa14 8598.4 |
| 8664.4 | 0.047 | 0.011 | 8664.6 | 0.052 | 0.010 | Pa13 8665.0 |
| 8750.6 | 0.043 | 0.0098 | 8750.4 | 0.051 | 0.0095 | Pa12 8750.5 |
| 8862.1 | 0.058 | 0.013 | 8861.3 | 0.056 | 0.010 | Pa11 8862.8 |
| 9014.2 | 0.075 | 0.016 | 9014.6 | 0.12 | 0.020 | Pa10 9014.9 |
| 9068.7 | 1.16 | 0.24 | 9068.3 | 1.39 | 0.24 | [S III] 9068.9 |
| $I(\text{H}\beta)$ | $3.25 \times 10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$ | | $3.47 \times 10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$ | | | |
| c | 0.97 | | 1.10 | | | |
| $Size$ | 4''1 | | 4''1 | | | |
| d^a | 6''2 | | 6''2 | | | |

^a Distance from the center of the extracted region to the core.

Table 7. Physical conditions and ionic abundances (X^{i+}/H^+).

| Position | $N_e[\text{S II}]$ (cm^{-3}) | $T_e[\text{N II}]$ (K) | O^+ | O^{++} | N^+ | S^+ | S^{++} | Ar^{++} | Ne^{++} | He^+ | He^{++} | Fe^{++} |
|------------|--|---------------------------|--------------|-----------------|--------------|--------------|-----------------|------------------|------------------|---------------|------------------|------------------|
| He 2-428 A | 1100 | 13 700 | 2.7e-5 | 4.9e-5 | 6.9e-6 | 2.4e-7 | 2.6e-6 | 4.3e-7 | ... | 0.13 | ... | ... |
| He 2-428 B | 1200 | 14 500 | 2.2e-5 | 3.9e-5 | 8.4e-6 | 2.8e-7 | 2.1e-6 | 4.3e-7 | ... | 0.12 | ... | ... |
| M 1-91 A | 2400 | 8700 | 2.0e-4 | 8.8e-5 | 6.3e-5 | 1.5e-6 | 8.1e-6 | 1.4e-6 | 1.5e-5 | 0.11 | ... | 2.3e-6 |
| M 1-91 B | 2300 | 8600 | 2.2e-4 | 9.4e-5 | 6.8e-5 | 1.6e-6 | 8.3e-6 | 1.5e-6 | 1.3e-5 | 0.11 | ... | 1.6e-6 |
| A 79 A | 110 | 14 000 | 3.7e-5 | 1.4e-4 | 1.2e-4 | 1.9e-6 | 8.8e-6 | ... | 6.9e-5 | 0.095 | 0.102 | ... |
| A 79 B | 170 | 12 600 | 6.7e-5 | 1.4e-4 | 1.9e-4 | 3.2e-6 | 6.2e-6 | ... | 8.2e-5 | 0.15 | 0.078 | ... |

Table 8. Total abundances, $[X/H] = \log(X/H) + 12$.

| Position | $[\text{O}/\text{H}]$ | $\log(\text{N}/\text{O})$ | $[\text{N}/\text{H}]$ | $[\text{S}/\text{H}]$ | $[\text{Ar}/\text{H}]$ | $[\text{Ne}/\text{H}]$ | He/H |
|-------------------|-----------------------|---------------------------|-----------------------|-----------------------|------------------------|------------------------|----------------------|
| He 2-428 A | 7.88 | -0.59 | 7.30 | 6.51 | 5.90 | ... | ≥ 0.13 |
| He 2-428 B | 7.79 | -0.42 | 7.36 | 6.38 | 5.90 | ... | ≥ 0.12 |
| M 1-91 A | 8.46 | -0.50 | 7.97 | 6.98 | 6.41 | 7.69 | ≥ 0.11 |
| M 1-91 B | 8.49 | -0.51 | 7.98 | 7.00 | 6.45 | 7.63 | ≥ 0.11 |
| A 79 A | 8.45 | +0.50 | 8.94 | 7.18 | ... | 8.15 | 0.19 |
| A 79 B | 8.43 | +0.45 | 8.89 | 7.04 | ... | 8.20 | 0.21 |
| BPN ^a | 7.95 to 8.87 | -0.68 to +0.47 | 7.95 to 8.86 | 6.26 to 7.18 | 6.04 to 6.76 | 7.78 to 8.34 | 0.11 to 0.25 |
| H II ^b | 8.45 \pm 0.10 | -0.75 \pm 0.10 | 7.70 \pm 0.10 | 7.00 \pm 0.10 | 6.40 \pm 0.10 | 7.60 \pm 0.10 | ≥ 0.093 |
| M2-9 ^c | 8.36 | -0.57 | 7.79 | ... | ... | 7.41 | ≥ 0.10 |

^a A sample of 15 bipolar planetary nebulae (Perinotto & Corradi 1998; Pottasch et al. 2000).

^b H II regions in the solar neighbourhood (Osterbrock et al. 1992; Rodríguez 1999).

^c Derived from the line intensities presented by Barker (1978).

$a \simeq 11''.6$ and inclination $i = 49^\circ$. The ring of He 2-428 is more clearly defined, with its major semi-axis at PA = 82° , with $a = 6''.3$ and $i = 68^\circ$.

The velocities in the rings and lobes of the nebulae were measured by fitting Gaussian profiles to the [N II] $\lambda 6583$ line in the echelle spectra; this line was chosen since it has a lower thermal broadening than the $\text{H}\alpha$ line.

The slit orientations for A 79 were located $\sim 20^\circ$ off the major and minor axes of the ellipse that fits the ring in the image. The differences in velocity between opposite regions of the ring were found to be $\Delta V = 18 \text{ km s}^{-1}$, for the position near the minor axis (PA = 33°), and $\Delta V = 11 \text{ km s}^{-1}$ for the position near the major axis (PA = -57°). These velocities can be deprojected to the plane of the ring by using the expression $\Delta V/2 = V_{\text{exp}} \sin \varphi \sin i$, where $\tan \varphi = \tan \vartheta / \cos i$, and ϑ is the offset angle between the slit and the major axis of the ellipse. The deprojected velocities are consistent, within the errors, with the hypothesis of a circular ring expanding at $V_{\text{exp}} = 13 \pm 3 \text{ km s}^{-1}$ (its northern side approaching us and the southern one receding with respect to the core). Assuming a constant expansion velocity, its kinematical age is then $4300 D$ yrs, where D is the distance in kpc. The systemic velocity of A 79 is $-44 \pm 8 \text{ km s}^{-1}$ with respect to the Local Standard of Rest. No detailed

information is available for the expansion pattern in the faint, asymmetrical lobes.

In He 2-428, the long slit was oriented very close to the minor and major axes of the ring. As expected for an inclined expanding ring, no velocity difference was found between regions of the ring on either side of the central star along the major axis (PA = 80°), while a difference of $\Delta V = 28 \text{ km s}^{-1}$ was found along the minor axis (PA = -10°). Correcting for an inclination $i = 68^\circ$ ($V_{\text{exp}} = \Delta V/2 \sin i$), the deprojected expansion velocity of the ring is found to be 15 km s^{-1} , with the northern side receding and the southern one approaching us with respect to the core. Its kinematical age is $2000 D$ yrs, where D is the distance in kpc. The systemic velocity of He 2-428, as computed from the symmetry of the velocity field of the ring, is $70 \pm 8 \text{ km s}^{-1}$ in the frame of the Local Standard of Rest. The lobes show hints of expansion velocities larger by $\sim 20 \text{ km s}^{-1}$ than those in the ring, as usually found in bipolar PNe, but the signal is faint and no detailed spatiokinematical modeling was possible.

In the core of He 2-428, $\text{H}\alpha$ is found to have a relatively broad, double-peaked and asymmetrical profile. The full-width at zero intensity of the line is 137 km s^{-1} . This profile might reflect a complex velocity field in the unresolved circumstellar nebula, but its double peak, if not the

asymmetry, could be the consequence of transfer effects in a static stellar envelope (Magnan & de Laverny 1997).

The expansion velocities of the rings of He 2-428 and A 79 are low when compared with the usual expansion velocities of bipolar PNe, which go up to several hundred km s^{-1} (Corradi & Schwarz 1995). However, these high velocities are found in the polar directions of bipolar PNe, whereas the equatorial velocities of these objects are generally much lower (e.g. Corradi & Schwarz 1993), and similar to the velocities found for A 79 and He 2-428.

7. Discussion

The distances to A 79 and He 2-428 have been derived assuming that their measured systemic velocities reflect their participation in the general circular rotation around the Galactic centre. This is expected to be a good assumption for most bipolar PNe, since many of the characteristics of these objects relate them to the Galactic young disc population (Corradi & Schwarz 1995), but it could fail for He 2-428 if – as its low abundances may imply – this nebula is related to an older population.

For a standard Galactic rotation curve (cf. Corradi & Schwarz 1995), the distance to A 79 is found to be 5 ± 2 kpc, with the error taking into account the uncertainty in its derived systemic velocity and the dispersion in the velocity ellipsoids at a given location in the Galaxy. An independent estimate of the distance to A 79 can be obtained assuming that its central star belongs to the nebula. We have performed synthetic photometry on our low-resolution spectrum of this star to derive its V magnitude. Correcting for a light loss of 50% due to the narrow slit width, we derive $V = 16.7$ mag. Assuming that the star is not a supergiant and correcting the spectrum for a reddening $A_V = 1.3$ – 1.9 mag (each value obtained from the comparison of the observed spectrum with the spectra given by Jacoby et al. (1984) for stars of type F0 V, F0 IV, F0 III, F3 V or A9 V) we obtain $V = 14.8$ – 15.4 . These values, when compared with the absolute magnitudes expected for the corresponding spectral types (Schmidt-Kaler 1982) give a distance range 2.7–4.5 kpc, which is consistent with our distance estimate for A 79 given above and thus provides marginal evidence for the association of the star with the nebula. With a distance of 3–5 kpc, the age of the nebular ring of A 79 would be 13 000–21 500 yrs, its radius 0.17–0.28 pc, and the total size of the nebula 1.2–2.0 pc. Previous distance determinations for this object give 1.8–4.5 kpc (Zhang 1995 and references therein).

Assuming that the systemic velocity of He 2-428 is also due to its circular rotation around the Galactic centre, we find a distance between 4 and 8 kpc. For this distance range, the kinematical age of the ring would be 8000–16 000 yrs, its radius 0.12–0.24 pc and the total size of the nebula, including what is observed of the faint lobes, 1–2 pc. The possibility that He 2-428 is a type III PN (see Sect. 5), a class with peculiar velocities of ~ 64 km s^{-1} (Costa et al. 1996), casts some doubts on the derived parameters. However, previous distance determinations for

this object, based on independent methods, give a distance of 7.1–10.0 kpc (Zhang 1995 and references therein); the lower limit is consistent with our derived distance range and the upper limit implies negligible changes in the age and size derived for the nebula.

The ages derived for A 79 and He 2-428, $\geq 10^4$ yrs, imply that they are evolved PNe. At such ages, the stellar remnants are expected to have evolved to high temperatures and then to low luminosities in their post-AGB evolution, unless they have low masses. The large He and N abundances of A 79 suggest a high-mass progenitor (cf. Corradi & Schwarz 1995), but assuming that the star at its centre belongs to the system, its relative brightness and spectral type (F0) do not match those of an aged post-AGB nucleus. In the case of He 2-428, the central star is hidden within a compact gaseous envelope, partly neutral with very high densities ($N_e > 10^{10}$ cm^{-3} in the Ca II emitting region) and partly ionized with lower but still notable densities (N_e from $10^{3.3}$ to 10^6 cm^{-3} , see Sect. 4.2). The presence of this dense circumstellar envelope is clearly inconsistent with a post-AGB star 10^4 yrs after the ejection of the PN.

It has been proposed that the nuclei of proto-PNe and young PNe with anomalous spectral types, unable to produce the ionization observed in their nebulae, are rapidly evolving single stars that experience rapid increases of their temperature (up to a level at which the surrounding nebula gets ionized) following sporadic post-AGB mass loss episodes (see e.g. Bobrowsky et al. 1998). However, this cannot be the case for A 79 or He 2-428 because this scenario is expected to apply to the early phases of the post-AGB evolution, whereas these objects have quite old nebulae.

The simplest explanation of these observations is then that the central stars of both He 2-428 and A 79 are binaries. In the former, the nebular core would be produced by mass transfer effects in an interacting binary system, leading to the formation of a dense circumbinary nebula and possibly an accretion disc (e.g. Morris 1987; Soker & Rappaport 2001). In fact, He 2-428 might be similar to the symbiotic binaries R Aqr and V417 Cen (Solf & Ulrich 1985; van Winckel et al. 1994), which in addition of having a dense circumbinary core do also have bipolar/ring nebulae as He 2-428 (the similarity with the nebula of V417 Cen is especially striking). This would imply the presence in He 2-428 of a cool star with a strong wind, which could explain the red excess found in the spectrum (see Sect. 4.2).

As for A 79, the absence of nebular emission from the core suggests that no strong winds and mass transfer/exchange between the two stellar components are now present (this is expected for a system composed of an F star plus an aged post-AGB companion providing the ionization of the nebula). A similar case might be NGC 2346, which is known to have a binary central star (Feibelman & Aller 1983). Note that the presence of a binary system would also offer a natural explanation for the

collimation of the large bipolar nebulae of He 2-428 and A 79 (Soker & Rappaport 2001).

We have no constraints on the age of the nebula in M 1-91 and we cannot therefore exclude that it is very young and fits the single-star scenario above. However, the properties of its sibling M 2-9 also point to the presence of a binary system to produce the variety of its outflows (Doyle et al. 2000; Livio & Soker 2001). The similarity between M 1-91 and M 2-9 is not limited to the overall morphology. The available distances for M 1-91, of 7.0 or 7.8 kpc (Acker et al. 1992), imply a height over the Galactic plane $z = 440\text{--}490$ pc, to be compared with $z = 309$ pc for M 2-9 and a mean $\langle |z| \rangle = 130$ pc for a sample of 35 bipolar PNe (Corradi & Schwarz 1995). The chemical compositions of M 1-91 and M 2-9 are also similar, both at the lower limit or below the abundance range spanned by other bipolar PNe, as can be seen in Table 8, where the abundances shown for M 2-9 have been derived from the line intensities given by Barker (1978) and the same atomic data and ionization correction factors used for the other objects (see also Corradi & Schwarz 1995).

Finally, note that the departure from axisymmetry observed in the lobes of He 2-428 and A 79 (see Fig. 1), as well as in the symbiotic nebula V417 Cen (van Winckel et al. 1994), are all very similar to each other. This suggests that the asymmetry is not just due to irregular mass loss (e.g. caused by local mass loss events on the progenitor surface). A binary system (especially with an eccentric orbit) would also offer an explanation for the formation of such asymmetries (Soker & Rappaport 2001).

8. Summary and conclusions

We have presented a spectroscopical study of the bipolar PNe A 79, He 2-428 and M 1-91, with the following results:

- He 2-428 and M 1-91 have high density (from $10^{3.3}$ to $10^{6.5}$ cm^{-3}) unresolved nebular cores that indicate that strong mass loss/exchange phenomena are occurring close to their central stars.
- an additional region with densities larger than 10^{10} cm^{-3} is revealed in the core of He 2-428 by the presence of the Ca II infrared triplet in emission, possibly originating in an (accretion?) disk.
- an F0 star is found at the symmetry centre of the nebula of A 79. Its reddening and distance are consistent with the star being physically associated with the system, but radial velocity measurements of the stellar features would be needed to confirm this association.
- the continuum emission and the absorption lines in the core of He 2-428 can be reproduced with a hot star and an additional continuum component, which is probably due to a late-type stellar companion.
- while A 79 is overabundant in N and He, He 2-428 and M 1-91 have N/O abundance ratios one order of magnitude lower, but still within the range spanned by bipolar PNe.

- He 2-428 shows rather low abundances of all elements relative to H (excluding He), which suggests that it has arisen from a low-mass progenitor. This conclusion is strengthened by the absence of H₂ emission in the nebula (Guerrero et al. 2000).
- the nebulae of A 79 and He 2-428 are composed of tilted equatorial rings expanding at a velocity of ~ 15 km s^{-1} , from which faint and irregular lobes depart. The nebulae are evolved, with ages $\geq 10^4$ yrs.

The associations of these old nebulae with a dense nebular core (He 2-428) or with a central star with F0 spectral type (A 79) are interpreted as evidence for the binarity of their nuclei. In the literature, another dozen of bipolar PNe are known to possess very dense nebular cores or central stars with anomalous spectral types (see Corradi 1995). They provide prime targets for future observational studies, by means of radial velocity monitoring or IR and UV imaging and photometric searches for companions, aimed at testing the idea that *all* bipolar PNe contain binary systems.

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